Social Health Insurance: 
A Quantitative Exploration

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Social Health Insurance: A Quantitative Exploration*

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Abstract

We quantify the welfare implications of three alternative approaches to providing health insurance: (i) a US-style mix of private and public health insurance, (ii) compulsory universal public health insurance (UPHI) and (iii) private health insurance for workers combined with government subsidies and price regulation. We use a Bewley-Grossman lifecycle model calibrated to match the lifecycle structure of earnings and health risks in the US. For all three systems we find that welfare gains triggered by a combination of improvements in risk sharing and wealth redistribution dominate welfare losses caused by tax distortions and ex-post moral hazard effects. Overall, the UPHI system outperforms the other two systems in terms of welfare gains if the coinsurance rate is properly designed. A direct comparison between the US system to a well-designed UPHI system reveals that large welfare gains are possible in the long-run. However, such a radical reform faces political impediments due to opposing welfare effects across different income groups.

JEL: I13, D52, E62, H31

Keywords: Health capital, lifecycle health risk, incomplete insurance markets, social insurance, optimal policy, dynamic general equilibrium with idiosyncratic shocks.

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1 Introduction

Health risk is an important source of uncertainty over the lifecycle. A common view in the health insurance literature is that health risk is not easily insurable via private health insurance markets. This is mainly due to do the nature of the risk itself (e.g., autocorrelated shocks and age dependent shock magnitudes) and information asymmetries, both of which result in insurance market failures and call for government intervention (e.g., see Rothschild and Stiglitz (1976)).\footnote{The institution of social health insurance can also be justified on other grounds including high administration costs of private health insurance systems, altruism, free riding issues, optimal taxation problems, equity reasons including redistribution of wealth and health capital across and within age cohorts (e.g., see Blomqvist and Horn (1984a), Besley (1988), Culyer and Wagstaff (1995), Cremer and Pestieau (1996), Zweifel and Manning (2000) as well as Nyman (2003)).}

The purpose of this paper is to quantify the welfare implications of different approaches to providing social health insurance using a stylized model calibrated to the US.

Many countries have introduced some kind of collective financing of health care services via taxes or direct contributions (Carrin and James (2005)). Public (social) health insurance systems are often characterized by mandatory membership, open enrollment and community rating. However, there is no uniform approach to the public provision of health insurance across OECD countries. Most European countries publicly finance a compulsory public health insurance system with almost universal insurance coverage where voluntary private health insurance provides supplementary insurance. The US, on the other hand, has a mixed health insurance system with a significant market-based component. Public health insurance covers retirees and low income individuals, whereas private health insurance covers most of the working population as can be seen in Figure 1. These two distinct approaches result in significant differences in insurance take-up rates, the fraction of cost sharing, the level of health expenditures at the individual and aggregate levels as well as the share of private vs. public contributions to total health expenditures. The latter is depicted in Figure 2.

In the health insurance literature the introduction of public health insurance can be justified by the classic trade-off between insurance and incentive effects. The public provision of health insurance decreases adverse selection issues and usually institutes more equitable risk sharing which is referred to as the insurance effect. On the other hand, a social health insurance program needs to be financed by mandatory contributions or taxes which distort household incentives to consume, save and work. In addition, health insurance in general triggers a moral hazard problem. The literature summarizes these distortions under the umbrella of the incentive effect.\footnote{Compare Spence and Zeckhauser (1971), Pauly (1974), Blomqvist and Horn (1984b), Besley (1988), Besley (1989), Manning and Marquis (1996), Nyman (1999) and Petretto (1999).} Arguably, a government-based approach with a universal public health insurance system has the advantage of eliminating the adverse selection issue; but it increases the adverse effects on incentives due to moral hazard and large tax distortions. Conversely, mixed systems that employ significant shares of both, government- and market-based approaches, cannot completely eliminate the adverse selection issue which leads to inefficient market outcomes with low insurance take-up rates, especially among low income groups. However, the mixed system triggers
smaller tax distortions due to the smaller size of the public health insurance component.

Every design of a social health insurance system trades-off these insurance and incentive effects. The literature mentioned above is inconclusive about which approach results in better overall welfare outcomes. The answer to this question hinges on the economic fundamentals of the modeling environment including production technologies, endowments, the risk structure and household preferences for risk exposure, efficiency and equity. A welfare ranking of different health insurance systems depends on how the insurance and incentive trade-off plays out quantitatively. In this paper we formulate a dynamic general equilibrium framework with a healthcare sector to quantify the welfare implications of various designs of health insurance systems.

More specifically, we develop a Bewley model with individual income risk and incomplete markets (Bewley (1986)) and incorporate key features from the Grossman health capital model (Grossman (1972a)) under uncertainty. Our Bewley-Grossman lifecycle model is able to capture the lifecycle structure of health risk in conjunction with income risk as observed in the data. In the model individuals value their health in addition to a consumption goods basket. Health affects the labor market productivity of workers so that health serves as a consumption and as an investment good. Individuals subsequently smooth their consumption in the presence of idiosyncratic earnings shocks using a limited set of instruments. In addition to earnings shocks individuals are also exposed to idiosyncratic health shocks. Individuals choose to invest in their health via purchases of medical services. The inclusion of health capital into the model endogenizes health care spending and health insurance take-up rates so that they are jointly determined with consumption, savings and the supply of labor over the lifecycle. Elements of adverse selection and ex-post moral hazard in health expenditures are thus present in our framework.\(^3\)

To discipline our quantitative analysis we require our benchmark model to match the lifecycle patterns of shocks to income and health, labor supply, asset holdings, consumption and health expenditures in the US. Health expenditures are low early in life because of low health risk for young individuals. They subsequently rise as the probability of negative health shocks increases and health capital depreciates. On average, health expenditures rise exponentially later in life because individuals are exposed to more frequent and larger health shocks. Our benchmark model also reproduces the hump-shaped lifecycle profile of insurance take-up rates in the US. Finally, our model replicates the income distribution from the Panel of Income Dynamics (PSID) as well as macroeconomic aggregates from national income accounts (NIPA).

We use the calibrated model to quantitatively explore the welfare implications of different approaches to providing social health insurance. We compare three distinct health insurance systems: (i) a US-style mixed private-public health insurance system, (ii) a government-based system with compulsory universal public health insurance (UPHI), and (iii) a market-based system with only private health insurance for working individuals in combination with government

\(^3\)Ex-ante moral hazard (i.e., increasing the probability of health shocks when insured) and self-protection (i.e., reducing the probability of health shocks by being more prudent) are not present in the model.
subsidies and price regulations.

We first construct a baseline case for comparison where we remove all private and public health insurance arrangements from the calibrated version of the model. In this laissez-faire competitive economy individuals are forced to self-finance all health expenditures. We are thus able to quantify the substantial welfare cost that a complete lack of insurance contracts would impose on a society with economic fundamentals similar to the US economy. This is a well-known result from a large literature (e.g., Deaton (1991), Huggett (1993), Aiyagari (1994) and Levine and Zame (2002)). In our model idiosyncratic risk enters in two ways. First, idiosyncratic wage income shocks enter on the right hand side of the individual’s budget constraint. Second, idiosyncratic health shocks translate into (health) expenditure risk on the left hand side of the budget constraint. The lack of market instruments to insure against health risk interacts with the limited set of market instruments against income risk (i.e., essentially constrained household savings and adjustments of the labor supply) and amplifies the welfare cost of augmented consumption variance viz-a-viz a standard Bewley model without health risk. In our model the overall welfare cost is the sum of the cost of missing insurance against income risk, the cost of incomplete health insurance against health risk and the interaction between the two.

Since individuals are risk-averse they benefit, at least in expectation, from health insurance contracts that insure partially against health risk. We start the analysis with an assessment of how well the benchmark US health insurance system –pre Affordable Care Act (ACA) in 2010– compares to a laissez-faire economy without any insurance. Retirees and poor individuals benefit from public insurance through Medicare and Medicaid, while working individuals have the option to participate in private health insurance markets. This mixed system fails to eliminate adverse selection and therefore does not provide universal insurance take-up. Still, the US system results in significant welfare gains across all income groups when compared to an economy without any health insurance contracts. The overall welfare gain is large at about 5.2 percent of compensating equivalent consumption variation (CEV) measured as percent of lifetime consumption of a newborn individual.

In a second step we evaluate a universal public health insurance (UPHI) system against the no insurance case. Not surprisingly we observe a significant reduction of self-insurance via savings that leads to a 12 percent decline in the long-run capital stock. The share of GDP spent on health care increases due to an ex-post moral hazard effect. As GDP falls, the health expenditure to GDP ratio increases even further. Tax distortions add to the negative income effect. We summarize these effects under the umbrella of negative efficiency effects due to the publicly financed health insurance system. On the other hand, adverse selection effects completely disappear as the entire population enters the insurance pool which leads to improvements in the allocation of risk and subsequent welfare gains. Since the model exhibits a negative correlation between labor productivity and health risk, public health insurance financed by flat taxes implicitly redistributes wealth and subsequently improves welfare of the high-risk

\[4\text{In our related work in Jung and Tran (2016) we analyze the long-run effects of the ACA.}\]
low-income cohorts. This outcome is triggered by positive insurance/redistributive effects. The dominating effect (incentive vs. insurance) will determine whether or not public health insurance is socially desirable –measured as welfare gains/losses over laissez-faire– for the economy as a whole. Our result implies that the positive insurance effect is dominant. In addition, we are able to identify “optimal” coinsurance rates for UPHI that result in welfare gains over US-style mixed systems as they better balance the insurance and incentive effects and are not negatively affected by adverse selection.

Next we explore the extent to which a more market-based approach can reduce the health risk exposure. We first consider a setting in which only private health insurance is available for working-age individuals (we still allow for Medicare for the old) without any further government regulation. This is similar to an insurance market that is only comprised of individual health insurances (IHI) where insurers are relatively free to adjust insurance premiums and are allowed to price discriminate between different risk groups. We find that IHI markets by themselves are not maintainable due to an adverse selection spiral. However, once the government introduces additional regulation on insurance premiums, medical prices and tax deductibility of insurance premiums similar to group health insurance plans (GHI) in the US system, private health insurance becomes viable with insurance take-up rates close to 83 percent among the active working population. Welfare gains can be realized but they are relatively small compared to the welfare gains generated by the US and UPHI systems. The main reason is that income is not redistributed as forcefully as under systems with a larger public insurance component.

In our final experiment we compare the outcome of a US-type insurance system to a UPHI system. We find that the UPHI system with sufficiently large coinsurance rates outperforms the US health insurance system in terms of efficiency and welfare. This outcome is mainly driven by welfare gains of low income groups as middle and high income groups would actually prefer the US system over the UPHI system. The opposing welfare effects highlight the political challenge associated with radically reforming the US system into a UPHI system.

**Related Literature.** Our work is connected to different branches of the quantitative macroeconomics and health economics literature. First, our paper is related to the literature on incomplete markets macroeconomic models with heterogeneous agents as pioneered by Bewley (1986) and extended by Huggett (1993) and Aiyagari (1994). This model has been applied widely to quantify the welfare cost of public insurance for idiosyncratic income and longevity risks (e.g., Hubbard and Judd (1987), Hansen and Imrohoroglu (1992), Imrohoroglu, Imrohoroglu and Joines (1995), Golosov and Tsyvinski (2006), Heathcote, Storesletten and Violante (2008), Conesa, Kitao and Krueger (2009), Krueger and Perri (2011) and Huggett and Parra (2010)). This literature shows that if the ability of risk sharing in private markets is limited, then publicly provided risk sharing mechanisms improve the allocation of risk and increase welfare. This literature focuses on the welfare cost triggered by labor income risk in combination with a lack of insurance for non-medical consumption. In this paper, we extend this literature by incorporating health risk and medical consumption into the Bewley framework. This allows us to analyze the welfare cost of shocks to both, income and health when no insurance
instruments are available.

A number of studies address health risk and precautionary savings (e.g., Kotlikoff (1988), Levin (1995), Hubbard, Skinner and Zeldes (1995) and Palumbo (1999)). These studies commonly assume exogenous health expenditure shocks. More recent contributions to this literature have incorporated exogenous health expenditure shocks into large-scale dynamic general equilibrium models which are then used to evaluate the macroeconomic effects of health insurance reforms (e.g., Jeske and Kitao (2009), Imrohoroglu and Kitao (2012), Pashchenko and Porapakkarm (2013) and Braun, Kopecky and Koreshkova (2015)). Unlike these studies we consider the micro-foundations of health capital accumulation and therefore endogenize decisions on health care expenditures and health insurance take-up. We are therefore able to account for the two-way interaction between insurance status and health expenditures which is an important determinant of the behavioral response (i.e., ex-post moral hazard) arising from changes in the insurance system.

Our work can be viewed as a quantitative extension of the Grossman health capital model. The roots of the health accumulation process in our model are established in the Grossman literature on health capital (Grossman (1972a) and Grossman (1972b)). Follow-up studies in health economics concentrate on examining the theoretical and empirical micro-foundations of medical spending. Grossman (2000) provides a review of this literature. However, the Grossman literature abstracts from matching the models directly to the stylized facts of health related lifecycle behaviors as they tend to be rather parsimonious. We extend the Grossman model and incorporate health shocks, private insurance choice, a realistic institutional setting and general equilibrium channels. We demonstrate that a calibrated version of our generalized Grossman model can generate the lifecycle patterns of health expenditures and the take-up rates of different types of private health insurance in US data. More recent lifecycle models include medical and non-medical consumption e.g., Suen (2006), Hall and Jones (2007), Jung and Tran (2008), Yogo (2009), De Nardi, French and Jones (2010), Feng (2010), Hugonnier, Pelgrin and St-Amour (2013), Fonseca et al. (2013) and Scholz and Seshadri (2013). We differ from these papers in that we explore an optimal approach to providing social health insurance in a richer institutional environment. This paper is closely related to our own work in Jung and Tran (2016) where we follow a similar modeling approach and analyze the long-run effects of the Affordable Care Act.

Our paper contributes to the literature on optimal insurance and government redistribution (e.g., Blomqvist and Horn (1984b), Rochet (1991) and Cremer and Pestieau (1996)) as well as the literature on mixed public-private health insurance systems (e.g., Besley (1989), Selden (1997), Blomqvist and Johansson (1997), Petretto (1999) and Chetty and Saez (2010)). These studies analytically investigate the optimal structure of mixed insurance systems in terms of efficiency and equity in rather simplified models. We extend this literature and provide a quantitative analysis using more realistic assumptions. First, we take general equilibrium effects from price changes in factor markets and insurance markets on savings and health care expenditures into account. Second, the formation of health insurance premiums, the price of medical care, interest
rates and wage rates is simultaneously determined in insurance, medical care, capital and labor markets, respectively. Third, we account for the interactions between distortionary taxes and individual’s economic behavior.

