Please provide feedback

Please support the ScholarWorks@UMBC repository by emailing scholarworks-group@umbc.edu and telling us what having access to this work means to you and why it’s important to you. Thank you.
Developing the Physical Understanding of Intermediate Polars: An X-Ray Study of TV Col and V2731 Oph

R. Lopes de Oliveira1,2,3,4 and K. Mukai2,5

1 X-ray Astrophysics Laboratory, NASA Goddard Space Flight Center, Greenbelt, MD 20771, USA; rlopes@ufs.br
2 Center for Space Science and Technology, University of Maryland, Baltimore County, 1000 Hilltop Circle, Baltimore, MD 21250, USA
3 Departamento de Física, Universidade Federal de Sergipe, Av. Marechal Rondon, S/N, 49000-000 São Cristóvão, SE, Brazil
4 Observatório Nacional, Rua Gal. José Cristino 77, 20921-400, Rio de Janeiro, RJ, Brazil
5 CRESST II and X-ray Astrophysics Laboratory, NASA Goddard Space Flight Center, Greenbelt, MD 20771, USA

Received 2019 March 14; revised 2019 June 17; accepted 2019 June 18; published 2019 August 2

Abstract

The X-rays in intermediate polars (IPs) originate in a compact region near the surface of a magnetic white dwarf (WD) and interact with the complex environment surrounding the emission region. Here we report a case study of two IPs, TV Col and V2731 Oph, with selected archival X-ray observations (NuSTAR, Swift, Suzaku, and XMM-Newton). For TV Col, we were successful in simultaneously accounting for the primary X-rays, the secondary X-rays due to Compton scattering and fluorescence, and the effects of local absorbers. In this case, we were able to demonstrate that the shock height is small, based on the high reflection amplitude; hence, the maximum temperature of the post-shock region can be used to derive the WD mass of $0.735 \pm 0.015 M_\odot$. Despite the high specific accretion rate required to explain the small shock height, we do not detect any spin modulation in our NuSTAR data, consistent with the modest amount of complex absorption seen spectroscopically. We argue that our results are robust because they are based on the joint temporal–spectral analysis of broadband X-ray data. The spectrum of V2731 Oph is more highly absorbed. Through our analysis of the Suzaku data, we present a spectral model with nitrogen overabundance without the previously claimed soft blackbody that should be further explored. We have been unable to constrain the reflection amplitude for V2731 Oph; this and the detection of spin modulation above 10 keV suggest that it may have a tall shock. Hence, we only derive a lower limit to the mass of its WD ($>0.9 M_\odot$).

Key words: novae, cataclysmic variables – stars: individual (TV Col, V2731 Oph) – ultraviolet: stars – X-rays: binaries

1. Introduction

Intermediate polars (IPs) are a subgroup of cataclysmic variables (CVs) in which a moderately magnetic ($10^{-7}$ G) white dwarf (WD) accretes matter via Roche-lobe overflow from a companion, usually a low-mass star on or near the main sequence. An accretion disk is usually formed, and its inner part is truncated by the magnetic field, which channels the gas in accretion columns toward the magnetic poles of the WD. Strong shocks are formed in the columns, heating up the gas to a high temperature defined in the first order by the depth of the gravitational potential well of the WD ($kT \propto M_{\text{WD}}/R_{\text{WD}}$). The shocked gas subsequently settles onto the WD surface as it is cooled by radiating X-rays and cyclotron emission. Thus, the X-ray emission is intrinsically multitemperature in nature.

Information on the accretion geometry and WD mass is encoded in the intrinsic emission and its subsequent interaction with its surroundings. The observed radiation in IPs has a significant contribution from X-ray photons that have interacted with the environment, including the stellar surface of the WD itself, the accretion column, the accretion disk, and any circumstellar medium that might exist. Part of the interacting X-rays suffers photoelectric absorption inducing a deficit in the observed X-rays that is more pronounced for softer photons. Another part is reflected and results in excess in the continuum around 10–30 keV as a Compton hump and in fluorescent emission lines, notably the FeK line at 6.4 keV. The description of both components, absorption and reflection, is necessary for an in-depth understanding of the accretion geometry and characteristics of the intrinsic X-rays, which can also lead to the determination of the WD mass. This task requires wide-bandpass spectroscopy covering both soft and hard X-rays—especially because the partial-covering absorption, expected in IPs due to their complex environment, can have a similar effect on the spectral shape around the Fe K edge as reflection.

The advent of imaging hard X-ray observations using NuSTAR has allowed the detailed investigation of X-ray spectra of IPs, including both absorption and reflection (Mukai et al. 2015). While other recent papers have concentrated on deriving the WD mass using hard X-ray spectroscopy (Shaw et al. 2018), including the effects of tall shocks and a small inner radius of the disk (Suleimanov et al. 2019), concerns remain that such investigations can be compromised if inadequate attention is paid to the complex interplay of absorption, reflection, and intrinsic spectral shape. Here we present our detailed analysis of wideband X-ray spectra of two IPs, TV Col and V2731 Oph, to test the potential degeneracy in spectral analysis results. We also follow Mukai et al. (2015) in analyzing the hard X-ray spin modulation as a method to break the degeneracy.

2. The Targets

According to the Gaia DR2 parallax, TV Col is at a distance of 513±2 pc (Gaia Collaboration et al. 2016, 2018). The system has been investigated with many X-ray observatories since its first detection with the Ariel V satellite (2A 0526-328; Cooke et al. 1978). EXOSAT observations (~2–10 keV) revealed it to be an absorbed hard X-ray emitter with flux modulated at
3. Observations and Data Reduction

Details of the X-ray observations used in this investigation are given in Table 1. The NuSTAR satellite observed TV Col on 2014 May 11 for 49.7 ks (ObsID 30001020002). The system was also simultaneously observed by Swift for ~1.9 ks on 2014 May 12 (ObsID 00080734001). For the first time, we explored the corresponding NuSTAR FPMA/FPMB and Swift/XRT data sets to carry out consistent wideband spectroscopy from 0.35 to 75 keV. We also investigated five other Swift/XRT observations in order to obtain clues on the spectral variations of the source.

We investigated V2731 Oph using a NuSTAR observation carried out for ~50 ks on 2014 May 14 (ObsID 30001019002), for which there is no contemporaneous X-ray observation with another satellite. However, we used archival observations, namely, XMM-Newton/EPIC (2005 August 29, 13.5 ks; ObsID 0302100201), Suzaku (2009 February 16, 32.9 ks; ObsID 403026010), and the longest Swift (2007 February 23, 12.8 ks; ObsID 00035086002) observations in order to evaluate the source in soft X-rays and discuss implications for the description of the system.

The data reduction followed standard procedures with the appropriated tools (with HEASOFT-v6.22 for the NuSTAR, Swift, and Suzaku data and SAS-v16.1.0 for the XMM-Newton data) with the latest calibration files that were available in 2017 November. We use different extraction regions for the NuSTAR modules, FPMA and FPMB, based on their individual images to accommodate the relative astrometric offset between them.

All spectra from both TV Col and V2731 Oph were binned such that each energy bin contains at least 25 counts, except for the Swift/XRT data of TV Col. For those data, a 5 count limit was adopted, as enforcing 25 counts per bin, making Gaussian errors a reasonable approximation, would have meant too few spectral bins for the spectrum to be useful. Spectral fits were done with Xspec v12.9.1.m by using the χ2 as fit and test statistics but applying the C statistic for the fit in all cases in which the Swift/XRT data of TV Col were investigated—as it is appropriate to low count per energy bin, following the deviation from Gaussian to Poisson data.

4. X-Ray Spectroscopy

Throughout this work, we use XSPEC and models available within it to carry out modeling of XMM-Newton, Swift, Suzaku, and NuSTAR X-ray spectra. Two optically thin thermal models were used: a single-temperature APEC model and a
multitemperature cooling-flow model with MKCFLOW, also based on APEC (with the switch parameter equal to 2), which is model M1. In addition, an optically thick blackbody model, BBODY, was included as necessary. The abundance table applied in both optically thin thermal models was that of Asplund et al. (2009). The redshift required by construction in the MKCFLOW model cannot be zero. It was assumed to be 8.5867 \times 10^{-5} for TV Col and 5.367 \times 10^{-7} for V2731 Oph, as estimated from the Gaia DR2 distances (513.2\pm30 and 2300\pm270 pc, respectively; Gaia Collaboration et al. 2016, 2018) and standard cosmological values of XSPEC. The low temperature of the MKCFLOW was fixed to the minimum value allowed by the model (kT = 80.8 eV).

The interaction of the radiation with matter was accounted for by the following models. For the photoelectric absorption by cold matter, we use both the single-absorber PHABS and the complex-absorber pwab (Done & Magdziarz 1998) components. The usual partial-covering absorber models (either the PCFABS multiplicative model or the PARTCOV convolution model combined with any absorption model) represent two lines of sight, one with and one without an intervening absorber. However, the absorption in the pre-shock accretion columns of magnetic CVs requires a model with a continuous distribution of covering fraction as a function of column height. Done & Magdziarz (1998) developed pwab to represent this situation, in which the covering fraction is assumed to be a power-law function of the column (β index, from a minimum (N_{H,\text{min}}) to a maximum (N_{H,\text{max}}) equivalent hydrogen columns). An EDGE component was used to account for a warm absorber, only necessary in the case of V2731 Oph, associated with the O VI absorption edge at 0.74 keV. The REFLECT model was applied when investigating the reflection of X-rays in the systems, in all cases keeping the (unconstrained) inclination angle (i) of the reflecting surface equal to the default value in the model, such that cos(i) is equal to 0.45.

The GAUSS model was used to describe the 6.4 keV fluorescence iron line, with the line energy (E_x) and width (σ) fixed to 6.4 and 0.01 keV, respectively. An energy-independent multiplicative factor, the CONSTANT model, was included to account for the cross-calibration uncertainties of the different instruments (namely, the impact on normalization in spectral modeling) when two or more spectra were used in simultaneous fits. CONSTANT also helps with source flux variability, since the observations are not all simultaneous. All parameters cited above as being fixed were not constrained when they were allowed to vary freely during the fit.

We notice that the statistical significance for the NuSTAR and Swift simultaneous fit of the TV Col spectra is biased to the NuSTAR data, and thus the visual check was crucial to choose between the models. For TV Col, we started with the simplest model based on single absorption for the two optically thin thermal models cited above (APEC and MKCFLOW; M1), then added the reflection model (M2), replaced the reflection model with the partial-covering model (M3), and finally, used both partial-covering and reflection models (M4). In all cases, a Gaussian line at 6.4 keV was added to describe the Fe Kα fluorescence feature. Some Swift spectra of TV Col presented an excess in soft X-rays that was accounted for as an additional thermal component (M5). Thus, the four initial models are a subgroup of M5, as described in Table 2. For V2731 Oph, the starting point was the result of de Martino et al. (2008) from XMM-Newton and INTEGRAL data. Finally, the model applied to the system was CONSTANT*PHABS*PWAB*EDGE (MKCFLOW + APEC + BBODY + GAUSSIAN). Table 2 summarizes the models.

When using the REFLECT component, we extended the energy range over which the model is calculated to 100 keV, because photons with energies above the instrumental coverage can be Compton down-scattered to the energy range which is covered by the instrument (command ENERGIES EXTEND HIGH 100.0, in XSPEC). The output spectrum was limited to 80 keV to speed up the calculation of the spectrum (command XSET REFLECT_MAX_E 80.0 in XSPEC).

### 4.1. TV Col

TV Col is among the brightest IPs in the hard X-ray band (Pretorius & Mukai 2014). Its X-rays are due to optically thin, thermal plasma, as supported by the strong Fe K line complex. Because of its Galactic latitude of −30°7 and distance of 513.2 pc, most of the interstellar medium (ISM) in its direction is between us and TV Col. However, the system occupies a relatively unobscured part of the Galaxy with an integrated HI column density estimate of only \sim 2.39 \times 10^{20} \text{ cm}^{-2} (Kalberla et al. 2005). Thus, the X-rays from TV Col are only slightly affected by the ISM, and any absorption we measure is due to local contributions. These circumstances make it an ideal target for a detailed study of intrinsic absorbers in the system and therefore of reflection effects. We base our spectral analysis on these two premises and proceed from the simplest model to more complex ones until satisfactory fits are obtained.

#### 4.1.1. Broadband Spectroscopy from Simultaneous Swift and NuSTAR Observations

We first investigate TV Col by simultaneously fitting the contemporaneous NuSTAR (FPMA + FPMB; 3–60 keV) and Swift/XRT spectra (0.35–10 keV; Section 3) that together

<table>
<thead>
<tr>
<th>Target</th>
<th>Model</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>TV Col</td>
<td>M1</td>
<td>CONSTANT<em>PHABS</em>[APEC or MKCFLOW]+GAUSSIAN</td>
</tr>
<tr>
<td></td>
<td>M2</td>
<td>CONSTANT<em>PHABS</em>[EDGE][APEC or MKCFLOW]+GAUSSIAN</td>
</tr>
<tr>
<td></td>
<td>M3</td>
<td>CONSTANT<em>PHABS</em>[PWAB][APEC or MKCFLOW]+GAUSSIAN</td>
</tr>
<tr>
<td></td>
<td>M4</td>
<td>CONSTANT<em>PHABS</em>[PWAB*EDGE][APEC or MKCFLOW]+GAUSSIAN</td>
</tr>
<tr>
<td></td>
<td>M5</td>
<td>CONSTANT<em>PHABS</em>[PWAB*EDGE][APEC or MKCFLOW]+GAUSSIAN</td>
</tr>
<tr>
<td>V2731 Oph</td>
<td>M6</td>
<td>CONSTANT<em>PHABS</em>[PWAB*EDGE][APEC+MKCFLOW+BBODY+GAUSSIAN]</td>
</tr>
<tr>
<td></td>
<td>M7</td>
<td>CONSTANT<em>PHABS</em>[PWAB][APEC+REFLECT*MKCFLOW+BBODY+GAUSSIAN]</td>
</tr>
<tr>
<td></td>
<td>M8</td>
<td>CONSTANT<em>PHABS</em>[PWAB][APEC+MKCFLOW+GAUSSIAN]</td>
</tr>
<tr>
<td></td>
<td>M9</td>
<td>CONSTANT<em>PHABS</em>[PWAB][VAPEC+MKCFLOW+BBODY+GAUSSIAN+GAUSSIAN+GAUSSIAN]</td>
</tr>
</tbody>
</table>
covered the wide energy range from 0.35 to 60 keV. The iron line complex (via NuSTAR) and the soft part of the spectrum (via XRT) were always included, which played a key role in disentangling the models.