The paper is structured as follows. Section 2 describes the insurance and incentive trade off in a two-period model. Section 3 presents the full dynamic model. Section 4 describes our calibration strategy. Section 5 describes our experiments and quantitative results. Section 6 concludes. The Appendix presents all calibration tables figures.

2 A Two Period Model with Health Risk

We start by demonstrating how the public provision of health insurance can improve welfare when health risks are present and markets are incomplete.

Environment. We consider a two period overlapping generations model. Young individuals in period 1 work and earn labor income. They subsequently retire in period 2 and live on their savings. Each cohort has measure one. The health state $h_2$ of retired individuals is a random variable with density $f(h_2)$. The health state subsequently determines the level of health care expenditures $m(h_2)$ in the second period. Insurance markets are assumed to be incomplete so that agents are not able to share health risk across households and generations. They rely on their precautionary savings as self-insurance device.

Health Risk and Demand for Insurance. A young individual knows the distribution of future health states, $f(h_2)$, but not the specific health state that she will end up in when old. At the beginning of period 1, the individual decides on consumption, labor supply and savings to maximize expected utility, while forming an expectation about her future health $h_2$. The optimization problem can be written as

$$V(\Gamma_1) = \max_{c_1, n_1, s_1, c_2} \left( u(c_1) - \theta v(n_1) + Eu(c_2, h_2) \right) \text{ s.t.}$$

$$c_1 + s_1 = n_1 w_1 \text{ and } c_2 + m_2 = R s_1,$$

where $Eu(c_2, h_2) = \{ u(c_2, h_2) f(h_2) \, dh_2 \}$ is expected utility derived from health and consumption, $w_1$ and $R$ are the market wage and interest rates, respectively, $c_1$ is consumption and $n_1$ is labor supply when young, $s_1$ is saving, $c_2$ is consumption when old, $m_2 = m(h_2) \geq 0$ is the health expenditure in the second period as a function of health status. Note that, it is assumed that the utility functions $u(c), v(n)$ and $u(c, h)$ have standard properties: $u_c > 0, \ v_n > 0, \ u_n > 0, \ ucc < 0.$ The F.O.Cs for the household problem are: $u_{c_1} \quad (c_1) = \theta \gamma_{\phi} (n_1)$ and $u_{c_1} (c_1) = R \beta Eu_{c_2} (c_2, h_2).$ Let $\Gamma_1$ denote the state variable vector. The individual’s optimal decision rules are $c_1 = g^c(\Gamma_1), \ n_1 = g^v(\Gamma_1)$ and $s_1 = g^r(\Gamma_1)$ and the value function with no health insurance is $V(\Gamma_1)$.

In our setting agents are risk averse. Since no health insurance option is available they are forced to self-insure against health risk by “oversaving.” Young agents are therefore willing to pay more than the actuarially fair premium for an insurance contract that eliminates future
health expenditure risk which creates demand for health insurance.
Social Health Insurance. In the absence of well functioning health insurance markets, the presence of health risk gives rise to government intervention through tax-transfer programs that provide alternative mechanisms for pooling health risk across households. We consider a government-run health insurance program for retirees where the government sets coinsurance rate \( \gamma \) which determines the fraction of total health expenditure that individuals end up paying out-of-pocket. In order to finance the program the government imposes a tax rate \( \tau \) on labor income in period 1 so that \( \tau n_{1w1} = (1 - \gamma)m(h_2)f(h_2)dh_2 \). Let \( \Gamma_2 \) denote the state variable vector in this setting so that the optimization problem can be written as

\[
V(\Gamma_2) = \max_{c_1, h_1, s_1, c_2} \mathcal{C} \quad \begin{array}{l}
u(c_1) - \theta v(n_1) + Eu(h_2, c_2) \text{ s.t.} \\
c_1 + s_1 = 1, \quad c_2 + \gamma m_2 = R s_1.
\end{array}
\]

The optimal decision rules are \( c_1^* = g^c(\Gamma_2), n_1^* = g^n(\Gamma_2) \) and \( s_1^* = g^s(\Gamma_2) \) and the value function with a public health insurance program is \( V(\Gamma_2) \).

In our second-best setting the provision of public health insurance institutes more equitable risk sharing across retirees which results in welfare gains. We refer to this as the insurance effect. On the other hand, the public health insurance program needs to be financed by taxes which distort household incentives to work and save in period 1 which tends to cause welfare losses. We refer to these distortions as the incentive effect. The introduction of a public health insurance program is often justified based on the classic trade-off between insurance and incentive effects. If the insurance effect is dominant, welfare gains are realized, \( V(\Gamma_2) > V(\Gamma_1) \).

An optimal design of a public health insurance program is obtained when the system efficiently trades-off between insurance and incentive effects. We next consider an optimal policy problem in which the government chooses the coinsurance rate of the public health insurance system \( \gamma \) and the tax rate \( \tau \) to maximize a social welfare function that weighs each individual equally subject to (i) balancing the government budget constraint and (ii) solving household optimization problems. In our framework, each agent has a known and common wage income when young but face uncertain future health states. Old agents are thus heterogeneous in their health status and their second period utilities. The government’s objective function takes this distribution into account and chooses a coinsurance rate \( \gamma \) and a tax rate \( \tau \) so that the aggregate expected lifetime welfare is maximized. The government problem can be written as

\[
W = \max_{\gamma, \tau} \quad \{ \begin{array}{l} -\theta v(n) + 2u(h, z)f(h)dh \text{ s.t.} \\
\tau n_{1w1} = (1 - \gamma)m_2f(h_2)dh_2, \\
c_1 = g^c(\Gamma_2), \quad n_1 = g^n(\Gamma_2) \text{ and } s_1 = g^s(\Gamma_2).
\end{array} \}
\]

Evaluating the government’s F.O.Cs yields the optimal coinsurance rate as

\[
\gamma^* = 1 - \frac{\beta R (u_{c2}m_2f(h_2))dh_2 - u_{c1}\mu}{u_{c1}\mu^\prime n_{1}}.
\]
where $\mu = \{ m(h_2) f(h_2) \, dh_2 \}$ is the average health expenditure and $n_1^t = \frac{\partial n_1}{\partial t}$. 
This expression illustrates the classic trade-off that determines how much social insurance should be provided through a public health insurance program. A quantitative judgment of this trade-off is challenging. How the trade-off plays out depends on economy-based fundamentals such as preferences, endowments including income and health risks, the evolution of health capital over the lifecycle, the insurance market structure and institutional settings. In the next section, we therefore formulate a more realistic model of the US economy where some of these factors are taken into account. We then quantify the welfare implications of different approaches to designing a health insurance system and search for the optimal coinsurance rate.

3 A Full Model with Income and Health Risk

3.1 Demographics

The economy is populated with overlapping generations of individuals who live to a maximum of $J$ periods. Individuals work for $J_1$ periods and then retire for $J - J_1$ periods. In each period individuals of age $j$ face an exogenous survival probability $\pi_j$. Deceased agents leave an accidental bequest that is taxed and redistributed equally to all working-age agents alive. The population grows exogenously at an annual net rate $n$. We assume stable demographic patterns, so that age $j$ agents make up a constant fraction $\mu_j$ of the entire population at any point in time. The relative sizes of the cohorts alive $\mu_j$ and the mass of individuals dying $\tilde{\mu}_j$ in each period (conditional on survival up to the previous period) can be recursively defined as $\mu_j = \frac{\pi_j}{(1+n)^{\text{years}}\mu_{j-1}}$ and $\tilde{\mu}_j = \frac{1}{1+n}^{\text{years}}\mu_{j-1}$, where years denotes the number of years per model period.

3.2 Endowments and Preferences

In each period individuals are endowed with one unit of time that can be used for work $l$ or leisure. Individual utility is denoted by function $u(c, l, h)$ where $u : R^3_+ \to R$ is $C^2$, increases in consumption $c$ and health $h$, and decreases in labor $l$. Individuals are born with a specific skill type $\theta$ that cannot be changed over their lifecycle and that together with their health state $h_j$ and an idiosyncratic labor productivity shock $\tilde{E}_j^l$ determines their age-specific labor efficiency $e^{\theta, h_j, E_j^l}$. The transition probabilities for the idiosyncratic productivity shock $E_j^l$ follow an age-dependent Markov process with transition probability matrix $\Pi^l$. An element of this transition matrix is defined as the conditional probability $\Pr\left(\tilde{E}_{i,j+1}^l | \tilde{E}_{i,j}^l\right)$, where the probability of next period’s labor productivity $\tilde{E}_{i,j+1}^l$ depends on today’s productivity shock $\tilde{E}_{i,j}^l$.

3.3 Health Capital

Health capital depreciates at rate $\delta_j^h$. In addition, individuals face idiosyncratic health shocks $E_j^h$. Individuals can buy medical services $m_j$ at price $p_m$ to improve their health capital as in
Grossman (1972a). Health capital therefore evolves according to

\[ h_j = i \cdot m_j, h_{j-1}, \delta^h, E_j^h, \]  

(1)

where \( h_j \) denotes current health capital and \( h_{j-1} \) denotes health capital of the previous period. The exogenous health shock \( E_j^h \) follows a Markov process with age dependent transition probability matrix \( \Pi^h \). Transition probabilities to next period’s health shock \( E_{j+1}^h \) depend on the current health shock \( E_j^h \) so that an element of transition matrix \( \Pi^h \) is defined as the conditional probability \( \Pr(E_{j+1}^h | E_j^h) \).

### 3.4 Technologies and Firms

The economy consists of two production sectors. The two sectors are assumed to grow at a constant rate \( g \). In sector one, there is a representative firm that uses physical capital \( K \) and effective labor services \( L \) to produce non-medical consumption goods \( c \) with a normalized price of one. The firm in the non-medical sector are perfectly competitive and solve the following maximization problem

\[
\max_{K, L} \{ F(K, L) - qK - wL \},
\]  

(2)

taking the rental rate of capital \( q \) and the wage rate \( w \) as given. Capital depreciates at rate \( \delta \) in each period. Sector two, the medical sector, is also populated by a continuum of identical firms that use capital \( K_m \) and labor \( L_m \) to produce medical services \( m \) at a price of \( p_m \). The representative firm in the medical sector chooses capital \( K_m \) and effective labor \( L_m \) in order to maximize its profit according to

\[
\max_{K_m, L_m} \{ p_m F_m(K_m, L_m) - qK_m - wL_m \}.
\]  

(3)

### 3.5 Government

The government engages in a number of activities via various government programs: social security program, social insurance programs, a general consumption program and an accidental bequest redistribution program. The social security program operates on the basis of the Pay-As-You-Go (PAYG) principle in which the government collects a payroll tax \( \tau^{SS} \) from the working population to finance social security benefits of \( t^{SS} \) per retired household. The PAYG program is self-financed.

In addition, the government provides social insurance through a public health insurance program \( (M^G) \) and a social transfer program \( (T^{SI}) \) that guarantees a minimum consumption level. The government also operates a government spending program \( (G) \) that is exogenous and unproductive. The government collects consumption tax revenue at a flat rate, \( \tau^C \), and income tax revenue at a progressive rate to balance its budget every period. Finally, the government collects and redistributes accidental bequests \( i^{Beq}_j \) in a lump-sum fashion to each working-age household.
3.6 Household Problem

Agents with age \( j \leq J_1 \) are workers and thus exposed to labor shocks. Old agents, \( j > J_1 \), are retired \((l_j = 1)\) and receive pension payments. They do not face labor market shocks anymore. The agent state vector at age \( j \) is given by

\[
x_j \in D_j \equiv \begin{cases} 
\{ a_j, h_{j-1}, \theta_j, E_j, \ell^{h_j}, \ln_j \} & \in R_+ \times R_+ \times R_+ \times R+ \times I \quad \text{if } j \not\in J_1, \\
\{ a_j, h_{j-1}, \theta_j, E_j, \ell^{h_j}, \ln_j \} & \in R_+ \times R_+ \times R_+ \times R- \times I \quad \text{if } j > J_1,
\end{cases}
\]

where \( a_j \) is the capital stock at the beginning of the period, \( h_{j-1} \) is the health state at the beginning of the period, \( \theta \) is the skill type, \( E_j \) is the positive labor productivity shock, \( E^h_j \) is a negative health shock, \( \ln \) is the insurance state and \( I \) denotes the dimension of the insurance state. After the realization of the state variables, agents simultaneously chose from their choice set

\[
\mathcal{C}_j \equiv \begin{cases} 
\{ c_j, l_j, m_j, a_{j+1}, \ln_{j+1} \} & \in R_+ \times [0, 1] \times R_+ \times R+ \times I \quad \text{if } j \leq J_1, \\
\{ c_j, m_j, a_{j+1}, \ln_{j+1} \} & \in R_+ \times R_+ \times R_+ \times I \quad \text{if } j > J_1,
\end{cases}
\]

where \( c_j \) is consumption, \( l_j \) is labor supply, \( m_j \) are health care services, \( a_{j+1} \) are asset holdings for the next period and \( \ln_{j+1} \) is the insurance state for the next period in order to maximize their lifetime utility. All choice variables in the household problem depend on state vector \( x_j \). We suppress this dependence in the notation to improve readability. The household optimization problem is

\[
V (x_j) = \max_{\{C_j\}} \{ u(c_j, h_j, l_j) + \beta \pi_j E[V (x_{j+1}) | x_j] \} \text{ s.t.} \quad (5)
\]

\[
0 \leq a_{j+1}, \ 0 \leq l_j \leq 1, \text{ and } (1),
\]

where \( o(m_j) \) is out-of-pocket medical spending, \( i(\ln_{j+1}) \) is the net contribution of the insurance system, \( y_j \) is the sum of all income including labor, assets and bequests, \( \text{tax}_j \) is total income taxes paid and \( \text{tax}^{SS}_j \) is the social security tax. Household income and tax payments are defined as

\[
y_j = \begin{cases} 
\ell^j \times h_j \times w + R(a_j + \hat{h} + i^{SS}) j & \text{if } j \leq J_1, \\
\ell^{SS} + R(a_j + \ell^{beq} + t^{SS}) j & \text{if } j > J_1,
\end{cases}
\]

\[
\text{tax}_j = \tilde{\tau}(\tilde{y}_j),
\]

\[
\text{tax}_j = y_j - a_j - \ell^{beq} - 0.5 \times \text{tax}^{SS}_j.
\]

\[
(6)
\]

\[
13
\]
\[ \text{tax}_{j}^{ss} = \tau^{ss} \times \min \left\{ \bar{y}_{ss}, e^{\theta}, h_{j}, E_{j} \times l_{j} \times w \right\}, \]
\[ t_{j}^{sl} = \max \left\{ 0, \zeta + \theta (m_{j}) + \text{tax}_{j} - y_{j} \right\}. \]
Variable \( w \) is the market wage rate and \( R \) is the gross interest rate. Variable \( \tilde{y}_j \) is taxable income, \( \tilde{t} (\tilde{y}_j) \) is the progressive income tax payment and \( \tau x_j \) is the social security tax with marginal rate \( \tau^S_j \) that finances the social security payments \( \tau^S_j \). The maximum contribution to social security is \( \tilde{y}_{ss} \). The social insurance payment \( \tau^i_j \) guarantees a minimum consumption level \( c \). If social insurance is paid out, then automatically \( a_{j+1} = 0 \), so that social insurance cannot be used to finance savings.