A thermal model affected by a single absorption component (M1) with either APEC and MKCFLOW does not describe the data. It fails in the description of the continuum, especially at low energies (see Figure 1). However, this simple model immediately reveals the presence of a complex absorption pattern in the system. This model underestimates the flux for $E < 1.5$ keV appreciably, showing that the absorber with a high column density that is required to explain the spectral shape at higher energies absorbs too many soft photons. Similar results were obtained when including the reflection component (M2). The fit was substantially improved when the reflection component was replaced by the partial-covering model (M3) but still yielded an unacceptable description for energies up to $\sim 6$ keV, below which the model oscillates between underestimating and overestimating the flux. Finally, the reflection was added to M3 by using the M4 model. This model significantly improved the fit over the whole spectrum, as described below.

Contrary to the first three models, M4 describes the continuum from 0.35 to 60 keV (see Figure 1). The distinction between model M4 using APEC (M4a) or MKCFLOW (M4m) comes from the description of the Fe K complex and the surrounding continuum. While the spectral fit from APEC substantially underestimates the flux from the ionized Fe XXV line, the MKCFLOW model describes both it and the Fe XXVI lines and results in a better description of the continuum at $\sim 4–8$ keV—M4m, the assumed model for TV Col in this work, resulting in a $\chi^2_r$ of 0.95 for 1007 degrees of freedom.

We present the best-fit parameters for M4m in Table 3. The equivalent hydrogen column from the PHABS model is constrained to be less than $3.0 \times 10^{20}$ cm$^{-2}$ such that any intrinsic absorption would be mitigated by the effect of the dominant local partial-covering absorber. Thus, although the values of all parameters are still mutually consistent at 1σ, we assume a conservative upper limit by fixing the column value to the total Galactic column in the direction of TV Col ($2.39 \times 10^{20}$ cm$^{-2}$, Kalberla et al. 2005). This procedure improves the determination of the absorption derived from the partial-covering absorption pwab model, resulting in

<table>
<thead>
<tr>
<th>Component</th>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>PHABS</td>
<td>$N_H$ (10$^{22}$ cm$^{-2}$)</td>
<td>0.0230*</td>
</tr>
<tr>
<td></td>
<td>$N_{H_{\text{min}}}$ (10$^{22}$ cm$^{-2}$)</td>
<td>$10^{-7}$</td>
</tr>
<tr>
<td></td>
<td>$N_{H_{\text{max}}}$ (10$^{23}$ cm$^{-2}$)</td>
<td>$10^{5.3}$</td>
</tr>
<tr>
<td></td>
<td>$\beta$</td>
<td>$-0.41^{+0.04}_{-0.03}$</td>
</tr>
<tr>
<td>REFLECT</td>
<td>refl</td>
<td>$0.88^{+0.13}_{-0.13}$</td>
</tr>
<tr>
<td></td>
<td>cos(i)</td>
<td>0.45*</td>
</tr>
<tr>
<td>MKCFLOW</td>
<td>$kT_{\text{low}}$ (keV)</td>
<td>0.0808*</td>
</tr>
<tr>
<td></td>
<td>$kT_{\text{max}}$ (keV)</td>
<td>31.0$^{+1.1}_{-1.1}$</td>
</tr>
<tr>
<td></td>
<td>$Z$ ($Z_\odot$)</td>
<td>0.49$^{+0.04}_{-0.03}$</td>
</tr>
<tr>
<td></td>
<td>Redshift</td>
<td>$1.197 \times 10^{-7}$*</td>
</tr>
<tr>
<td></td>
<td>Switch</td>
<td>2</td>
</tr>
</tbody>
</table>

$\chi^2_r$/d.o.f. | 0.95/1007 |

Note. (*) fixed parameter (see text).

$N_{H_{\text{max}}} = 1.05^{+0.17}_{-0.08} \times 10^{23}$ cm$^{-2}$ and $\beta = -0.41^{+0.03}_{-0.04}$. The primary source of X-rays is a high-temperature plasma with an abundance of 0.49 $\pm$ 0.04 times the solar values, cooling down from a maximum temperature $kT$ of 31.0 $\pm$ 1.1 keV. If we take this as the measurement of the gravitational potential at the surface of the WD, then its mass is 0.735 $M_\odot$ (following Aizu 1973). Our subsequent analysis justifies this assumption as we discuss in Section 6.2.

We find that the reflection of the primary X-rays makes a nonnegligible contribution to the observed X-rays. According to the best-fit model (M4m), the reflection amplitude is constrained to be $0.88^{+0.13}_{-0.13}$. The reflection accounts for about 16% of a total unabsorbed flux of $\sim 1.37 \times 10^{-10}$ erg s$^{-1}$ cm$^{-2}$ at 0.3–75 keV, increasing to 30% of a total of $\sim 5.3 \times 10^{-11}$ erg s$^{-1}$ cm$^{-2}$ at 10–50 keV (and 7.6% of $\sim 7.9 \times 10^{-11}$ erg s$^{-1}$ cm$^{-2}$ at 0.3–10 keV). On 2014 May 11/12, TV Col was observed with a luminosity of $4.3 \times 10^{33}$ erg s$^{-1}$ at 0.3–75 keV and a bolometric X-ray luminosity of $4.6 \pm 0.3 \times 10^{33}$ erg s$^{-1}$.

The NuSTAR data suggest a pronounced fluorescent iron line at 6.4 keV with an equivalent width (EW) estimated in $179^{+70}_{-64}$ eV. As we show below, this value is significantly higher than that derived for V2731 Oph with the same instrument, even though V2731 Oph is significantly more absorbed than TV Col. Thus, the fluorescent line, at least for TV Col, seems to have a contribution not only from the absorber but also from the reflector.

4.1.2. Spectral Evolution from Swift/XRT Observations

We investigated other archival Swift/XRT observations of TV Col individually in order to evaluate its spectral evolution (Table 1). Thermal models resulted in unconstrained values for the plasma temperature and abundance, while they were consistent with those obtained from the simultaneous NuSTAR and Swift observations. Subsequently, we fitted the spectra by assuming the model M4m, keeping the plasma temperature and abundance values of the MKCFLOW and the parameters of the REFLECT component fixed to those determined previously from the NuSTAR/Swift observations.

Figure 1. TV Col: NuSTAR/FPMA and Swift/XRT spectra fitted with models M1 (magenta), M2 (blue), M3 (green), and M4m (black; see text for further details). The lower panel shows the residual with respect to M4m.
of 2014 May 11/12, presented in Table 3. We also adopted the same fixed parameter values as done previously for the M₄₃ model. The best-fit spectral parameters are summarized in Table 4.

There is an excess emission below ~1 keV that indicates the presence of an additional thermal component for two observations (00035282002 and 00037150005) and is suspected for two others (00035282001 and 00037150003). Its description suggests that it is more likely due to a cool, optically thin plasma (\(kT \sim 0.15\) keV), but a blackbody emission (\(kT \sim 0.12\) keV) cannot be ruled out. No strong change in the spectral shape of TV Col is observed in the first five Swift observations listed in Table 1, but they still exhibit variability in the absorbers and the unabsorbed flux at 0.3–10 keV. Remarkably, during the fifth observation, the values increased by 50%–100%.

### 4.2. V2731 Oph

It is clear from the investigation of TV Col that simultaneous, or at least contemporaneous, broadband coverage is essential in describing the effects of both absorption and reflection of X-rays and hence in characterizing the system. Even though V2731 Oph has been observed with high signal-to-noise ratios in soft and hard X-rays, the coverage in both energy bands with different satellites was not contemporaneous.

We started by comparing the previous XMM-Newton observation (carried out on 2005 August 29) already reported by de Martino et al. (2008) with the Suzaku (2009 February 16; Yuasa et al. 2010) and the longest Swift (2007 February 23) archival observations of V2731 Oph (Table 1). Those observations were investigated separately and, subsequently, via a joint fit with the 20–75 keV NuSTAR (2014 May 14) spectra. For the purpose of obtaining the base fit of the XMM-Newton data below 10 keV, we fit them jointly with the NuSTAR spectra restricted to the 20–75 keV range, allowing us to utilize the parameters that best describe the high-energy shape of the spectrum. In this procedure, we ignored the NuSTAR data below 20 keV because of our suspicion (later confirmed) that there is more spectral variability at low energies. We then proceeded with an investigation of the NuSTAR observations of the system separately using the whole available spectral range (3–75 keV), and then with the Swift and Suzaku spectra, also separately, in all cases fixing the values of the cooling-flow component to those derived from the simultaneous fit of the XMM-Newton and the 20–75 keV NuSTAR spectra. Figure 2 shows the spectra.

#### 4.2.1. Clues about the Spectral Evolution

As reported by de Martino et al. (2008), an XMM-Newton observation revealed a complex X-ray spectrum of V2731 Oph. A good fit required multiple thermal plasma components, with both a cold and another hot optically thin plasma, and an additional blackbody emission. Once produced, the X-rays are reflected in the system separately using the whole available spectral range (3–75 keV), and then with the Swift and Suzaku spectra, also

---

**Table 4**

<table>
<thead>
<tr>
<th>Swift/XRT (ObsID)</th>
<th>(N_{\text{H}}\text{max} (10^{22} \text{ cm}^{-2}))</th>
<th>(\beta)</th>
<th>APEC</th>
<th>BBODY</th>
<th>(F_{\text{unabs,0.3–7keV}} (\text{erg cm}^{-2} \text{ s}^{-1}))</th>
<th>(\chi^2/\text{d.o.f.})</th>
</tr>
</thead>
<tbody>
<tr>
<td>00035282001</td>
<td>13.8 ± 2.4</td>
<td>-0.41 ± 0.03</td>
<td>...</td>
<td>...</td>
<td>6.5</td>
<td>1.04/398</td>
</tr>
<tr>
<td>00037150002</td>
<td>12.7 ± 2.6</td>
<td>-0.38 ± 0.04</td>
<td>0.14 ± 0.06</td>
<td>0.12 ± 0.01</td>
<td>6.7</td>
<td>1.04/396</td>
</tr>
<tr>
<td>00037150003</td>
<td>12.7 ± 3.0</td>
<td>-0.38 ± 0.02</td>
<td>0.11 ± 0.05</td>
<td>0.15 ± 0.02</td>
<td>6.6</td>
<td>1.04/396</td>
</tr>
<tr>
<td>00037150005</td>
<td>13.6 ± 3.5</td>
<td>-0.40 ± 0.09</td>
<td>...</td>
<td>...</td>
<td>6.9</td>
<td>0.88/65</td>
</tr>
<tr>
<td>00037150006</td>
<td>17.2 ± 3.9</td>
<td>-0.37 ± 0.02</td>
<td>0.18 ± 0.02</td>
<td>0.12 ± 0.03</td>
<td>8.6</td>
<td>1.00/389</td>
</tr>
<tr>
<td>00037150007</td>
<td>15.9 ± 2.1</td>
<td>-0.35 ± 0.03</td>
<td>0.18 ± 0.05</td>
<td>0.15 ± 0.02</td>
<td>7.8</td>
<td>1.01/297</td>
</tr>
<tr>
<td>00037150008</td>
<td>13.4 ± 2.3</td>
<td>-0.36 ± 0.04</td>
<td>0.18 ± 0.06</td>
<td>...</td>
<td>7.9</td>
<td>1.01/297</td>
</tr>
<tr>
<td>00037150009</td>
<td>25.3 ± 3.7</td>
<td>-0.43 ± 0.02</td>
<td>0.15 ± 0.03</td>
<td>...</td>
<td>11.2</td>
<td>1.00/389</td>
</tr>
<tr>
<td>31.7 ± 3.5</td>
<td>-0.45 ± 0.02</td>
<td>...</td>
<td>0.09 ± 0.02</td>
<td>...</td>
<td>11.6</td>
<td>1.03/389</td>
</tr>
</tbody>
</table>

**Note.** From M₄₃ or M₅ (see Table 2).
thermal component with the MKCFLOW model, in line with the case of our other target, TV Col, and as it is expected for IPs. Thus, the final model is M6: CONSTANT’PHABS’PWAB’EDGE’ (MKCFLOW+APEC+BBODY+GAUSSIAN).

Model M6 describes the XMM-Newton data well, resulting in $\chi^2_\nu = 1.05$ for 834 degrees of freedom, but the hottest component of the MKCFLOW component converged to the hard limit of $kT = 79.9$ keV. The coldest component, as for the case of TV Col, was not constrained and therefore fixed to $kT = 80.8$ eV. We added to the fit the NuSTAR spectra limited to the 20–75 keV energy range. This inclusion improves the statistic to $\chi^2_\nu = 1.01$ for 962 degrees of freedom while resulting in well-constrained values (Table 5). Starting with the plasma parameters, the temperature derived from the MKCFLOW model peaks at $kT = 47.6^{+2.4}_{-1.5}$ keV. A cold ($kT = 0.17^{+0.03}_{-0.02}$ keV), optically thin plasma component is necessary to account for a substantial part of the ~0.5–1.5 keV range that is not described by the MKCFLOW model, even taking its low temperature as a free parameter during the fit. A fit without the cold plasma but with the low temperature left to vary free only achieves $\chi^2_\nu = 1.15$. On the other hand, we confirm that a blackbody component (with $kT = 0.094^{+0.002}_{-0.002}$ keV) is a good description for the excess emission in soft X-rays not explained by the optically thin plasma emission. However, this is unphysical for a WD, as is argued at the end of this section. In terms of absorption, the modeling with pwab resulted in a complex structure with $N_{H,\text{max}} = 156^{+270}_{-120} \times 10^{22}$ cm$^{-2}$ and $\beta = -0.68^{+0.01}_{-0.01}$. Although poorly constrained, the lower limit to $N_{H,\text{max}}$ is still high: at least $\sim 10^{24}$ cm$^{-2}$. The $N_{H,\text{min}}$ parameter, unconstrained, was fixed to 10$^{15}$ cm$^{-2}$, the minimum value allowed by the model. The PHABS resulted in the equivalent to $N_H = (3.3 \pm 0.2) \times 10^{21}$ cm$^{-2}$. Such a value is higher than the total Galactic H1 column density in the direction of V2731 Oph of about 1.6 $\times 10^{21}$ cm$^{-2}$ estimated by Kalberla et al. (2005) but slightly lower than the value of 3.9 $\times 10^{21}$ cm$^{-2}$ derived from the 3D dust mapping with Pan-STARRS 1 (Green et al. 2018). The abundance was tied to the APEC and MKCFLOW models, resulting in $Z = 0.30 \pm 0.09 Z_\odot$. This value is consistent with the two values reported by de Martino et al. (2008) of 0.33$^{+0.17}_{-0.37} Z_\odot$ from the 0.3–10 keV XMM-Newton EPIC data alone and 0.40$^{+0.07}_{-0.08} Z_\odot$ when the 20–100 keV INTEGRAL/ISGRI spectrum was also included in

\begin{table}[h]
\centering
\caption{Table 5}
\begin{tabular}{cccccccc}
\hline
PHABS & pwab & $N_H$ & $N_{H,\text{max}}$ & $\beta$ & EDGE & APEC & BBODY & MKCFLOW
\hline
\end{tabular}
\end{table}

Notes.

\begin{itemize}
\item $N_{H,\text{max}} = 10^{15}$ cm$^{-2}$.
\item $\beta$ Threshold energy equal to 0.74 keV.
\item $kT_{\text{low}} = 80.8$ eV.
\item $Z$ Tied to the APEC, MKCFLOW, and, when present, REFLECT components for all of the elements.
\item Using only the 20–75 keV NuSTAR spectra (FPMA and FPMB).
\item Fixed to the values of the joining XMM + NuSTAR analysis. For the REFLECT component, when applied, the reflection scaling factor is equal to 1 and $\cos(\iota) = 0.45$. The lack of coverage for $E < 3$ keV from NuSTAR data does not allow a reliable determination of the flux at 0.3–10 keV. For the Suzaku analysis, see text.
\end{itemize}
the analysis. The energy of the EDGE component was fixed at 0.74 keV (corresponding to the O VII absorption edge reported by de Martino et al. 2008).