The contribution of the insurance system \( i (\text{in}_{j+1}) \) depends on the design of the health insurance system and may include premium payments, tax contributions to public insurance, tax refunds and shares in insurance company profits.

For each \( x_j \in D \), let \( \Lambda (x_j) \) denote the measure of age \( j \) agents with \( x_j \in D \). Then expression \( \mu_j \Lambda (x_j) \) becomes the population measure of age-\( j \) agents with state vector \( x_j \in D \) that is used for aggregation.

### 3.7 Recursive Equilibrium

Given transition probability matrices \( \prod_{j=1}^{J} \{ \mu_j \} \) and exogenous government policies \( \text{tax}(x_j), \tau^c, \tau^S, \tilde{y}_{ss} \) a competitive equilibrium is

\[
\{ c_j (x_j), l_j (x_j), a_{j+1} (x_j), m_j (x_j), \text{in}_{j+1} (x_j) \}_{j=1}^{J} \]

a collection of sequences of distributions \( \{ \mu_j, \Lambda (x_j) \}_{j=1}^{J} \) of individual household decisions \( \{ c_j (x_j), l_j (x_j), a_{j+1} (x_j), m_j (x_j), \text{in}_{j+1} (x_j) \}_{j=1}^{J} \), aggregate stocks of physical capital and effective labor services \( \{ K, L, K_m, L_m \} \), and factor prices \( \{ w, q, R, p_m \} \) such that

(a) \( \{ c_j (x_j), l_j (x_j), a_{j+1} (x_j), m_j (x_j), \text{in}_{j+1} (x_j) \}_{j=1}^{J} \) solves the consumer problem (5),

(b) the firm first order conditions hold in both sectors

\[
\begin{align*}
w & = F_L (K, L) = p_m F_{m.L} (K_m, L_m), \\
q & = F_K (K, L) = p_m F_{m.K} (K_m, L_m), \\
& = q + 1 - \delta,
\end{align*}
\]

(c) markets clear

\[
\begin{align*}
K + K_m & = \sum_{j=1}^{J} \mu_j (a (x_j)) d\Lambda (x_j) + \sum_{j=1}^{J} \tilde{\mu}_j a_j (x_j) d\Lambda (x_j), \\
L + L_m & = \sum_{j=1}^{J} \mu_j e_j (x_j) l_j (x_j) d\Lambda (x_j),
\end{align*}
\]
(d) the aggregate resource constraint holds

\[
G + (1 + g)S + \sum_{j=1}^{r} \mu_j (c(x_j) + p_m m(x_j)) \Lambda(x_j) = Y + p_m Y_m + (1 - \delta) K, 
\]
(e) the government programs clear
\[ \sum_{j=J_1}^{J_2} \mu_j \int_{x_j} \text{tax} GHI \ d\Lambda(x_j) = \sum_{j=J_1}^{J_2} \mu_j \int_{x_j} \text{tax} SSI \ d\Lambda(x_j), \]

\[ M^G + \sum_{j=1}^{J_1} \mu_j \int_{x_j} \text{tax} SSI \ d\Lambda(x_j) + G = \sum_{j=1}^{J_1} \mu_j \int_{x_j} \text{tax} C(x_j) + \text{tax} \ d\Lambda(x_j), \]  

(f) the accidental bequest redistribution program clears
\[ \sum_{j=J_1}^{J_2} \mu_j \int_{x_j} \text{tax} \ Beq \ d\Lambda(x_j) = \sum_{j=J_1}^{J_2} \mu_j \int_{x_j} \text{tax} \ d\Lambda(x_j), \]

(g) the insurance system is self-financed so that insurance payouts over all participants equal premium contributions and/or earmarked tax collections and

(h) the distribution is stationary \( \mu_{j+1}, \Lambda(x_{j+1}) = T_{\mu,\Lambda}(\mu_j, \Lambda(x_j)) \) where \( T_{\mu,\Lambda} \) is a one period transition operator on the distribution.

3.8 Health Insurance Systems

We now specify three approaches to providing social health insurance: System [1] is a mixed private-public health insurance system similar to the US system. System [2] is a universal public health insurance system. System [3] is a private health insurance system for workers.

3.8.1 System 1: Mixed Public/Private US-Style Health Insurance

The health insurance systems consist of private health insurance companies and public health insurance programs. Insurance companies offer two types of health insurance policies: an individual health insurance plan (IHI) and a group health insurance plan (GHI). IHI can be bought by any agent for an age and health dependent premium, \( \text{prem}_{IHI}(j, h) \). GHI can only be bought by workers who are randomly matched with an employer that offers GHI which is indicated by a binary random variable \( E_{GHI} = 1 \). The insurance premium, \( \text{prem}_{GHI} \), is tax deductible and group rated so that insurance companies are not allowed to screen workers by health or age. If a worker is not offered group insurance from the employer, i.e., \( E_{GHI} = 0 \), the worker can still buy IHI. In this case the insurance premium is not tax deductible and the insurance company screens the worker by age and health status.

There is a Markov process that governs the group insurance offer probability. The Markov process is a function of the permanent skill type \( \vartheta \) of an individual. Let \( \Pr(E_{GHI} | E_{GHI}, \vartheta) \) be
We discuss the specifics of the insurance system in the following sections.
the conditional probability that an agent has group insurance status \( L_{j+1}^{\text{GHI}} \) at age \( j+1 \) given she had group insurance status \( L_j^{\text{GHI}} \) at age \( j \). The \( 2 \times 2 \) transition probability matrix \( \Pi_{j,j+1}^{\text{GHI}} \) collects all conditional probabilities for group insurance status.

Individuals are required to buy insurance one period prior to the realization of their health shock in order to be insured in the following period. The insurance policy needs to be renewed each period. By construction, agents in their first period are thus not covered by any insurance.

The government runs two public health insurance programs, Medicaid for the poor and Medicare for retirees. To be eligible for Medicaid, individuals are required to pass an income and asset test. The health insurance state \( i_n \) for workers can therefore take on the following values:

\[
    i_n = \begin{cases} 
        0 & \text{if not insured}, \\
        1 & \text{if Individual health insurance (IHI)}, \\
        2 & \text{if Group health insurance (GHI)}, \\
        3 & \text{if Medicaid}.
    \end{cases}
\]

After retirement (\( j > J_1 \)) all agents are covered by public health insurance which is a combination of Medicare and Medicaid for which they pay a premium, \( \text{prem}^R \).

An agent’s total health expenditure in any given period is \( p_{i_n} \times m \), where the price of medical services \( p_{i_n} \) depends on insurance state \( i_n \). The out-of-pocket health expenditure of a working-age agent is given by

\[
o(m_j) = \begin{cases} 
    
    p_{i_n} m_j \gamma_{i_n} & \text{if } i_n = 0, \\
    p_{i_n} m_j & \text{if } i_n > 0
    \end{cases}
\]

where \( 0 \leq \gamma_{i_n} \leq 1 \) are the insurance state specific coinsurance rates. The coinsurance rate denotes the fraction of the medical bill that the patient has to pay out-of-pocket.\(^6\) A retiree’s out-of-pocket expenditure is \( o(m_j) = \gamma^R \times \left( p_{m} \times m_j \right) \), where \( \gamma^R \) is the coinsurance rate of Medicare and \( p_{m} \) is the price that a retiree pays for medical services.

**Household Optimization.** The state vector for the household optimization problem includes one additional dimension for workers due to the employer matching shock \( E^{\text{GHI}} \):

\[
x_j \in D_j \equiv \begin{cases} 
    \left( a_j, h_{j-1}, g_j, E_j^{\text{GHI}}, i_n \right) & \in \mathbb{R}_+ \times \mathbb{R}_+ \times \mathbb{R}_+ \times \mathbb{R} \times \{0,1\} \times \{0,1,2,3\} & \text{if } j \leq J_1, \\
    \left( a_j, h_{j-1}, g_j, E_j^{\text{GHI}}, i_n \right) & \in \mathbb{R}_+ \times \mathbb{R}_+ \times \mathbb{R}_+ \times \{0,1\} & \text{if } j > J_1.
    \end{cases}
\]

The household choice set is defined as

\[
    \mathcal{C}_j \equiv \begin{cases} 
    \left( c_j, l_j, m_j, a_{j+1}, i_n \right) & \in \mathbb{R}_+ \times [0,1] \times \mathbb{R}_+ \times \mathbb{R}_+ \times \{0,1,2,3\} & \text{if } j \leq J_1, \\
    \left( c_j, m_j, a_{j+1} \right) & \in \mathbb{R}_+ \times \mathbb{R}_+ \times \mathbb{R}_+ & \text{if } j > J_1.
    \end{cases}
\]

\(^6\)For simplicity we include deductibles and copays into the coinsurance rate.
For simplicity we include deductibles and co-pays into the coinsurance rate.
The insurance system component that enters the household problem is

\[ i \{ i = 1 \} \text{prem}^{\text{HII}}(j, h) + 1 \{ i \{ i = 1 \} \} \text{prem}^{GHI} + \text{tax}^{\text{Med}} - \left( \text{profits}^M + \text{profits}^L \right) \]

for each age individual maximizing

\[ j \text{prem}^{\text{Med}} - \left( \text{profits}^M + \text{profits}^L \right) \]

where \( 1 \{ i = 1 \} \) and \( 1 \{ i = 2 \} \) are indicator variables that are equal to one if the individual chooses the respective insurance state and zero otherwise. Medicare is financed by a payroll tax \( \text{tax}^{\text{Med}} \) and premium payments \( \text{prem}^{\text{Med}} \). Per capita provider profits are denoted \( \text{profits}^M \) and per capita insurance company profits are denoted \( \text{profits}^L \). Taxable income \( \tilde{y}_j \) now includes provider profits, GHI premium deductions and payroll tax deductions from Medicaid payments:

\[ \tilde{y}_j = y_j + \text{profits}^M + \text{profits}^L - a_j - \frac{\text{tax}^{\text{SS}}}{\text{tax}^{\text{Med}}} \]

\[ \text{tax}^{\text{SS}} = \tau^{\text{SS}} \times \min \left \{ \tilde{y}_j, \left \{ \tilde{y}_j, \left \{ \tilde{y}_j, \left \{ \tilde{y}_j \right \} \right \} \right \} \right \} \]

\[ \text{tax}^{\text{Med}} = \tau^{\text{Med}} \times \left \{ \tilde{y}_j, \left \{ \tilde{y}_j, \left \{ \tilde{y}_j, \left \{ \tilde{y}_j \right \} \right \} \right \} \right \} \]

where \( \tau^{\text{Med}} \) is a payroll tax financing Medicare.

**Insurance Sector.** For simplicity we abstain from modeling insurance companies as profit maximizing firms and simply allow for a premium markup \( \omega \). Since insurance companies in the individual market screen customers by age and health, we impose separate clearing conditions for each age-health type, so that premium, \( \text{prem}^{\text{HII}}(j, h) \), adjusts to balance

\[ \left( 1 + \omega^{\text{HII}} \right) \mu_j \left[ \text{prem}^{\text{HII}}(j, h) \right] = R \mu_j \left[ \text{prem}^{\text{HII}}(j - 1, h) \right] \]

where \( x_{j-1} \) is the state vector for cohort age \( j \) not containing \( h \) since we do not want to aggregate over the health state vector \( h \) in this case. The clearing condition for the group health insurances is simpler as only one price, \( \text{prem}^{GHI} \), adjusts to balance

\[ \left( 1 + \omega^{GHI} \right) \mu_j \left[ \text{prem}^{GHI}(j, x) \right] = R \mu_j \left[ \text{prem}^{GHI}(j, x) \right] \]
where $\omega_{HI}$ and $\omega_{GHI}$ are markup factors that determine loading costs (fixed costs or profits), $\gamma_{HI}$ and $\gamma_{GHI}$ are the coinsurance rates, and $p_{IH}^m$ and $p_{GHI}^m$ are the prices for health care services of the two insurance types. The respective left-hand-sides in the above expressions summarize aggregate payments made by insurance companies whereas the right-hand-sides aggregate the premium collections one period prior. Since premiums are invested for one period, they enter the capital stock and we therefore multiply the term with the after tax gross interest rate $R$. 
The premium markups generate profits that are redistributed in equal (per-capita) amounts, denoted \( \text{profit}^\text{In} \), to all surviving agents.\(^7\)

Medicare is financed by a Medicare tax and premium payments and together with Medicaid enter the government budget in the following way:

\[
G + T^{SL} + \sum_{j=1}^{J_1} \mu_j \int_{[m(x)=3]} \left( 1 - \gamma^{\text{Maid}} \right) p^{\text{Maid}} m_j(x_j) d\Lambda(x_j)
\]

\[
+j = 2 \sum_{j=2}^{J} \mu_j \left( 1 - \gamma^R \right) p^{m} R m_j(x_j) d\Lambda(x_j)
\]

\[
+ \sum_{j=J_1+1}^{J} \mu_j \int_{m(x)=3} \left( r \right) \left( c(x_j) + \text{tax}_{m_j}(x_j) \right) d\Lambda(x_j) + \sum_{j=J_1+1}^{J} \mu_j \text{prem}^R(x_j) d\Lambda(x_j) + \sum_{j=1}^{J_1} \mu_j \text{tax}^\text{Med} d\Lambda(x_j),
\]

where \( \gamma^{\text{Maid}} \) and \( \gamma^R \) are the coinsurance rate of Medicaid and of the combined Medicare/Medicaid program for the old, respectively.