The aim of this analysis is to compare how the spectral energy distribution has evolved when comparing observations carried out at different epochs. In this exercise, we explore the longest archival Swift observations and the Suzaku observation of V2731 Oph, verifying the consistency of the spectra with the model used to describe the 0.3–10 keV XMM-Newton plus the 20–75 keV NuSTAR spectra.

We first investigate the Swift/XRT spectrum (ObsID 00035086002). The model and values derived from the joint XMM-Newton and NuSTAR analysis, keeping only the normalization as free parameters, result in an unacceptable description of the Swift spectrum ($\chi^2 = 3.18$). The statistic is slightly improved when allowing the parameter of the PHABS to vary ($\chi^2 = 2.54$). There is no improvement when allowing the $N_{\text{H, max}}$ parameter of the $\text{pwab}$ model free to vary during the fit, and its value is unconstrained. On the other hand, the fit is significantly improved when the $\beta$ parameter of this component is allowed to vary ($\chi^2 = 1.59$), again keeping the lower limit for the absorption fixed. The statistic improves to $\chi^2 = 1.14$ when the absorption depth of the EDGE component is also a free parameter. Allowing the plasma temperature of the APEC component to also vary improves the fit description ($\chi^2 = 1.06$). On the other hand, there is no improvement when allowing the temperature of the BBODY component and the high-temperature parameter of the MKCFLOW model to vary. As their values are consistent with those derived from the XMM-Newton plus NuSTAR analysis, we kept them fixed to the corresponding values. The best-fit spectral parameters are summarized in Table 5. The analysis revealed a significant change in the partial-covering absorption and the temperature of the cold plasma component, while the spectral energy distribution of hard X-rays remained essentially unchanged.

We extended the same methodology to the Suzaku XIS0, XIS1, and XIS3 spectra. Allowing only the normalization to vary during the fit resulted in $\chi^2 = 6.30$. As for the XRT spectrum, the description is improved when allowing the absorption column of the PHABS ($\chi^2 = 3.70$), the $\beta$ parameter of the $\text{pwab}$ model ($\chi^2 = 2.34$), the absorption depth of the EDGE component ($\chi^2 = 1.54$), and the plasma temperature of the APEC component ($\chi^2 = 1.42$) to vary. The column derived from the PHABS model is virtually equal to zero ($N_{\text{H}} \sim 10^{16}$ cm$^{-2}$) and unphysical, and this component was removed without impacting the fit. The lower limit of the absorption in the PHABS converges to the minimum value when assumed as a free parameter. In contrast with the Swift spectrum, the fit for the Suzaku spectra is statistically improved when the temperature of the BBODY component is free during the fit ($kT \sim 0.18$ keV; $\chi^2 = 1.22$). Table 5 includes the best-fit parameters of the Suzaku observation.

However, there are four significant issues with the fit to the Suzaku data. First, the model underestimates the flux around 0.5 keV and also around 0.8 keV (see Figure 3). Second, the column density for the PHABS component is unrealistically low in comparison with the total Galactic H I column density in this direction (≈1.6 × 10$^{21}$ cm$^{-2}$ according to Kalberla et al. 2005 and 3.9 × 10$^{21}$ cm$^{-2}$ from the 3D dust mapping with Pan-STARRS 1 by Green et al. 2018). Given the large distance to V2731 Oph (at least 2 kpc), we expect that a substantial fraction of this column is between V2731 Oph and the solar system. The fact that the $N_{\text{H}}$ for the PHABS component was negligible when fitting the Suzaku data, while it was higher than the Galactic value in the XMM-Newton and Swift data, points to a possible problem with the fit. Third, the blackbody temperature, already worryingly high in the XMM-Newton fit, is so high as to be clearly unphysical for a WD (Williams et al. 1987); we will return to this point in Section 6.1. Fourth, this model does not fit the XIS1 data, which show significant residuals below ~0.8 keV, especially around 0.5 keV. While some cross-calibration issues among the XIS units of Suzaku are commonly seen, what we see in V2731 Oph is far beyond the residuals seen in other Suzaku observations. One likely explanation is that the model is wrong but nevertheless works well enough, phenomenologically, with XMM-Newton, Swift/ XRT, and Suzaku XIS0+XIS3 data (Table 5). In fact, the best-fit spectral parameters from the XIS0+XIS3 data with M6 and M7–like models are similar to those obtained from the XIS0 +XIS1+XIS3 data. Because the Suzaku/XIS1, using an advanced backside-illuminated CCD chip, has a relatively high effective area below 0.8 keV and a superior spectral resolution at these energies to those of the other cameras used in this work, some inadequacies of these models become readily visible in the XIS1 data. Thus, we explore in the next section an alternative spectral description of V2731 Oph.

4.2.2. Alternative Spectral Description

The Suzaku/XIS1 spectrum indicates a more pronounced excess around 0.5 keV than in other spectra, suggesting the presence of an intense N VII Lyα line (see red line from M6 in Figure 3). In order to check for an overabundance of $N$, we replace APEC with VAPEC and MKCFLOW with VMCFLOW and apply the model without reflection to the Suzaku XIS0, XIS1, and XIS3 spectra simultaneously, as the variants of the first models that allow the user to set the abundance of the main elements individually. The abundance for the VAPEC and VMCFLOW were tied together, allowing $Z_{\odot}$ to vary freely during the fit but keeping all other elemental abundances equal to 0.30 $Z_{\odot}$. The fit improves significantly with a better description of the soft tail ($\chi^2_{\text{red}}$ from 1.50 to 1.25; yet unacceptable and not presented). It indicates $Z_{\odot} = 3.2(\pm 0.3)Z_{\odot}$ while the normalization of the BBODY
component tends to zero; therefore, such a component would not be necessary anymore. The PHABS \( N_\text{H} \) value of \( 7.4^{+1.0}_{-0.9} \times 10^{20} \text{ cm}^{-2} \) is consistent with the ISM value, while the complex absorption via \( \text{pwab} \) indicates an \( N_{\text{H,max}} \) of at least \( 10^{24} \text{ cm}^{-2} \) with \( \beta \) equal to \( -0.90 \pm 0.01 \). Another difference with respect to the values inferred from the other spectra is the substantially lower absorption depth associated with the oxygen edge of 0.21 \( \pm \) 0.05. We then assumed the O abundance as a free parameter during the fit, as well as the Fe abundance, which was tied to that of Ni. The fit resulted in \( Z_\text{O} = 16.9^{+2.3}_{-2.1} Z_\text{Fe} \), \( Z_\text{Ni} = 1.3^{+0.2}_{-0.1} Z_\text{O} \), and \( Z_{\text{Fe}(=Z_{\text{Ni}})} = 0.19 \pm 0.02 Z_\text{Fe} \), with \( \chi^2 \) of 1.19. 

The analysis presented in Section 4.2.1, the PHABS results in a unrealistically low column density. The results are summarized in Table 6.

The model has the O VII edge at 0.74 keV, and some of the oxygen ions that absorbed such photons would emit the O VII He-like triplet. We then added a Gaussian line to the variable abundance model, and its energy centroid converged to 0.58 keV, the expected value of the O VII triplet. It results in \( \chi^2 \) of 1.15, but this time not only with low column density from the PHABS component but also underestimating the spectra below 0.6 keV. We then added the BBODY component, resulting in a better description. The continuum below 0.6 keV is well described, the column density from PHABS converges to \( \sim 3.8 \times 10^{21} \text{ cm}^{-2} \), and the temperature of the BBODY, contrary to the model presented in Section 4.2.1, has a low temperature of \( \sim 28 \text{ eV} \) but an unrealistic normalization of 2.5. The \( \chi^2 \) is 1.16.

Because of the excess observed around 0.90–0.94 keV, which is consistent with the position of the Ne IX triplet, we added a new Gaussian component. The centroid energies of the Gaussian lines converge to 0.58 \( \pm \) 0.01 and 0.94 \( \pm \) 0.01 keV, in good agreement with what is expected for the O VII and Ne IX He-like triplets, respectively. For the blackbody
component, we derive $kT = 39^{+5}_{-4}$ eV and a normalization of 
\(4.3^{+2.1}_{-1.4} \times 10^{-2}\). The column from the PHABS component 
is $2.9^{+0.7}_{-0.5} \times 10^{21}$ cm\(^{-2}\), consistent with the value 
expected from the ISM in the light of sight of V2731 Oph. The fit also 
results in $N_{T,max} = 68^{+10}_{-20} \times 10^{22}$ cm\(^{-2}\) and $\beta = 0.77^{+0.02}_{-0.01}$ for p\(\alpha\)ab 
and $kT = 0.49 \pm 0.02$ keV for v\(\alpha\)pec. For the VMCFLOW 
component, we kept $k_{T,max} = 47.6$ keV. Also, the fit, with $\chi^2_{\text{red}} = 1.12$, resulted in $Z_N = 69^{+16}_{-10}$ Z\(_o\), $Z_O = 4.6^{+0.8}_{-0.5}$ Z\(_o\), and $Z_{Fe}(=Z_{Ni}) = 0.6^{+0.1}_{-0.1}$ Z\(_o\). The best-fit spectral parameters are 
presented in Table 6. In Figure 3, we present the fits from M6 and M9 for Suzaku/XIS1 (red and black lines, respectively), 
where we also present the XIS0 and XIS3 spectra and the 
corresponding results from M9.

We applied the above models to the XMM-Newton EPIC spectra. 
The fit with variable $Z_N$ was found to be statistically 
weaker than the previous description using model M6 (Table 5), 
with a $\chi^2_{\text{red}}$ of 1.14. When both $Z_N$ and $Z_O$ are allowed to be 
free, without the O absorption edge, it results in difficulties in 
explaining the emission from 0.7 to 0.8 keV. Finally, we 
applied M8 (see Table 2) to the combined XMM-Newton 
and 20–75 keV NuSTAR data and obtained a $\chi^2_{\text{red}}$ of 1.08 (compared 
to 1.01 for M6) with similar parameter values when exploring 
only the XMM-Newton spectra, particularly $k_{T,max}$ which 
shows no statistically significant changes. The results are 
shown in Table 6. The addition of a BBODY and the two 
GAUSSIAN lines as in M9 does not improve the fit. With a low 
temperature ($kT \sim 15$ eV), the BBODY component converges to 
a normalization of only $\sim 10^{-19}$, meaning that such an addition 
is not supported by the data. A GAUSSIAN component at 
0.94 keV, as applied to the Suzaku data, is not constrained by 
the fit, and fixing its parameters to the values derived from the 
Suzaku spectra does not improve the fit. Also, although still in 
agreement with the XMM-Newton data, the GAUSSIAN line 
around 0.58 keV results in no significant improvement in the 
fit, still with a $\chi^2_{\text{red}}$ of 1.08. The values derived from M8 (Table 6) are mutually consistent with those 
when applying M9 to the 0.3–10 keV XMM-Newton plus the 20–75 
keV NuSTAR spectra, although these fits are not shown.

Thus, even though we have not found a completely 
satisfactory fit to the soft X-ray spectrum, our idea to combine 
XMM-Newton and 20–75 keV NuSTAR data appears to be 
valid. First, the spectral energy distributions for hard X-rays in 
both sets of data are mutually consistent and confirmed from 
the whole spectral range covered by NuSTAR (Section 4.2.3). 
The difficulties with either model in describing the Suzaku 
data with all applied models and the XMM-Newton spectra with the 
alternative M8 and M9 models are limited to the soft end of the 
spectrum (<1 keV). We notice that the elemental abundances 
derived independently from the Suzaku and XMM-Newton 
spectra do not converge; both indicate that anomalies are 
present, at least for the N, O, and Fe. Second, the absorbed and 
unabsorbed 20–75 keV fluxes differ by less than 5%, showing 
that the absorption such as detected in the system, even though 
it is very high, has no significant rule in this spectral region. 
In addition, the investigation revealed that the luminosity of the 
source at 20–75 keV during the XMM-Newton observation is 
\(~35\%\) less than that observed during the NuSTAR observation, 
with the unabsorbed flux varying from \(~2.5 \times 10^{11} \text{ erg cm}^{-2} \text{s}^{-1}\) (over 9 yr). The estimated unabsorbed 
20–75 keV flux from both the Swift and Suzaku data sets is \(~2.1 \times 10^{11} \text{ erg cm}^{-2} \text{s}^{-1}\) (over 2 yr). Since the soft X-ray 
complexity is limited to energies below 0.8 keV, we will 
proceed by returning to the spectral model of de Martino et al. 
(2008) in the analysis of hard X-ray data and comment on the 
soft X-ray complexity in Section 6.1.

4.2.3. Spectroscopy Using the Full NuSTAR Data

The variability of V2731 Oph in X-rays prevents the use of 
noncontemporaneous campaigns to carry out a simultaneous 
spectral fit. Therefore, we instead explored the full spectral 
range covered by NuSTAR (3–75 keV) initially using model M6. As 
expected, the PHABS (that goes virtually to zero; $N_H = 10^{13}$ cm\(^{-2}\)), BBODY, APEC, and EDGE components do 
not contribute to the fit, and they were removed from the model. A fit that keeps the $N_{T,max}$ of the p\(\alpha\)ab component 
fixed to $156 \times 10^{22}$ cm\(^{-2}\) and the $kT_{\text{hot}}$ of the MKCFLOW 
to 47.6 keV, as derived from the analysis of the XMM-Newton 
and 20–50 keV NuSTAR spectra, yields $\chi^2_{\text{red}} = 1.48$. Freezing 
the thermal component to 47.6 keV and allowing the $N_{T,max}$ to 
vary during the fit results in a good description of the spectra 
with $N_{T,max} = 753^{+60}_{-60} \times 10^{22}$ cm\(^{-2}\) and $\beta = -0.68^{+0.01}_{-0.00}$ for $\chi^2_{\text{red}} = 1.00$ (Table 5). The abundance was kept fixed to 0.30 Z\(_o\). 
Similar values were obtained when allowing the high 
temperature of the MKCFLOW to vary during the fit. The 
$kT_{\text{hot}}$ of 47.6^{+1.4}_{-1.2}$ keV derived from the joint NuSTAR/XMM-Newton fit suggests a WD mass of $0.92 \pm 0.04 M_{\odot}$, if the shock temperature reflects the gravitational potential just above the 
WD surface (following Aizu 1973).