### 3.8.2 System 2: Universal Public Health Insurance

The universal public health insurance system (UPHI system) is mandatory and financed by taxes. In this setting, the out-of-pocket health expenditures of the household are given by

\[
o(m_j) = \gamma^{\text{UPHI}} \times \frac{c_j}{p_{m_j}^\text{UPHI}},
\]

where \( \gamma^{\text{UPHI}} \) is the coinsurance rate of the UPHI program and \( p_{m_j}^\text{UPHI} \) is the price that providers charge uniformly.

**Household Optimization.** The state vector for the household optimization problem is

\[
x_j \in D_j \equiv \begin{cases} \left\{ a_j, h_{j-1}, \partial_j E_{j-1}, in_j \right\} & \in R_+ \times R_+ \times R_+ \times \{1\} & \text{if } j \neq J_1, \\ \left\{ a_j, h_{j-1}, \partial_j, E_j, in_j \right\} & \in R_+ \times R_+ \times R_+ \times \{1\} & \text{if } j > J_1, \end{cases}
\]

the household choice set is

\[
\zeta_j \equiv \begin{cases} \left\{ c_j, l_j, m_j, a_j+1 \right\} & \in R_+ \times [0,1] \times R_+ \times R_+ & \text{if } j \leq J_1, \\ \left\{ c_j, m_j, a_j+1 \right\} & \in R_+ \times R_+ \times R_+ & \text{if } j > J_1, \end{cases}
\]

and the insurance system component that enters the household problem is either

\[
i \left( in_j = \text{UPHI} \right) = \tau_c \times c_j \text{ for } \forall j,
\]

\(^7\)Notice that ex-post moral hazard and adverse selection issues arise naturally in the model due to information.
asymmetry. Insurance companies cannot directly observe the idiosyncratic health shocks and have to reimburse agents based on the actual observed levels of health care spending. Adverse selection arises because insurance companies cannot observe the risk type of agents and therefore cannot price insurance premiums accordingly. They instead have to charge an average premium that clears the insurance companies’ profit conditions. Individual insurance contracts do distinguish agents by age and health status but not by their health shock.
if a consumption \( \tau_c \) is used to finance the system or

\[
i \left( in_j = \text{UPHI} \right) = \begin{cases} 
0 & \text{if income} < $200,000 \text{ and } j \leq J_1, \\
\tau_v \times e \left( \partial, h_j, E^j, l_jW \right) & \text{if income} \geq $200,000 \text{ and } j \leq J_1, 
\end{cases}
\]

if an earmarked payroll tax \( \tau_v \) on high income earners is used.  

**Insurance Sector.** The UPHI system results in aggregate insurance payments of

\[
\text{InsPay}_{\text{UPHI}} = \sum_{j=1}^{J_1} \mu_j \left( 1 - \gamma \right) \text{UPHI} p^{\text{UPHI}} m_j(x_j) d\Lambda (x_j). 
\]

The system is balanced. In the case with the consumption tax financing the system the government budget constraint changes to

\[
\text{InsPay}_{\text{UPHI}} + G + T_{\text{SI}} = \sum_{j=1}^{J_1} \mu_j \left( 1 - \gamma \right) \text{UPHI} p^{\text{UPHI}} m_j(x_j) d\Lambda (x_j). 
\]

If a payroll tax finances the UPHI system then

\[
\text{InsPay}_{\text{UPHI}} = \sum_{j=1}^{J_1} \mu_j \tau_v \times e_j(x_j) l_j(x_j) w \ d\Lambda (x_j) \tag{13}
\]

has to hold in addition to the government budget constraint in expression (8).

### 3.8.3 System 3: Private Health Insurance for Workers

We model two cases. First we analyze an unregulated market where premiums are priced according to the health state and age of a worker (similar to IHI in the US system). We then discuss a regulated market where (i) the government does not allow insurance companies to price discriminate based on health status and age and (ii) the government gives tax credits to individuals who buy private insurance. This market is similar to group health insurance plans (GHI) in the US system. Medicaid for workers is not available anymore. Retired workers are still insured via a Medicare type program.

The premiums for the two cases are again denoted by \( \text{prem}^{\text{IHI}} (j, h) \) or \( \text{prem}^{\text{GHI}} \), respectively. The health insurance state \( \text{in}_j \) for workers can therefore take on the following values:

\[
in_j = \begin{cases} 
0 & \text{if not insured}, \\
1 & \text{if privately insured (either IHI or GHI)}. 
\end{cases}
\]

After retirement (\( j > J_1 \)) all agents are covered by a public health insurance program which is a
combination of Medicare and Medicaid for which they pay a premium, prem. The out-of-pocket

The ACA uses a similar payroll tax on high income earners to finance components of the insurance expansion. See our earlier work in Jung and Tran (2016) for details.
health expenditures of a worker depend on the insurance state

\[
o (m_j) = \begin{cases} 
\gamma^{inj} \times p^{inj} m_j & \text{if } in_j = 0, \\
\gamma^{inj} \times p^{inj} m_j & \text{if } in_j > 0,
\end{cases}
\]

where \(0 \leq \gamma^{inj} \leq 1\) are the insurance type specific coinsurance rates. A retired agent’s out-of-pocket health expenditure is \(o (m_j) = \gamma^R \times p^R m_j\), where \(\gamma^R\) is the coinsurance rate of Medicare and \(p^R\) is the price that a retiree pays for medical services.

**Household Optimization.** The state vector for the household optimization problem is

\[
x_j \in D_j = \begin{cases} 
-c_j, h_{j-1}, a_j, \theta_j, E^j, j, in_j \in R_+ \times R_+ \times R_+ \times R_+ \times \{0, 1\} & \text{if } j \not\in J_1, \\
-c_j, h_{j-1}, a_j, \theta_j, E^j, j, in_j \in R_+ \times R_+ \times R_+ \times R_+ \times \{1\} & \text{if } j > J_1,
\end{cases}
\]

the household choice set is

\[
C_j = \begin{cases} 
-c_j, l_j, m_j, a_{j+1}, in_{j+1} \in R_+ \times [0, 1] \times R_+ \times R_+ \times \{0, 1\} & \text{if } j \leq J_1, \\
-c_j, m_j, a_{j+1} \in R_+ \times R_+ \times R_+ \times \{0, 1\} & \text{if } j > J_1,
\end{cases}
\]

and the insurance system component that enters the household problem is

\[
i(in_{j+1}) = \begin{cases} 
1\{i = 1\} prem^PI (j, h) + tax^Med_j - (profits^M + profits^In) & \text{if } j \leq J_1, \\
 prem^Med_j - (profits^M + profits^In) & \text{if } j > J_1,
\end{cases}
\]

with

\[
prem^PI (j, h) = \begin{cases} 
 prem^HIH (j, h) & \text{if IHI case,} \\
 prem^GHI & \text{if GHI case},
\end{cases}
\]

where \(1\{in_{j+1} = 1\}\) is an indicator variable that is equal to one if the individual chooses to buy private health insurance and zero otherwise. Per capita provider profits are denoted \(profits^M\) and per capita insurance company profits are denoted \(profits^In\). Taxable income \(\bar{y}_j\) now includes provider profits, GHI premium deductions for the case with GHI and payroll tax deductions from Medicaid payments.
\[
\bar{y}_j = y_j + \text{profits}^M + \text{profits}^I - a_j - t_{\text{eq}} - 1_{[n=2]} \text{prem}^\text{GHI} - 0.5 t_{\text{tax}^SS} + t_{\text{tax}^\text{Med}},
\]

\[
tax^SS = \tau^SS \times \min \left( \bar{y}_{ss}, e_j \Phi, h_j, E_j^l \times l_j \times w - 1_{[n=2]} \text{prem}^\text{GHI} \right).
\]

\[
tax^\text{Med} = \tau^\text{Med} \times \left( e_j \Phi, h_j, E_j^l \times l_j \times w - 1_{[n=2]} \text{prem}^\text{GHI} \right).
\]

**Insurance Sector.** The respective IHI and GHI sectors are set up identically to the US case in expressions (10) or (11), respectively.
4 Benchmark Calibration

In order to calibrate the structural parameters of our benchmark model we use the US-version of the model from Section 3.8.1 and match it to US data before the implementation of the Affordable Care Act in 2010.\footnote{Jung and Tran (2016) analyze the long-run effects of the ACA. Here we investigate alternative social health insurance systems.} We use a standard numeric algorithm to solve the model and determine parameter values. Specifically, we use a variant of the Gauss-Seidl algorithm and first guess a price vector, then backward solve the household problem using these prices, then aggregate the economy and finally solve for a new price vector using firm first order conditions. We then update the price vector and repeat all the steps until the price vector converges.

For our calibration we use data from the Medical Expenditure Panel Survey from 1999-2009 augmented with data from CMS, the Panel Study of Income Dynamics (PSID) from 1984-2005 as well as data from the National Income Accounts (NIPA). More details about the data is provided in an Online Appendix. In our calibration, we distinguish between two sets of parameters that we refer to as external and internal parameters. External parameters are estimated independently from our model and either based on our own estimates using data from MEPS and CMS, or estimates provided by other studies. We summarize these external parameters in the Appendix, Table 8. Internal parameters are calibrated so that model-generated data moments match a given set of targets from US data. These parameters are presented in the Appendix, Table 9. We next discuss how we choose the parameters, followed by a discussion of how well the US-model fits the data.

4.1 Demographics

One period is defined as 5 years. We model households from age 20 to age 95 which results in \( J = 15 \) periods. The annual conditional survival probabilities are taken from US life-tables in 2010 and adjusted for period length. The population growth rate for the US was 1.2 percent on average from 1950 to 1997 according to the Council of Economic Advisors (1998). In the model the total population over the age of 65 is 17.7 percent which is very close to the 17.4 percent as fraction of the 20+ year olds in the census.

4.2 Preferences and Endowments

Preferences. We choose a Cobb-Douglas type utility function of the form

\[
 u(c, l, h) = \frac{(c^\eta \times (1 - l - \frac{1}{\kappa} | l_0 | j)^{-\eta \frac{1}{\kappa}}}{1 - \frac{1}{\kappa} \sigma} \times 1 \kappa^{1 - \sigma},
\]

where \( c \) is consumption, \( l \) is labor supply, \( l_j \) is the age dependent fixed cost of working as in French (2005), \( \eta \) is the intensity parameter of consumption relative to leisure, \( \kappa \) is the intensity parameter of health services relative to consumption and leisure and \( \sigma \) is the inverse of the intertemporal rate of substitution (or relative risk aversion parameter). Cobb-Douglas
preferences are widely used in the macroeconomic literature (e.g., see Heathcote, Storesletten and Violante (2008)), as they are consistent with a balanced growth path, irrespective of the choice for $\sigma$.\textsuperscript{10}

Fixed cost of working is set in order to match labor hours per age group. Parameter $\sigma$ is set to 3.0 and the time preference parameter $\beta$ is set to 1.001 to match the capital output ratio and the interest rate.\textsuperscript{11} We set the intensity parameter $\eta = 0.43$ to match the aggregate labor supply and $\kappa = 0.75$ to match the ratio between final goods consumption and medical consumption. In conjunction with the health productivity parameters $\phi_j$ and $\xi$ from expression (16) these preference weights also ensure that the model matches total health spending and the health insurance take-up rate for each age group.

**Labor Productivity.** The effective quality of labor supplied by workers is

$$
e_j(\vartheta, h_j, E) = \left(\frac{\text{wage}_{j,\vartheta}}{h_{j,\vartheta}}\right)^{\chi} \times \exp \left[\frac{h_j - h_{j,\vartheta}}{h_{j,\vartheta}} \right]^{1-\chi} \times E \text{ for } j = \{1, \ldots, J\},$$

and has three components. First, we model the work efficiencies of four skill types, denoted $\vartheta$. Skill types are assumed to be predetermined and permanent and are formed by wage quartile. The work efficiencies of the skill types are hump-shaped over the lifecycle and are estimated using average hourly wage estimates $\text{wage}_{j,\vartheta}$ by wage quartile (i.e., the permanent skill group $\vartheta$) and age $j$ from MEPS data.

Second, the quality of labor can be influenced by health. Since $\text{wage}_{j,\vartheta}$ already reflects the productivity for average health capital of an $(j, \vartheta)$ type, the idiosyncratic health effect is measured as percent deviation from the average health capital $h_{j,\vartheta}$ of each skill and age group. In order to avoid negative numbers we use the exponent function. Parameter $\chi = 0.85$ measures the relative weight of the average productivity vs. the individual health effect.

The third component is an idiosyncratic labor productivity shock $E$ and is based on Storesletten, Telmer and Yaron (2004). We discretize this process into a five state Markov process following Tauchen (1986) with labor shocks $E_t \in \{4.41; 3.51; 2.88; 2.37; 1.89\}$.

### 4.3 Health Capital

**Health Production Technology.** The law of motion of health capital consists of three components:

$$h_j = h_m j, h_{j-1}, \vartheta_j, E_t^h = \frac{\text{Investment}}{\phi_j m_j^{\vartheta_j}} + \frac{\text{Trend}}{1 - \delta_j} + \frac{\text{Disturbance}}{j}.$$  

\textsuperscript{10}Palumbo (1999), French (2005), De Nardi, French and Jones (2010) and French and Jones (2011) use similar setups where health status serves as preference shifter.

\textsuperscript{11}It is understood that in a general equilibrium model every parameter affects the equilibrium value of all endogenous variables to some extent. Here we associate parameters with those equilibrium variables that are the most directly affected (quantitatively).
The first component is a health production function that uses health services \( m \) as inputs to produce new quantities of health capital. The second component measures the natural health deterioration over time with age-dependent depreciation rate \( \delta^h \). The third component represents a random and age-dependent health shock. Grossman (1972b) and Stratmann (1999) estimate positive effects of medical services on measures of health outcomes. However, we are not aware of any precise estimates for parameters \( \phi_j \) and \( \zeta \) in expression (16). A recent empirical contribution by Galama et al. (2012) finds weak evidence for decreasing returns to scale which would imply that \( \zeta < 0 \). In our paper we let \( \phi_j \) be age-dependent and let \( \zeta \) and \( \phi_j \) endogenously adjust to match aggregate health expenditures and the medical expenditure profile over age.

**Health Capital Space.** MEPS contains two possible sources of information on health status that could serve as a measure of health capital: self-reported health status and the health index Short-Form 12 Version 2 (SF – 12v2).\(^{12}\) Since the \( SF – 12v2 \) index is more objective and comparable over the lifecycle, we use this index as a measure for health capital in our model. In order to construct a health capital space we assume a maximum health capital level \( h_{max} = 3.5 \). All other health shock and health production parameters are then re-scaled using this value. We allow for 15 states on the health grid. The lower bound of the health grid \( h_{min} \) is treated as an internal parameter that is chosen in conjunction with the health production parameters \( \phi_j \) and \( \zeta \).

**Health Depreciation Rate.** We next approximate the natural rate of health depreciation \( \delta^h \) per age group. We calculate the average health capital \( \hat{h}_j \) per age group of individuals with group insurance and zero health spending in any given year. We then postulate that such individuals did not incur a negative health shock in this period as they could easily afford to buy medical services \( m \) to replenish their health due to their insurance status. This means that for those individuals the smoothing and shock component in expression (16) disappear as \( \xi^h = 0 \) and \( m_j = 0 \). The average law of motion of health capital then reduces to \( \hat{h}_j = 1 - \delta^h \hat{h}_{j-1} \), from which we can recover the age-dependent natural rate of health depreciation \( \hat{\rho}^h \). The depreciation rates are increasing in age and fall between 0.6 and 2.13 percent per period. Note that these values are rather small because they do not contain the negative health shocks that are modeled separately.

**Health Shock.** For each age cohort \( j \) we separate individuals into four risk groups: group 1, whose health capital levels fall into the 25\(^{th} \) percentile of age \( j \) individuals, group 2 whose health capital levels fall between the 25\(^{th} \) and the 50\(^{th} \) percentile, group 3 falls between the 50\(^{th} \) and the 75\(^{th} \) percentile, and group 4 whose health capital is in the top quartile. We assume that group 4 experiences no health shock, so that this group’s average health shock defines the maximum health capital \( h_{max} \) (where subscript \( d \) indicates that this variable is calculated from MEPS data). Group 3 experiences a “small” health shock, group 2 experiences a “moderate”

\(^{12}\)The \( SF – 12v2 \) includes twelve health measures of physical and mental health. There are two versions of this index available, one for physical health and the other for mental health. Both measures use the same health measures to construct the index but the physical health index puts more weight on variables measuring physical health components (compare Ware, Kosinski and Keller (1996) for further details about this health index). For this study we use the physical health index.
health shock, and group 1 suffers from a “large” health shock. The averages of health capital per age group are denoted \( \bar{h}_{j,d}^{\text{max}} > \bar{h}_{j,d}^2 > \bar{h}_{j,d}^3 > \bar{h}_{j,d}^1 \). We next express the shock magnitudes as percentage deviations from the maximum health state in the data, so that the shock vector is:

\[
E_{\%} = \begin{pmatrix}
0, & -\bar{h}_{j,d}^3, & -\bar{h}_{j,d}^2, & -\bar{h}_{j,d}^1
\end{pmatrix},
\]

This vector is then multiplied with the maximum health capital level in the model \( \bar{h}_{t,n}^{\text{max}} \) to calculate the shock levels in the model. The transition probability matrix of health shocks \( \Pi_t \) is calculated by counting how many individuals move across risk groups between two consecutive years in MEPS data. We smooth the transition probabilities and adjust for period length.

### 4.4 Technologies and Firms

We impose a standard Cobb-Douglas production technology that uses physical capital and labor as inputs to produce a final consumption good according to \( F(K, L) = AK^\alpha L^{1-\alpha} \). The medical sector uses \( F_m(K_m, L_m) = A_mK_m^{\alpha_m} L_m^{1-\alpha_m} \). We set the capital share of production \( \alpha \) to 0.33 and the annual capital depreciation rate at \( \delta = 0.1 \), which are both standard values in the calibration literature (e.g., Kydland and Prescott (1982)). The capital share in production in the health care sector is set lower at \( \alpha_m = 0.26 \) (based on Donahoe (2000) and our own calculations).

### 4.5 Government

**Pensions.** In the model, social security transfers are defined as a function of average labor income per skill type \( wL(\theta) \) where \( L(\theta) \) denotes the average effective human capital of type \( \theta \). Let \( R_{ss}(\theta) = \Psi \times wL(\theta) \) be type specific pension payments where \( \Psi \) is a scaling factor that determines the size of the pension payment. Total pension payments amount to 4.1 percent of GDP. This is close to the number reported in the budget tables of the Office of Management and Budget (OMB) for 2008 which is close to 5 percent.

**Taxes.** We use the formula from Gouveia and Strauss (1994) to calculate the progressive income tax as

\[
\tau(\bar{y}) = a_0 \bar{y} - \bar{y}^{-a_1} + a_2 \bar{y}^{-1/a_1},
\]

where \( \bar{y} \) is taxable income. The parameter estimates for this tax polynomial are \( a_0 = 0.258, a_1 = 0.768 \) and \( a_2 = 0.031 \). The social security system is self-financed via a payroll tax of \( \tau_{ss} = 9.4 \) percent which is similar to the 10.6 percent used in Jeske and Kitao (2009). The payroll tax is collected on labor income up to a maximum of $97,500. The consumption tax rate is set to 5.0 percent (Mendoza, Razin and Tesar (1994) report 5.67 percent). The model results in total tax revenue of 21.8% of GDP and residual (unproductive) government consumption of 12 percent.

### 4.6 US Health Insurance
Medicare. We use data from CMS (Keehan et al. (2011)) and calculate that the share of total Medicaid spending that is spent on individuals older than 65 is about 36 percent. Adding this
amount to the total size of Medicare results in a combined total of 4.16 percent of GDP of public health insurance reimbursements for the old. Since MEPS only accounts for about 65-70 percent of health care spending in the national accounts (see Sing et al. (2006) and Bernard et al. (2012)) we target a size of 3.0 percent of GDP. Given a coinsurance rate of $γ^R = 0.20$, the size of the combined Medicare/Medicaid program in the model is 3.1 percent of GDP. We fix the premium for Medicare at 2.11 percent of per-capita GDP as in Jeske and Kitao (2009). The Medicare tax $τ^M ore$ is set to 2.9 percent.\footnote{Medicare payroll taxes are 2.945 percent on all earnings split in employer and employee contributions (see Social Security Update 2007 (2007)).}

**Medicaid.** According to Kaiser (2013), 16 states have Medicaid eligibility thresholds below 50 percent of the FPL, 17 states have eligibility levels between 50 and 99 percent, and 18 states have eligibility levels that exceed 100 percent of the FPL. In addition, state regulations vary greatly with respect to the asset test of Medicaid. According to MEPS data, 9.2 percent of working age individuals have some form of public health insurance. In the model we therefore calibrate the Medicaid eligibility level to 70 percent of the FPL ($FPL_{Medicaid} = 0.7 \times \text{FPL}$) and calibrate the asset test level, $\tilde{a}_{Medicaid}$, so that 9.2 percent of the working age population become eligible for Medicaid. For the reasons explained above, using the FPL directly would grossly overstate the Medicaid population. The size of Medicaid for workers is about 1.46 percent of GDP according to national accounts data but Medicaid spending in MEPS only accounts for about 0.95 to 1.02 percent of GDP (see Sing et al. (2006), Keehan et al. (2011) and Bernard et al. (2012)). The Medicaid coinsurance rate is based on MEPS estimates and depends on age so that $γ_{Medicaid}^j \in [0.11, 0.21]$. The resulting size of Medicaid for workers is 0.5 percent of GDP in the model.

**Group Insurance Offer.** We estimate a Markov process that governs the group insurance offer probability from MEPS which contains information about whether agents have received a group health insurance offer from their employer i.e. offer shock $E^GHI \in \{0, 1\}$ where 0 indicates no offer and 1 indicates a group insurance offer. Since the probability of a GHI offer is highly correlated with income, we construct the group offer transition matrix $\Pi^GHI_{j+1, j}$ by skill type $j$. That is, for each skill type we count the fraction of individuals with a GHI offer in year $j$ that is still offered group insurance in $j+1$. We smooth the transition probabilities and adjust for the five-year period length.

**Coinsurance Rates and Insurance Premiums.** Age and health dependent markup profits $ω_{HIj}$ in expression (10) are calibrated to match the IHI take-up rate over the lifecycle. The GHI markup profit $ω_{GHI}$ in expression (11) is calibrated to match the insurance take-up rate of GHI.\footnote{In the GHI we allow for lower premiums for the two youngest age cohorts in order to match the relatively high take-up rates despite the very low probability of adverse health shocks. Without this “minor” discrimination, GHI premiums would be too high and not enough young low risk types would buy GHI to match the take-up rate in the data.} We define the coinsurance rate as the fraction of out-of-pocket health expenditures over total health expenditures, so that our coinsurance rates include deductibles and copayments. We again use MEPS data to estimate the age dependent coinsurance rates of both types of insurances to be $γ_{HIj} \in [0.22, 0.52]$ and $γ_{GHI} \in [0.33, 0.5]$, respectively. The insurance premiums
are endogenously adjusted to solve the insurance companies’ problems.

**Price of Medical Services.** The base price of medical services \( p_m \) is endogenous. Shatto and Clemens (2011) report that the reimbursement rates of Medicare and Medicaid are close to 70 percent of the price that private health insurances pay for comparable health care services. Furthermore, various studies have found that uninsured individuals pay over 50 percent higher prices for prescription drugs as well as hospital services than insured individuals (see *Playing Fair, State Action to Lower Prescription Drug Prices* (2000), Anderson (2007), Gruber and Rodriguez (2007)). According to Brown (2006) the national average is a markup of around 60 percent. Large group insurance companies are able to operate at lower average fixed costs and will also be able to negotiate lower prices for health care services (see Phelps (2003)). Based on this information and assuming that Medicaid reimbursement levels result in zero provider profits, we pick the following markup factors for \( p_m \):

\[
\frac{r}{p_m^{\text{noIns}}, p_m^{\text{IHI}}, p_m^{\text{GHI}}, p_m^{\text{Med}}, p_m^{\text{Mcare}}} = (1 + [0.70, 0.20, 0.10, 0.0, -0.10]) \times p_m.
\]

When the experiments are run, this relative pricing structure is held constant so that Medicaid and Medicare remain the programs that pay the lowest prices for medical services. Thus, providers are assumed to not being able to renegotiate reimbursement rates.\(^{15}\)

### 4.7 Model Fit

Generated data moments and target moments from US data are juxtaposed in Table 10. Our calibrated model is capable of producing lifecycle trends of average medical expenditures that match US data. Figures 3 and 4 and Tables 10 and 11 summarize the model output. Health expenditures are low early in life because of high initial health capital and low health risk, and then rise as health capital depreciates. Health expenditures rise exponentially later in life because agents are exposed to more health risk. Our model also produces a hump-shaped lifecycle profile of insurance take-up rate in the US.

**Medical Expenditures.** Panel 1 of Figure 3 compares health expenditure profiles as fraction of income with MEPS data for heads of households. Our model generates total medical expenditures of 17.7 percent of gross household income which matches data provided by CMS. In addition, our model reproduces the distribution of health expenditures as seen in panel 2 of Figure 3.

**Insurance Take-up Ratio.** Panels 3, 4 and 5 of Figure 3 plot the lifecycle profiles of insurance take-up rates for individual health insurance (IHI), group health insurance (GHI) and Medicaid of the working age population. Young agents with low income are less likely to buy private health insurance compared to middle aged agents at the peak of their lifecycle earnings ability. Young individuals face lower health risk and are less willing to buy private health insurance than older individuals who are both, more willing (i.e., they face higher expected

\(^{15}\)We are not able to formally model the bargaining process between medical care providers and the insurance companies due to computational constraints.
negative health shocks) and more able to buy health insurance. The model slightly overstates the take-up rate of Medicaid among young agents.

**Income Distribution.** Table 11 provides a summary of the income distribution compared to data from MEPS. Our benchmark model matches the lower and upper tails of the income distribution with around 14.8 percent of individuals having income below the FPL vs. 16.4 percent in MEPS.

**Assets and Labor Supply.** The model reproduces the hump-shaped patterns of lifecycle asset holdings from the PSID. However, the model does not match the peak age of asset holdings in the data. Our model slightly overstates the hours worked of the youngest cohort.

**Aggregates.** The model reproduces many important macroeconomic aggregates in the US data. Table 10 compares model moments with moments from MEPS, CMS, and National Income data.

### 5 Quantitative Analysis

In this section we examine the welfare and efficiency outcomes of three alternative health insurance systems. We use the values of the structural parameters that resulted from the calibration of the US-version of the model for three alternative health insurance settings. In order to isolate the welfare effects of the different health insurance systems we first compare each system to an economy without any health insurance. We refer to this stripped down version of the model as the No-Health Insurance version from here onward.

The No-Health Insurance model inherits the structural parameter values for preferences, technologies, labor productivity and health shocks from the US-calibration but eliminates all private and public health insurance programs. All fiscal policies such as social security, food-stamp programs, government consumption and taxes are maintained. This approach allows us to focus on the social insurance role of different health insurance systems, while keeping other forms of social insurance provided through the tax-transfer system unchanged.

Contrary to a standard Bewley model, in the health and income risk model the lack of insurance options against health shocks interacts with the limited set of market instruments against income risk (i.e., household savings with borrowing constraints) and amplifies consumption variance. This additional variation generates a welfare cost that is the sum of (i) welfare losses due to missing insurance options against income risk, (ii) losses due to incomplete health insurance against health risk and (iii) the dynamic interaction between the two. Traditional Bewley type models have focused on the first source of these welfare losses. Our experiment, on the other hand, allows for a richer set of interactions and quantifies the trade-off between welfare gains from sharing health risk via insurance and the welfare losses due to distorted incentives when instituting different health insurance schemes under asymmetric information. The latter triggers ex-post moral hazard and adverse selection effects.
5.1 System 1: Mixed Public/Private Insurance System

We first compare the US system introduced in Section 3.8.1 to the No-Health-Insurance system in Table 1. We normalize the values of the No-Health Insurance case to 0 or 100 to facilitate model comparison. The value differences between the two columns are interpreted as the long-run impact of introducing the insurance components of the US health insurance system into a perfectly competitive economy with health risk, income risk and borrowing constraints.