4.2.4. Investigating the Hypothesis of Reflection

We move back to the spectral investigation of V2731 Oph to 
verify how the occurrence of X-ray reflection in the system 
would affect the results. Contrary to the case of TV Col, it was 
not possible to constrain the reflection—if it is present—for 
V2731 Oph. Adding the REFLECT component and allowing the 
reflection scaling factor to vary during the fits resulted, 
systematically, in values greater than 3, which are unrealistic. 
We froze this value to 1 while keeping $\cos i = 0.45$ to see how 
this conservative assumption would impact the spectral results 
when reflection is present. In doing this, we followed the same 
procedure as in the case without REFLECT: we investigated the 
EPIC XMM-Newton and 20–75 keV NuSTAR (FPMA + 
FPMB) simultaneously, then individually investigated the 
Swift/XRT, Suzaku (XIS0+XIS3 and XIS0+XIS1+XIS3), and 
3–75 keV NuSTAR spectra. The results are summarized in 
Table 5. The $kT_{\text{max}}$ of 55.1^{+6.2}_{-4.3}$ keV derived from the joint 
NuSTAR/XMM-Newton fit (with the abundance fixed to 0.3 Z\(_o\)) 
suggests a WD mass of 0.99^{+0.05}_{-0.04} M_{\odot}, if the shock temperature reflects the gravitational potential just above the 
WD surface.

The inclusion of reflection does not change the high 
temperature in the MKCFLOW model at the 1\(\sigma\) level. But this 
result can be masked by effects of the photoelectric absorption 
that is not well constrained from the NuSTAR data alone. A 
conclusive investigation of reflection in V2731 Oph demands 
high signal-to-noise spectroscopy covering at least the 
0.3–75 keV energy range. High-resolution spectroscopy would 
play a crucial role in the description of the lines in the soft 
X-rays and therefore the continuum and, finally, the intervening 
amber. As of now, our results suggest that 35\% of the total 
flux at 10–50 keV derived for V2731 Oph from the XMM-Newton 
fit can be due to reflection—similar to the fraction 
inferred for TV Col, in which the presence of reflection is clear.
show the power spectra over the range of periods we investigated 120 s. The set of panels show the power spectra over the range of periods we investigated (longer than 120 s). The blue dashed line is drawn at the known spin period of TV Col, 1909.7 s, while the red dashed line indicates the prominent peak at 2976 s. The right set of panels shows the power spectra around 1909.7 s in more detail.

Figure 4. TV Col: periodogram from NuSTAR data in three X-ray energy bands: 3–6 (bottom), 6–10 (middle) and 10–30 keV (top). The set of panels show the power spectra over the range of periods we investigated (longer than 120 s). The blue dashed line is drawn at the known spin period of TV Col, 1909.7 s, while the red dashed line indicates the prominent peak at 2976 s. The right set of panels shows the power spectra around 1909.7 s in more detail.

From the XMM-Newton (pn; on 2005 August 29) observation, we estimate an EW of 145 ± 40 eV for the fluorescent iron line at 6.4 keV. The NuSTAR data have a poorer spectral resolution but suggest a lower value on 2014 May 14 of about 69 eV, even in a situation in which X-rays seem to be more absorbed than they were during the XMM-Newton observation (Figure 2, inset). Perhaps the low EW suggests that the 6.4 keV line can be accounted for only by the absorbers with only a small contribution, if any, from reflection.

4.2.5. X-Ray Luminosity and Mass Accretion Rate

V2731 Oph is a luminous IP in the X-rays, with a high mass accretion rate. Here we concentrate on results from the XMM-Newton and NuSTAR analyses. From the cooling-flow model, we infer directly from its normalization parameter value that the mass accretion rate during the XMM-Newton observation (2005 August 29) was 5.1 ± 0.7 × 10⁻⁹ M⊙ yr⁻¹, with a bolometric luminosity of 4.2 × 10³⁶(d/2300 pc)² erg s⁻¹, while the rate during the NuSTAR observation (2014 May 14) was (8.4 ± 0.2) × 10⁻⁹ M⊙ yr⁻¹. Because NuSTAR does not cover energies below 3 keV, where the system has a significant contribution from additional components that are therefore not constrained from those data, we cannot infer the X-ray bolometric luminosity securely from the NuSTAR data. To carry out a more realistic comparison, we adopt the luminosity in the 3–75 keV band. The values are 4.4 × 10³⁶(d/2300 pc)² and 7.8 × 10³⁴(d/2300 pc)² erg s⁻¹ for the XMM-Newton and NuSTAR observations, respectively. We estimate that the 3–75 keV luminosity is about 10% less than the bolometric X-ray luminosity.

5. Timing Properties from the NuSTAR Observations

The NuSTAR observations allowed us to investigate the spin variability of both TV Col and V2731 Oph in hard X-rays. We proceeded from background-subtracted light curves in three energy bands: 3–6, 6–10, and 10–30 keV. We chose 60 s bins for TV Col, given its long spin period (resulting in 32 bins per cycle), and 10 s bins for V2731 Oph, given its short period (13 bins per cycle). Since the NuSTAR count rates of these IPs are modest, we neglected dead-time correction, which should be small. We also neglected barycentric correction to simplify the analysis procedure, since we intended to limit our analysis to the times of the NuSTAR observations. We combined the FPMA and FPMB light curves in the three bands and searched for periodic modulations using the Fourier power spectrum and the normalization according to Scargle (1982). There are no Swift data at the time of the NuSTAR observation of V2731 Oph, while that contemporaneous with the NuSTAR observation of TV Col is too short to provide conclusive results. As a timing analysis of all archival X-ray data is beyond the scope of our work, and given that an extensive body of work already exists in print, we focus on the NuSTAR observations.

5.1. TV Col

The known spin modulation in TV Col, refined by Rana et al. (2004) as 1909.7 ± 2.5 s, was not detected in the NuSTAR data. Figure 4 shows the power spectra up to 8 mHz from the three energy ranges cited above, where the blue dashed lines mark the position of the expected spin frequency. The red dashed lines in the figure mark the highest peak below 10 keV, at ~2976 s, while it is the second in power in the 10–30 keV energy range after the one at very low frequency (~96,000 s). The peak at 2976 s is statistically significant if white (i.e., frequency-independent) noise is assumed. However,
no previous reports of an \(\sim 3000 \text{ s}\) period exist, so we consider this to be a noise peak.

We show folded light curves with periods of 1909 and 2976 s in the right and left panels of Figure 5, respectively. As anticipated from the power spectrum, no modulation is associated with the spin period. Using amplitude/average convention, the relative modulation amplitudes for the 2976 s peak are \(~7.5\%\) (3–6 keV), \(~6.6\%\) (6–10 keV), and \(8.4\%\) (10–30 keV), and they can be taken as conservative upper limits of the spin (1909.7 s) signal. In comparison, Rana et al. (2004) found spin amplitudes of 14% (2–5 keV), 8.5% (5–10 keV), and 6% (10–20 keV). Such modulations would have been detectable in the NuSTAR data below 10 keV, if not above. Thus, we conclude that the X-ray spin amplitude of TV Col is variable and that we caught it in a low spin modulation state. We note that optical observations of TV Col have long indicated a variable spin modulation amplitude (see, e.g., Bonnet-Bidaud et al. 1985; Barrett et al. 1988).