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Insured (%):</td>
<td>0</td>
<td>77.46</td>
</tr>
<tr>
<td>· IHI (%)</td>
<td>0</td>
<td>6.37</td>
</tr>
<tr>
<td>· GHI (%)</td>
<td>0</td>
<td>61.43</td>
</tr>
<tr>
<td>· Medicaid (%)</td>
<td>0</td>
<td>9.65</td>
</tr>
<tr>
<td></td>
<td>0</td>
<td>17.68</td>
</tr>
<tr>
<td>Med. consumption ((M))</td>
<td>100</td>
<td>107.71</td>
</tr>
<tr>
<td>Med. spending ((p_n M))</td>
<td>100</td>
<td>88.35</td>
</tr>
<tr>
<td>Capital ((K_0))</td>
<td>100</td>
<td>87.47</td>
</tr>
<tr>
<td>Output ((Y_0))</td>
<td>100</td>
<td>92.69</td>
</tr>
<tr>
<td>Welfare (CEV):</td>
<td></td>
<td></td>
</tr>
<tr>
<td>· Income Group 1 (low)</td>
<td>0</td>
<td>+5.21</td>
</tr>
<tr>
<td>· Income Group 2</td>
<td>0</td>
<td>+6.54</td>
</tr>
<tr>
<td>· Income Group 3</td>
<td>0</td>
<td>+6.79</td>
</tr>
<tr>
<td></td>
<td>0</td>
<td>+2.63</td>
</tr>
<tr>
<td></td>
<td>0</td>
<td>+1.51</td>
</tr>
</tbody>
</table>

Table 1: Mixed Public/Private Health Insurance System.

This table presents steady state results comparing the benchmark equilibrium which is calibrated to the US economy and includes a mix of private and public health insurance (column [1] US-System) to the equilibrium outcome of an otherwise identical economy without any health insurance in place (column [0] No-Health-Insurance). Data in rows marked with the % symbol are either fractions in percent or tax rates in percent. The other rows are indexed to normalized values of the No-Health-Insurance case. Each column presents steady-state results. CEV values are reported as percentage changes in terms of lifetime consumption of a newborn individual.

**Aggregates.** In the No-Health-Insurance economy insurance take-up rates are zero and individuals rely on their own investments to self-insure against health and income risk by either accumulating a risk-free asset, investing in health capital or working longer hours to generate higher per period incomes. Conversely, in the US model individuals have access to a mixed public and private health insurance system. Health insurance introduces significant distortions to individuals’ incentives to save and consume. As a result physical capital accumulation in the US system is about 12 percent below the level of the No-Health-Insurance steady state. Individuals move from self-insurance via savings into buying insurance contracts or signing up for Medicaid if they fulfill the eligibility criteria. As a result, the production of non-medical goods \(Y_c\) is 7 percent lower in the US system.

On the other hand, the medical sector production in the US system is 7.7 percent larger due to increases in demand triggered by the wide availability of insurance. This is a typical ex-post moral hazard effect. Insurance decreases the effective price of health care via two channels: (i)
health insurance picks up a share of the medical bill so that households only pay a fraction of the price and (ii) health insurance reduces the sticker price charged for medical services by providers because insurance companies have market power and can negotiate lower prices on behalf of their clients.\footnote{As discussed in Section 4.6 we do not model this bargaining process explicitly. We exogenously impose markups over a base price for medical services so that the price difference between an uninsured and insured individual matches price differences observed in the data.} Overall medical spending under the US system is lower despite the increase in medical consumption. This is mainly driven by the decrease in the medical goods prices.

**Welfare.** To quantify the welfare gains from having access to health insurance we construct a welfare measure expressed in terms of permanent consumption compensation. More specifically, we compute the consumption equivalent variation (CEV) which is the percentage increase in lifetime consumption required to make a newborn individual indifferent between the No-Health-Insurance system and the US system. A negative CEV denotes a welfare loss and a positive CEV denotes a welfare gain of the US system over the No-Health-Insurance case.

In a conventional Bewley model, idiosyncratic income shocks and missing consumption insurance impose a welfare cost caused by consumption uncertainty. Our model is an extended Bewley model with health shocks that introduce an additional source of disturbance to individual consumption and health capital holdings. Risk-averse individuals benefit, at least in expectation, from health insurance contracts against health risk as they facilitate consumption smoothing.

Under the US system retirees and low income workers have access to public health insurance (Medicare and Medicaid) while working individuals have the option to purchase private health insurance (IHI and GHI) as illustrated in Table 1. We therefore observe welfare gains across all four income groups. The low income groups benefit relatively more from health insurance. The lowest income group experiences welfare gains of about 6.5 percent of CEV. This outcome is mainly due to the redistribution effect of Medicare and, more importantly, Medicaid which targets low income groups.

Overall, the US system generates a significant welfare gain of about 5.2 percent. Arguably, the significant decrease in aggregate income due to introducing insurance also triggers negative welfare effects in our model. However, the positive welfare effects from redistributing income and from reducing the exposure to health risk outweigh the negative welfare effects triggered by incentive distortions and moral hazard. Other things equal, all income groups prefer to live in an economy with a US-style health insurance system over an economy without any health insurance.

### 5.2 System 2: Universal Public Health Insurance (UPHI)

In this section we analyze the effects of the UPHI system from Section 3.8.2. We set the coinsurance rate $\gamma_{\text{UPHI}} = 0.2$ which is identical to the calibrated value of Medicare in the US version of the model. Results for the UPHI system financed by a consumption tax are reported
in Table 2, column [2A] and results for UPHI financed by a payroll tax on high income earners are reported in column [2B].

<table>
<thead>
<tr>
<th></th>
<th>No-Health Ins.</th>
<th>[2] UPHI ($y^{Med} = 0.2$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Insured (%)</td>
<td>0</td>
<td>100.00</td>
</tr>
<tr>
<td>· Public health insurance</td>
<td>0</td>
<td>100.00</td>
</tr>
<tr>
<td>Cons. tax - $r_C$ (%)</td>
<td>4.31</td>
<td>19.59</td>
</tr>
<tr>
<td>Payroll tax - $r_Y$ (%)</td>
<td>0</td>
<td>0.00</td>
</tr>
<tr>
<td>Med. consumption ($M$)</td>
<td>100</td>
<td>117.09</td>
</tr>
<tr>
<td>Med. spending ($p_M M$)</td>
<td>100</td>
<td>87.04</td>
</tr>
<tr>
<td>Capital ($K_e$)</td>
<td>100</td>
<td>87.96</td>
</tr>
<tr>
<td>Output ($Y_e$)</td>
<td>100</td>
<td>91.78</td>
</tr>
<tr>
<td>Welfare (CEV)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>· Income Group 1 (low)</td>
<td>0</td>
<td>+4.06</td>
</tr>
<tr>
<td>· Income Group 2</td>
<td>0</td>
<td>+18.69</td>
</tr>
<tr>
<td>· Income Group 3</td>
<td>0</td>
<td>+6.19</td>
</tr>
<tr>
<td></td>
<td>0</td>
<td>−8.1</td>
</tr>
<tr>
<td></td>
<td>0</td>
<td>−13.13</td>
</tr>
</tbody>
</table>

Table 2: **Universal Public Health Insurance (UPHI).**

This table presents steady state results comparing the No-Health-Insurance regime to the equilibrium outcome of UPHI. The UPHI program is either financed by a consumption tax in column [2A] or payroll tax a payroll tax on wage income greater than $200,000 in column [2B]. Data in rows marked with the % symbol are either fractions in percent or tax rates in percent. The other rows are indexed to normalized values of the No-Health-Insurance case. Each column presents steady-state results. CEV values are reported as percentage changes in terms of lifetime consumption of a newborn individual.

**Aggregates.** Individuals who live under the UPHI system rely less on self-insurance via savings to fund their health expenditures. This subsequently leads to significant decreases in capital accumulation and output. Aggregate capital stock decreases by 12 percent and subsequently output decreases by 8.2 percent compared to the No-Health-Insurance case. The decline in capital accumulation is due to disincentives to save as well as negative income effects triggered by higher taxes that are needed to finance UPHI. Notice that the introduction of the UPHI system completely eliminates the adverse selection problem as participation through the tax system is compulsory. In order to finance the UPHI the government has to increase the consumption tax $\tau^C$ to 19.6 percent (from a benchmark of 4.31 percent). The increase in the consumption tax rate represents a direct measure of the cost of full health insurance coverage. If the UPHI is financed by a payroll tax on wage income greater than $200,000 then a 13.5 percent tax is needed.

**Welfare.** As is well documented in the literature, all social insurance programs that are financed by tax revenues trade-off gains from insurance with losses created by incentive distortions. The UPHI system is no exception. On one hand, the UPHI system pools the health risk of all individuals which is welfare improving (insurance effect). On the other hand, the

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17 This tax on the rich is similar to financing provisions in the Affordable Care Act. For more information on how the model reacts to the ACA see our work in Jung and Tran (2016).
The UPHI system creates incentive problems as it increases tax distortions, discourages individuals to save for self-insurance and encourages increased health spending (ex-post moral hazard) which potentially leads to efficiency and welfare losses (incentive effect).

The welfare effects vary significantly across income groups. First, low income groups experience welfare gains while higher income groups experience welfare losses compared to the No-Health-Insurance economy. The welfare gain is 18.7 percent for the lowest income group as opposed to a welfare loss of 13 percent for highest income group. These opposing welfare effects are driven by redistribution. The UPHI system redistributes income towards “unlucky” individuals that experience large health shocks. Overall, the UPHI system creates a welfare gain of about 4.06 percent in terms of CEV. This finding indicates that the welfare gains associated with the insurance effect dominate the welfare losses associated with the adverse incentive effects.

The insurance and incentive effects are also influenced by the specific tax policy that the government implements to finance the UPHI system. We next consider a payroll tax on high income earners who earn more than $200,000 annually in Table 2, column [28]. This payroll tax is more progressive as it redistributes funds from high income individuals to low income and less healthy individuals. The positive welfare effects experienced by low income groups are now much larger while high income groups suffer from larger welfare losses. Surprisingly, the aggregate welfare effect is similar across the two financing regimes.

**Optimal Coinsurance Rate.** In our model, the coinsurance rate is a policy tool that controls the sharing of health care costs between households and the government. Smaller coinsurance rates make insurance more generous and shift the financial burden of medical care to the government. Larger coinsurance rates make insurance less generous so that households have to finance more of their health investments. In order to quantify the trade-off between insurance and incentive effects with a varying degree of generosity of the UPHI system we solve the UPHI model for a range of different coinsurance rates \( \gamma_{\text{UPHI}} = [0.1, 0.2, 0.3, 0.4, 0.5] \) and report the results in Table 3.

The improved risk sharing and redistributitional measures embedded in the UPHI system result in welfare gains for low income individuals in poor health and welfare losses for high income individuals in good health. The overall welfare effect depends on the strength of the negative effects triggered by ex-post moral hazard and fiscal distortions. In our framework, the size of these negative forces depends on the level of the coinsurance rate. When the coinsurance rate is small, individuals share a smaller share of total health expenditure. This implies a larger ex-post moral hazard effect due to lower medical prices and larger tax distortions as the government has to impose higher taxes to finance the larger share of total health expenditure.

A coinsurance rate of \( \gamma_{\text{UPHI}} = 0.1 \) results in welfare losses caused by a large ex-post moral hazard effect (i.e., it increases medical consumption by 49%) and fiscal distortions from a large consumption tax rate of \( \tau_C = 31 \) percent. Potential welfare gains from improved risk sharing and income redistribution are dominated by these losses.

However, if the coinsurance rate gets too large, then the welfare gains start to decrease.
The approach in Conesa, Kitao and Krueger (2009) and characterize an amplify Imrohoroglu and Joines (1995)). That literature shows that the general equilibrium channels of social security in stochastic dynamic general equilibrium frameworks (e.g., Imrohoroglu, somewhat)

rates and

uses

in

while

Notice

rate. The government’s objective is defined by

utility optimal coinsurance rate.

This

percentage

steady
tax.

Table 3: UPHI with Different Coinsurance Rates.

This table presents steady state results comparing the No-Health-Insurance regime to the equilibrium outcomes with UPHI financed by a consumption tax. We allow for different levels of generosity of UPHI as presented by variations in the coinsurance rates. The UPHI program is financed by a consumption tax. Data in rows marked with the % symbol are either fractions in percent or tax rates in percent. The other rows are indexed to normalized values of the No-Health-Insurance case. Each column presents steady-state results solved with a different co-insurance rate for UPHI. CEV values are reported as percentage changes in terms of lifetime consumption of a newborn individual.

This hump-shaped pattern highlights how the health insurance system trades off the insurance and incentive effects. We find a similar pattern for the case where the government uses a payroll tax to finance the UPHI system. However, in this case the overall welfare gains are smaller.

We next follow the approach in Conesa, Kitao and Krueger (2009) and characterize an optimal coinsurance rate. We assume that the government maximizes the ex-ante lifetime utility of an individual born into the stationary equilibrium implied by the chosen coinsurance rate. The government’s objective is defined as

\[ \gamma_{UPHI}^{\text{Umax}} = \arg\max_{\gamma_{UPHI} \in [0,1]} \int V(x_{j+1}) \gamma_{UPHI} d\Lambda(x_{j+1}). \]

Notice that the government maximizes the social welfare function over the coinsurance rate only while keeping all other policy variables unchanged. We assume that the government uses either a consumption tax or a payroll tax to finance the UPHI system. We find that a coinsurance rate of 0.385 efficiently trades off the positive insurance/redistribution effects with the negative incentive effects and results in the largest welfare of a newborn individual. When the government uses a payroll tax the optimal coinsurance rate is slightly larger at 0.39.

This estimate is in the range of studies by Blomqvist (1997) who find optimal coinsurance rates in the mid 20 percent range and studies by Feldstein and Friedman (1977) and Manning and Marquis (1996) who find higher values up to 60 percent. Our positive welfare outcome is somewhat different from the classic result in the literature analyzing the welfare implications of social security in stochastic dynamic general equilibrium frameworks (e.g., Imrohoroglu, Imrohoroglu and Joines (1995)). That literature shows that the general equilibrium channels amplify the fiscal distortions caused by social security so that the introduction of a social security

<table>
<thead>
<tr>
<th>[2C] UPHI with ( \tau_{c} )</th>
<th>( \gamma_{UPHI}^{CRM} = 0.1 )</th>
<th>0.2</th>
<th>0.3</th>
<th>0.4</th>
<th>0.5</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cons. tax - ( \tau_{c} ) (%)</td>
<td>31.0</td>
<td>19.6</td>
<td>16.6</td>
<td>14.1</td>
<td>12.1</td>
</tr>
<tr>
<td>Med. consumption (( M_{i} ))</td>
<td>148.8</td>
<td>117.1</td>
<td>108.3</td>
<td>104.3</td>
<td>102.5</td>
</tr>
<tr>
<td>Med. spending (( p_{w}M_{i} ))</td>
<td>114.2</td>
<td>87.0</td>
<td>83.2</td>
<td>80.3</td>
<td>79.0</td>
</tr>
<tr>
<td>Output (( Y_{t} ))</td>
<td>88.3</td>
<td>91.8</td>
<td>93.7</td>
<td>95.2</td>
<td>96.4</td>
</tr>
<tr>
<td>Welfare (CEV):</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>• Income Group 1 (low)</td>
<td>-7.0</td>
<td>+4.1</td>
<td>+7.3</td>
<td>+7.1</td>
<td>+6.4</td>
</tr>
<tr>
<td>• Income Group 2</td>
<td>+10.1</td>
<td>+18.7</td>
<td>+20.2</td>
<td>+18.0</td>
<td>+15.3</td>
</tr>
<tr>
<td>• Income Group 3</td>
<td>-5.1</td>
<td>+6.2</td>
<td>+9.4</td>
<td>+9.3</td>
<td>+8.2</td>
</tr>
<tr>
<td>• Income Group 4</td>
<td>-20.6</td>
<td>-8.1</td>
<td>-4.0</td>
<td>-2.43</td>
<td>-1.63</td>
</tr>
<tr>
<td>• Income Group 4</td>
<td>-26.5</td>
<td>-13.2</td>
<td>-6.7</td>
<td>-6.71</td>
<td>-5.24</td>
</tr>
</tbody>
</table>
system generates welfare losses. Our welfare results indicate that this is not the case for social health insurance.

5.3 System 3: Private Health Insurance Markets for Workers

The health insurance literature suggests that health risk is not easily insured via private insurance markets due to information asymmetries that give rise to moral hazard and adverse selection inefficiencies. In addition, self-insurance of health shocks via savings is problematic due to the high persistence of these shocks. We next demonstrate the effects of purely private health insurance systems for the working population as introduced in Section 3.8.3 and report results in Table 4.

<table>
<thead>
<tr>
<th></th>
<th>No-Health Ins.</th>
<th>[3] Private Health Insurance</th>
</tr>
</thead>
<tbody>
<tr>
<td>Insured (%)</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>· IHI (%)</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>· GHI (%)</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>Med. consumption</td>
<td>100</td>
<td>100</td>
</tr>
<tr>
<td>Med. spending</td>
<td>100</td>
<td>100</td>
</tr>
<tr>
<td>Capital (Kc)</td>
<td>100</td>
<td>100</td>
</tr>
<tr>
<td>Output (Yc)</td>
<td>100</td>
<td>100</td>
</tr>
<tr>
<td>Welfare (CEV)</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>· Income Group 1 (low)</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>· Income Group 2</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>· Income Group 3</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 4: Private Health Insurance System.
This table presents steady state results comparing the No-Health-Insurance regime to the equilibrium outcomes with private health insurance but no public health insurance. We distinguish a regime with individual private health insurance (IHI) from a regime with group health insurance (GHI). Data in rows marked with the % symbol are either fractions in percent or tax rates in percent. The other rows are indexed to normalized values of the No-Health-Insurance case. Each column presents steady-state results. CEV values are reported as percentage changes in terms of lifetime consumption of a newborn individual.

Unregulated IHI Markets. Unregulated private health insurance markets are not viable in an economy with a health risk structure similar to the US economy. Price discrimination by health status and age prevents risk sharing between healthy and unhealthy individuals as the insurance pools are kept small and separate. Young agents with low income and low health risk are less likely to buy private health insurance compared to middle aged agents at the peak of their lifecycle earnings ability. Older individuals, on the other hand, are part of high risk pools and therefore face high premiums. Information asymmetry is present in our setting. Individuals know their past health shocks and type and form their expectations about future health shocks and their willingness to pay for health insurance accordingly. On the other hand, insurance companies have limited information about the history of individual-specific health shocks. They
can only observe age and the current health state before the new health shocks arrive. Insurance companies are thus unable to work out the actuarially fair price, which consequently produces an adverse selection spiral in the health insurance markets. As a result private health insurance markets fully collapse and all workers are left without insurance. This complete market failure is consistent with classic results documented in the insurance literature on adverse selection spirals (e.g., Pauly (1974) and Rothschild and Stiglitz (1976)).

**Regulated GHI Markets.** We next consider an economy in which the government regulates private insurance companies according to Section 3.8.3. These market regulations induce more individuals to participate in the private health insurance market as the tax deductibility of premium payments is a direct subsidy to households who choose to buy insurance. As reported in Table 4, column [3B], the GHI take-up is 82.9 percent of the working population. However, even with these market regulations in place the insurance system fails to provide full coverage. Young and healthy individuals who face very low health risk opt out of private health insurance as do low income groups who cannot afford the premiums.

**Aggregates.** Similar to our earlier experiments, individuals with health insurance reduce their savings. In addition, medical consumption increases by 4.6 percent while medical spending drops significantly by 17 percent. Insurance companies are again able to secure lower prices from providers than uninsured individuals who lack bargaining power.

Private insurance results in positive aggregate efficiency gains. The stock of aggregate capital decreases slightly by about 1 percent, while human capital increases due to increases in labor supply. Overall, we observe a small increase in final goods production by 0.45 percent.

**Welfare.** The existence of private health insurance markets in model [3B] provides a mechanism to pool workers so that they are able to share health risk at subsidized premium rates. This improves the allocation of health risk and redistributes income toward unhealthy individuals. Although the government does not provide health insurance directly, it implicitly provides social health insurance via subsidizing insurance premiums and regulating the insurance companies’ market behavior. Even though this market-based risk sharing mechanism is incomplete (i.e., a take-up rate of 83 percent) we still find welfare gains for all income groups as reported in the lower part of Table 4, column [3B].

Market-based health insurance systems, even with government subsidies and regulation, fail to eliminate the adverse selection issue and therefore cannot provide universal health insurance coverage. Compared to the UPHI system, this leads to a lower degree of risk pooling as well as to a lower degree of redistribution of wealth. Welfare gains are smaller which is especially true for low income groups and individuals in bad health. On the other hand, the efficiency losses in terms of capital accumulation and output are less pronounced with private health insurance markets as the tax burden of this system is much smaller.

**Private Health Insurance for Workers and Retirees.** In the next experiment we allow retirees access to a new self-clearing GHI market. The previously discussed GHI market for workers is maintained with identical parameters as in the US model. We then vary the co-insurance rate for the GHI-contract for retirees according to Table 5 and let the group premium
adjust to clear the market. We do find that by appropriately choosing the coinsurance rate – which in turn determines the insurance premium and the take-up rate – about a quarter of all retirees can be insured. This falls far short of the almost universal insurance take-up rates that are achievable with public health insurance like Medicare.

<table>
<thead>
<tr>
<th>[3C] GHI for Retirees</th>
<th>( \gamma^{\text{GHI}} = 0.1 )</th>
<th>0.2</th>
<th>0.25</th>
<th>0.3</th>
<th>0.4</th>
</tr>
</thead>
<tbody>
<tr>
<td>Insured retirees(%)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>· GHI</td>
<td>18.79</td>
<td>24.65</td>
<td>26.22</td>
<td>27.50</td>
<td>0.03</td>
</tr>
<tr>
<td>Med. consumption ((M))</td>
<td>104.97</td>
<td>104.52</td>
<td>104.49</td>
<td>104.45</td>
<td>104.59</td>
</tr>
<tr>
<td>Med. spending ((p_wM))</td>
<td>83.29</td>
<td>83.01</td>
<td>82.99</td>
<td>82.96</td>
<td>83.11</td>
</tr>
<tr>
<td>Capital ((Y_c))</td>
<td>101.86</td>
<td>100.74</td>
<td>100.66</td>
<td>100.59</td>
<td>100.45</td>
</tr>
<tr>
<td>Output ((K_r))</td>
<td>99.20</td>
<td>98.97</td>
<td>98.85</td>
<td>98.73</td>
<td>98.58</td>
</tr>
<tr>
<td>Welfare (CEV)</td>
<td>+4.08</td>
<td>+4.33</td>
<td>+4.14</td>
<td>+3.92</td>
<td>+0.99</td>
</tr>
</tbody>
</table>

Table 5: **GHI for Retirees with Various Coinsurance Rates.**

This table presents steady state results comparing the No-Health-Insurance regime to the equilibrium outcomes with GHI for workers and retirees. We allow for different levels of generosity of GHI for retirees as presented by variations in the coinsurance rates. Co-insurance rates for workers are left unchanged at benchmark US levels. Note that coinsurance rates for workers are still age dependent. Data in rows marked with the % symbol are either fractions in percent or tax rates in percent. The other rows are indexed to normalized values of the No-Health-Insurance case. Each column presents steady-state results solved with a different co-insurance rate for GHI. CEV values are reported as percentage changes in terms of lifetime consumption of a newborn individual.

If coinsurance rates are not generous enough (i.e., \( \gamma^{\text{GHI}} > 40\% \)) GHI for the old erodes. Similarly, GHI contracts that are too generous (i.e., \( \gamma^{\text{GHI}} < 10\% \)) also lose market share as they become too expensive. Richer cohorts benefit the most from very generous GHI contracts whereas low income cohorts benefit less. This is in contrast to the UPHI results in Table 3 where welfare effects were more favorable for low income groups. Private health insurance lacks the redistribution element of the UPHI system and is therefore less desirable for low income households.

### 5.4 The US Insurance System vs. the UPHI System

We have demonstrated that all three social health insurance systems result in welfare gains over the No-Health Insurance system. In this section, we compare the steady state of the pre-ACA US system to the steady state under the UPHI system. We consider a range of coinsurance rates for the UPHI system \( \gamma^{\text{UPHI}} = [0.2, 0.3, 0.4, 0.5] \) in Table 6. In these experiments the US-system serves as benchmark with level variables normalized to 100.

A UPHI system with a coinsurance rate of \( \gamma^{\text{UPHI}} = 0.2 \) results in a 1 percent drop of GDP compared to the steady state outcome under the US system. The same experiments with a slightly less generous UPHI system, i.e. \( \gamma^{\text{UPHI}} \geq 0.3 \), lead to GDP growth. This implies that a moderate coinsurance rate can mitigate the adverse effects from tax distortions so that risk pooling and redistribution ultimately lead to increases in capital accumulation and output.
Table 6: A Switch from the US-System to a UPHI-System Financed by Consumption Tax.

This table presents steady state results comparing the US health insurance system to the equilibrium outcomes with universal public health insurance (UPHI) financed by a consumption tax. We allow for different levels of generosity of UPHI as presented by variations in the coinsurance rates. Data in rows marked with the % symbol are either fractions in percent or tax rates in percent. The other rows are indexed to normalized values of the US-benchmark case. Each column presents steady-state results. CEV values are reported as percentage changes in terms of lifetime consumption of a newborn individual.

More importantly, we observe large welfare gains in a UPHI system with $\gamma_{UPHI} \geq 0.3$. The UPHI system results in much larger overall welfare gains as the UPHI system pools risk more efficiently across the different groups and redistributes wealth more equitable. As can be seen in Figures (5) and (6) the variation of out-of-pocket health expenditures and health capital is lowest over the entire lifecycle under the UPHI system (red line in the figures). Figure (7) shows relative variation normalized with the mean value of health capital per age group over the lifecycle. The welfare gains are mainly driven by welfare gains of low income groups who now can access to medical services at a lower price. High income groups fare better under the US system.\textsuperscript{18}

Payroll Tax as Financing Tool. We next compare the US system to a UPHI system financed by a payroll tax on wage income greater than $200,000. We report the results in in Table 7.

Taxing labor income to finance the UPHI system is more distortive than a consumption tax as it reduces labor supply and GDP more. However, the overall pattern of the welfare effects are quite similar to the UPHI system financed by a consumption tax. We again observe different welfare outcomes across all income groups. Interestingly, the optimal coinsurance rate is higher when using a payroll tax as financing source. The intuition is that the higher coinsurance rate

\textsuperscript{18}We assume that all markups on the price of medical care are removed when switching to the UPHI system. This redistribution mechanism through changing the price of medical services could affect welfare effects. After the reform, the working population can consume medical services at a lower price; meanwhile, the retiring population has to pay a higher price. We compare the reforms with and without markups and find that the effects from this channel does not change our main result.
Table 7: A Switch from the US-System to a UPHI-System Financed by Payroll Tax. This table presents steady state results comparing the US health insurance system to the equilibrium outcomes with universal public health insurance (UPHI) financed by a payroll tax on wage income greater than $200,000. We allow for different levels of generosity of UPHI as presented by variations in the coinsurance rates. Data in rows marked with the % symbol are either fractions in percent or tax rates in percent. The other rows are indexed to normalized values of the US-benchmark case. Each column presents steady-state results. CEV values are reported as percentage changes in terms of lifetime consumption of a newborn individual.

<table>
<thead>
<tr>
<th>[1] US-System</th>
<th>[2] UPHI with $\gamma_{UPHI} = 0.2$</th>
<th>0.3</th>
<th>0.4</th>
<th>0.5</th>
</tr>
</thead>
<tbody>
<tr>
<td>Payroll tax - $\tau_V$ (%)</td>
<td>0.0</td>
<td>13.5</td>
<td>11.2</td>
<td>9.1</td>
</tr>
<tr>
<td>Med. consumption ($M$)</td>
<td>100</td>
<td>103.58</td>
<td>97.86</td>
<td>95.75</td>
</tr>
<tr>
<td>Med. spending ($p_r M$)</td>
<td>100</td>
<td>93.37</td>
<td>91.50</td>
<td>89.65</td>
</tr>
<tr>
<td>GDP</td>
<td>100</td>
<td>93.82</td>
<td>96.33</td>
<td>98.61</td>
</tr>
<tr>
<td>Welfare (CEV):</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>· Income Group 1 (low)</td>
<td>0.00</td>
<td>−2.47</td>
<td>+0.78</td>
<td>+0.93</td>
</tr>
<tr>
<td>· Income Group 2</td>
<td>0.00</td>
<td>+15.17</td>
<td>+15.97</td>
<td>+12.94</td>
</tr>
<tr>
<td>· Income Group 3</td>
<td>0.00</td>
<td>−2.57</td>
<td>+0.93</td>
<td>+1.11</td>
</tr>
<tr>
<td>· Income Group 4</td>
<td>0.00</td>
<td>−14.51</td>
<td>−9.74</td>
<td>−7.46</td>
</tr>
<tr>
<td></td>
<td>0.00</td>
<td>−17.67</td>
<td>−13.18</td>
<td>−10.15</td>
</tr>
</tbody>
</table>

reduces the fiscal burden and therefore mitigates the distortion of work incentives.\(^{19}\)

In summary, our findings indicate that the UPHI system outperforms the US health insurance system in terms of output and welfare if the coinsurance rate is moderate. However, such radical reform faces political impediments because of opposing welfare effects across different income groups.

6 Conclusion

In this paper we investigate the welfare implications of different health insurance systems in a model with incomplete market mechanisms to insure against health risk. We develop a generalized Bewley-Grossman model and calibrate the baseline model to match the lifecycle structure of earnings and health risks in US data. We then apply the model to evaluate the benefits in terms of insurance and the cost in terms of incentive distortions across insurance systems that differ in the degree of government involvement. We consider three systems: (i) a mixed public/private insurance system similar to the pre-ACA US system, (ii) a pure government-based approach with a universal public health insurance (UPHI) system and (iii) a more market-based approach with a private health insurance system for workers assisted by government subsidies and market regulation.

\(^{19}\)The factor loading costs (fixed costs) of private health insurance under the US system could be due to inefficiency in these insurance markets. Removing these loads can be another motivation for a switch from the US system to a UPHI system. However, we abstract from this channel in this analysis by assuming that the loads on the private insurance markets are transformed into insurance firms’ profits and allocated back to the households as a lump-sum transfer. This simplified assumption allows us to focus our analysis on the insurance and incentive trade-off.
Our results indicate that the government provision of social insurance leads to positive welfare outcomes in all three systems. That is, the positive insurance/redistribution effects strongly dominate the negative incentive effects caused by tax distortions and ex-post moral hazard effects. In general, the UPHI system results in the largest welfare gains if the coinsurance rate is kept at moderate levels. We solve for the optimal coinsurance rate that balances the trade-off between positive insurance and the negative incentive effects and maximizes welfare of a newborn individual. More importantly, different degrees of government involvement lead to opposing welfare effects across income groups. Low income households benefit more from the government-based approach whereas high income households benefit more from the market-based or mixed approach. This result highlights political difficulties that policymakers would face should they decide to switch from the current market based US health insurance system to a universal insurer system like the UPHI system.

The introduction of a UPHI can be justified by the inefficiency of private insurance markets which leads to high administrative costs and price markups or because of concerns about equity in health outcomes. In this paper we do not focus on these issues. In addition, there are several other extensions left for future work. The optimality of insurance contracts is currently restricted to the analysis of a single policy instrument – coinsurance rates with a linear tax adjusting to balance the public insurance program or a base premium adjusting to balance the private health insurance contract. More general policy instruments (i.e., progressive taxes, differential premiums, etc.) can be investigated to describe optimal equilibrium outcomes. The large state space of the model and computational constraints prevent us from providing a description of the transition dynamics. Solutions for transitions between different health insurance systems would be required to answer the question of reform implementability. The lack of a bequest motive and the imposed independence of survival from health states lead to lower than observed assets holdings of the retired cohorts and affect the level of self-insurance via savings.

References


# Appendix

## 7.1 Appendix A: Calibration Tables

<table>
<thead>
<tr>
<th>Parameters:</th>
<th>Explanation/Source:</th>
</tr>
</thead>
<tbody>
<tr>
<td>- Periods working</td>
<td>$J_1 = 9$</td>
</tr>
<tr>
<td>- Periods retired</td>
<td>$J_2 = 6$</td>
</tr>
<tr>
<td>- Population growth rate</td>
<td>$n = 1.2%$</td>
</tr>
<tr>
<td>- Years modeled</td>
<td>$\text{years} = 75$</td>
</tr>
<tr>
<td>- Total factor productivity</td>
<td>$A = 1$</td>
</tr>
<tr>
<td>- Growth rate</td>
<td>$g = 2%$</td>
</tr>
<tr>
<td>- Capital share in production</td>
<td>$\alpha = 0.33$</td>
</tr>
<tr>
<td>- Capital in medical services prod.</td>
<td>$\alpha_m = 0.26$</td>
</tr>
<tr>
<td>- Capital depreciation</td>
<td>$\delta = 10%$</td>
</tr>
<tr>
<td>- Health depreciation</td>
<td>$\delta_h,j = [0.6% - 2.13%]$</td>
</tr>
<tr>
<td>- Survival probabilities</td>
<td>$\pi_j$</td>
</tr>
<tr>
<td>- Health Shocks</td>
<td>Technical Appendix</td>
</tr>
<tr>
<td>- Health transition prob.</td>
<td>Technical Appendix</td>
</tr>
<tr>
<td>- Productivity shocks</td>
<td>see Section 4</td>
</tr>
<tr>
<td>- Productivity transition prob.</td>
<td></td>
</tr>
<tr>
<td>- Group ins. transition prob.</td>
<td></td>
</tr>
<tr>
<td>- Price for medical care for uninsured</td>
<td>$\nu_{\text{noIns}} = 0.7$</td>
</tr>
<tr>
<td>- $M$ price markup for IHI insured</td>
<td>$\nu_{\text{IHI}} = 0.25$</td>
</tr>
<tr>
<td>- $M$ price markup for GHI insured</td>
<td>$\nu_{\text{GHI}} = 0.1$</td>
</tr>
<tr>
<td>- $M$ price markup for Medicaid</td>
<td>$\nu_{\text{Maid}} = 0.0$</td>
</tr>
<tr>
<td>- $M$ price markup for Medicare</td>
<td>$\nu_{\text{Medicare}} = -0.1$</td>
</tr>
<tr>
<td>- Coinsurance rate: IHI in %</td>
<td>$\gamma_{\text{IHI}} \in [22, 46, 48, 49, 50, 53, 52, 50]$</td>
</tr>
<tr>
<td>- Coinsurance rate: GHI in %</td>
<td>$\gamma_{\text{GHI}} \in [33, 33, 33, 34, 36, 36, 45, 50]$</td>
</tr>
<tr>
<td>- Medicare premiums/GDP</td>
<td>2.11%</td>
</tr>
<tr>
<td>- Medicaid coinsurance rate in %</td>
<td>$\gamma_{\text{Maid}} \in [11, 14, 17, 16, 17, 18, 20, 22]$</td>
</tr>
<tr>
<td>- Public coinsurance rate retired in %</td>
<td>$\gamma_R = 20$</td>
</tr>
</tbody>
</table>

Table 8: External Parameters.  
These parameters are based on our own estimates from MEPS and CMS data as well as other studies.
### Parameters:

- Relative risk aversion
- Preference on consumption vs. leisure:
- Preference on c and l vs. health
- Discount factor
- IHI markup profits

- Health production productivity
- TFP in medical production
- Production parameter of health
- Effective labor services production
- Health productivity

- Pension replacement rate
- Residual Government spending
- Minimum health state

- Total number of internal parameters:

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Explanation/Source</th>
<th>Nr.M.</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\sigma = 3.0)</td>
<td>to match (\frac{\zeta}{Y}) and (K)</td>
<td>1</td>
</tr>
<tr>
<td>(\eta = 0.43)</td>
<td>to match labor supply and (\frac{\nu^v}{Y})</td>
<td>1</td>
</tr>
<tr>
<td>(\kappa = 0.75)</td>
<td>to match labor supply and (\frac{\nu^v}{Y})</td>
<td>1</td>
</tr>
<tr>
<td>(\beta = 1.0)</td>
<td>to match (K) and (R)</td>
<td>1</td>
</tr>
<tr>
<td>(\omega_{j,h} \in [0.6 - 1.5])</td>
<td>to match spending profile</td>
<td>8</td>
</tr>
<tr>
<td>(\varphi_j \in [0.2 - 0.45])</td>
<td>to match spending profile</td>
<td>15</td>
</tr>
<tr>
<td>(A_m = 0.4)</td>
<td>to match (\frac{\nu^v}{Y})</td>
<td>1</td>
</tr>
<tr>
<td>(\zeta = 0.26)</td>
<td>to match labor supply</td>
<td>1</td>
</tr>
<tr>
<td>(\chi = 0.85)</td>
<td>used for sensitivity analysis</td>
<td>1</td>
</tr>
<tr>
<td>(\theta = 1.0)</td>
<td></td>
<td>1</td>
</tr>
<tr>
<td>(\Psi = 40%)</td>
<td>to match (r^{soc})</td>
<td>1</td>
</tr>
<tr>
<td>(\Delta_c = 12.0%)</td>
<td>to match size of tax revenue</td>
<td>1</td>
</tr>
<tr>
<td>(h_{min} = 0.01)</td>
<td>to match health spending</td>
<td>1</td>
</tr>
</tbody>
</table>

Table 9: **Internal Parameters.**
We choose these parameters in order to match a set of target moments in the data.

### Moments

<table>
<thead>
<tr>
<th>Moments</th>
<th>Model</th>
<th>Data</th>
<th>Source</th>
<th>Nr.M.</th>
</tr>
</thead>
<tbody>
<tr>
<td>- Medical expenses HH income</td>
<td>17.6%</td>
<td>17.07%</td>
<td>CMS communication</td>
<td>1</td>
</tr>
<tr>
<td>- Workers IHI</td>
<td>5.6%</td>
<td>7.2%</td>
<td>MEPS 1999/2009</td>
<td>1</td>
</tr>
<tr>
<td>- Workers GHI</td>
<td>61.1%</td>
<td>62.2%</td>
<td>MEPS 1999/2009</td>
<td>1</td>
</tr>
<tr>
<td>- Workers Medicaid</td>
<td>9.6%</td>
<td>9.2%</td>
<td>MEPS 1999/2009</td>
<td>1</td>
</tr>
<tr>
<td>- Capital output ratio: (K/Y)</td>
<td>2.7</td>
<td>2.6 – 3</td>
<td>NIPA</td>
<td>1</td>
</tr>
<tr>
<td>- Interest rate: (R)</td>
<td>4.2%</td>
<td>4%</td>
<td>NIPA</td>
<td>1</td>
</tr>
<tr>
<td>- Size of Social Security/(Y)</td>
<td>5.9%</td>
<td>5%</td>
<td>OMB 2008</td>
<td>1</td>
</tr>
<tr>
<td>- Size of Medicare/(Y)</td>
<td>3.1%</td>
<td>2.5 – 3.1%</td>
<td>U.S. Department of Health (2007)</td>
<td>1</td>
</tr>
<tr>
<td>- Payroll tax Social Security: (r^{soc})</td>
<td>9.4%</td>
<td>10 – 12%</td>
<td>IRS</td>
<td>1</td>
</tr>
<tr>
<td>- Consumption tax: (\tau^C)</td>
<td>5.0%</td>
<td>5.7%</td>
<td>Mendoza et al. (1994)</td>
<td>1</td>
</tr>
<tr>
<td>- Payroll tax Medicare: (\tau^{Med})</td>
<td>2.9%</td>
<td>1.5 – 2.9%</td>
<td>Social Security Update (2007)</td>
<td>1</td>
</tr>
<tr>
<td>- Medical spend. profile</td>
<td>Figure 3</td>
<td>Figure 3</td>
<td>MEPS 1999/2009</td>
<td>15</td>
</tr>
<tr>
<td>- IHI insurance take-up profile</td>
<td>Figure 3</td>
<td>Figure 3</td>
<td>MEPS 1999/2009</td>
<td>8</td>
</tr>
<tr>
<td>Total number of moments</td>
<td></td>
<td></td>
<td></td>
<td>34</td>
</tr>
</tbody>
</table>

Table 10: **Matched Data Moments.**
We choose internal parameters so that model generated data match data from MEPS, CMS and NIPA.
Table 11: **Select Quantiles of the Income Distribution.**

We compare model generated income quantiles to income quantiles from MEPS. These quantiles were not targeted in the calibration.

<table>
<thead>
<tr>
<th>Quantiles</th>
<th>MEPS Data (in $1,000)</th>
<th>Model (in $1,000)</th>
</tr>
</thead>
<tbody>
<tr>
<td>10%</td>
<td>11.02</td>
<td>8.12</td>
</tr>
<tr>
<td>20%</td>
<td>18.17</td>
<td>15.86</td>
</tr>
<tr>
<td>30%</td>
<td>24.88</td>
<td>23.39</td>
</tr>
<tr>
<td>40%</td>
<td>31.14</td>
<td>31.05</td>
</tr>
<tr>
<td>50%</td>
<td>37.98</td>
<td>38.00</td>
</tr>
<tr>
<td>60%</td>
<td>45.75</td>
<td>48.05</td>
</tr>
<tr>
<td>80%</td>
<td>68.82</td>
<td>78.21</td>
</tr>
<tr>
<td>100%</td>
<td>391.18</td>
<td>323.52</td>
</tr>
</tbody>
</table>
Appendix B: Figures

Figure 1: Health Spending over the Lifecycle by Financing Source.
We present average health spending per 5-year age cohort based on MEPS 1999-2009. We break down health spending by spending source. Spending values are inflation adjusted to 2009-dollar values.
Figure 2: Health Expenditures by Sources in OECD Economies (OECD, 2004).
Figure 3: Moment Matching using MEPS Data 2000-2009.
Blue lines are model generated data moments and black dotted lines are MEPS data. Panel [1] depicts the percentage of average medical spending as percent of total household income of a 5-year age-cohort. Panel [2] shows the health expenditure distribution of heads of households from MEPS vs. model generated health spending. Panels [3-4] show the fraction of individual, group and Medicaid insurance for the working age population.
Figure 4: Model vs. Data.
Figure 5: **Standard Deviation of Out-of-Pocket Health Expenditure over the Lifecycle.**

Panel [1] shows the standard deviations of out-of-pocket health expenditures of 5-year age-cohorts over the lifecycle for different policy regimes for skill group 1 (lowest wage quartile). The regime without any insurance (denoted: 1_NoIns) exhibits the largest standard deviations throughout the lifecycle. The regime with universal public health insurance (denoted: 3_UPHI) exhibits the least amount of variation over the lifecycle. The remaining panels show the standard deviations over the lifecycle for the second, third and fourth wage quartile.
Figure 6: **Standard Deviation of Health Capital over the Lifecycle.**
Panel [1] shows the standard deviations of health capital of 5-year age-cohorts over the lifecycle for different policy regimes for skill group 1 (lowest wage quartile). The regime without any insurance (denoted: 1_NoIns) exhibits the largest standard deviations throughout the lifecycle. The regime with universal public health insurance (denoted: 3_UPHI) exhibits the least amount of variation over the lifecycle. The remaining panels show the standard deviations over the lifecycle for the second, third and fourth wage quartile.
Figure 7: Coefficient of Variation of Health Capital over the Lifecycle.
Panel [1] shows the coefficients of variation of health capital of 5-year age-cohorts over the lifecycle for different policy regimes for skill group 1 (lowest wage quartile). The regime without any insurance (denoted: 1_NoIns) exhibits the largest variations throughout the lifecycle. The regime with universal public health insurance (denoted: 3_UPHI) exhibits the least amount of variation over the lifecycle. The remaining panels show the coefficients of variation over the lifecycle for the second, third and fourth wage quartile.