5.2. V2731 Oph

The 128 s spin period of V2731 Oph (de Martino et al. 2008) and the first harmonic are clearly dominant in the periodogram presented in Figure 6. The left panels show the periodogram over the entire frequency range (0–50 mHz, from the light curves with a time bin of 10 s) in the three X-ray energy bands under investigation. All three left panels have the same \(Y\) scale. The right panels show the expanded view around the fundamental frequency (with variable \(Y\) scales), where the peak corresponding to the 128 s period is seen with its two one-cycle-per-spacecraft-orbit aliases. The spin period for V2731 Oph is estimated to be 127.981 \(\pm 0.022\) s during the NuSTAR observation, consistent with the previous determination in the optical (e.g., 127.999909(49) s; Gánsicke et al. 2005) and X-rays (e.g., 128.02 \(\pm\) 0.02 s; de Martino et al. 2008).

The folded light curves are not quite sinusoidal, although they are mostly so in the 3–6 keV range (Figure 7). The red dashed lines in the top and middle panels are copies of the 3–6 keV spin profile, showing that the main peak remained the same, but a secondary peak is very pronounced in the 10–30 keV range.

6. Discussion

6.1. Soft X-Ray Complexity of V2731 Oph

The fact that V2731 Oph has a complex X-ray emission was already reported by de Martino et al. (2008). Our analysis shows that their model cannot fit the Suzaku XIS1 spectrum. Moreover, blackbody temperatures of 0.21 and 0.18 keV, as derived from Suzaku XIS0+XIS3 and XIS0+XIS1+XIS3 spectra, respectively, are clearly unphysical for WD accretion. Considering the local Eddington limit, the highest effective temperature for a blackbody contribution would be \(~140 \text{ eV}\) for a 1.4 \(M_\odot\) WD (Williams et al. 1987), which would imply a shock temperature \(kT_{\text{max}}\) of 230 keV. Even the 94 eV temperature, as derived from XMM-Newton data and consistent with Swift observations, demands a WD mass of at least 1.2 \(M_\odot\), with a high specific accretion rate of about 200 g cm\(^{-2}\) s\(^{-1}\) and \(kT_{\text{max}} > 100\) keV and therefore inconsistent with our spectral analysis.

Based on the Suzaku XIS1 spectrum, we have proposed an alternative spectral model that does not include a hot blackbody. For other instruments, but still acceptable for the Suzaku XIS0 and XIS3 spectra, this model results in a poorer fit than was obtained with the model with a blackbody. One plausible explanation is the limitation of the \(\text{pwab}\) model. While this model is the most sophisticated in terms of reproducing the
likely distribution of the number of lines of sight as a function of \( N_H \) (Done & Magdziarz 1998), it assumes that the absorber has the solar abundance and is not ionized. If the emitting plasma is overabundant in nitrogen, so, too, should the absorbing plasma, which is not currently taken into account. Moreover, the presence of the O VII edge means that the latter assumption is invalid. We currently model this using an edge model in addition to \( \Delta \nu_{ab} \), but we believe this is not the correct model for this situation. In reality, the absorption below 0.78 keV should be less than what \( \Delta \nu_{ab} \) predicts, because the complex absorber is ionized and mostly transparent at these energies. We therefore believe that the current inadequacies of the model is likely explanation for the imperfect fit. It is likely that high-resolution, high signal-to-noise X-ray spectroscopy combined with an improved grid of models would be needed to see if the alternative spectral description is correct. In the meantime, the abundance of N should be investigated using optical and UV spectroscopy. Nitrogen overabundance has been seen in a number of CVs, both magnetic and nonmagnetic (see, e.g., Gänsicke et al. 2003; Froning et al. 2012), and indicates the presence of CNO-processed matter in the system. This, in turn, can be either due to prior nuclear evolution of the donor (Schenker et al. 2002) or pollution by previous nova eruptions (Marks & Sama 1998).

For the main purposes of this work, the exercise we carried out by using three sets of X-ray observations for V2731 Oph shows that (i) while there is no significant evidence of change in the spectral distribution of the hottest thermal component, its luminosity is variable, and its X-ray photons suffer the effect of a variable absorbing column; (ii) the hottest thermal component is in agreement with a cooling-flow, stratified multithermal model, which is expected for IP systems; and (iii) the soft X-ray spectrum is variable in flux and spectral distribution. Given these findings, we believe our results are robust regarding the complex absorber, reflection amplitude, and maximum temperature of the post-shock region, despite our imperfect understanding of the soft (<1 keV) spectrum of V2731 Oph.

6.2. Clues from the Plasma Temperature and Reflection Amplitude

While the maximum temperature \( (kT_{\text{max}}) \) derived from the MKCFLOW model traces the gravitational potential well at the accretion column shock, the reflection amplitude \( (\Omega_{r}) \) depends on the shock height \( (h) \) with respect to the stellar surface. Thus, these two spectral signatures allow us to put constraints on the WD mass and the accretion geometry of the system.

For a pointlike emission region placed at height \( h \) above the WD, with \( h \) expressed as a fraction of the stellar radius, the stellar surface covers the solid angle (see Figure 2 of Tsujimoto et al. 2018):

\[
\Omega = 2\pi(1 - \sqrt{1 - 1/(1 + h)^2}).
\]

The reflection amplitude is defined as the solid angle covered by the reflector as seen from the emitter in such a way that it is 1.0 when the solid angle subtended is 2\( \pi \) (half the sky). This condition corresponds to \( h = 0 \) in Equation (1), and therefore \( \Omega_{r} \equiv \Omega]/2\pi \). Thus, a reflection amplitude of 0.88 ± 0.13 as derived from the spectral fit of TV Col (see Table 3) requires \( h \) of order 0.7% of the WD radius. Such a small shock height implies that \( kT_{\text{max}} \) traces the gravitational potential well virtually at the WD surface, and therefore the WD mass determined from our spectral fit \( (0.735 \pm 0.015 M_\odot) \) does not require additional corrections.

On the other hand, as first derived by Aizu (1973), the geometrical parameter \( h \) is physically determined by the post-shock cooling time \( (t_c) \) that defines the remaining time for the accreted material to settle onto the WD. Higher density \( (\rho) \) in the accretion column accelerates the cooling \( (t_c \propto 1/\rho) \), resulting in smaller \( h \). Thus, \( h \) is a function of WD mass and specific (or per unit area) accretion rate \( (g \text{ s}^{-1} \text{ cm}^{-2}) \).

Following Aizu (1973), the low \( h \) derived from the reflection in TV Col (<0.7%) is due to a high specific accretion rate, of order 15 g s\(^{-1} \) cm\(^{-2} \). Comparing the specific accretion rate with the mass accretion rate derived from the MKCFLOW model of \( (3.8 \pm 0.2) \times 10^{-10} M_\odot \text{ yr}^{-1} \), we estimate that the fractional area over which accretion happens \( (f) \) is about 0.02% for TV Col: a relatively high specific accretion rate and a small accretion spot. The best estimate for the spot size in IPs is that for XY Ari, for which Hellier (1997) used the X-ray eclipses to arrive at an estimate of <0.002. If reliable determination of reflection amplitude becomes routine, there is a potential to repeat the kind of analysis we have performed for TV Col to estimate the spot sizes of IPs. This might allow future researchers to perform a statistical study against other system parameters.

On the other hand, we did not detect an unambiguous sign of reflection in the NuSTAR observation of V2731 Oph. Thus, we are unable to derive the specific accretion rate or the shock height in V2731 Oph from its X-ray spectrum.

6.3. Additional Constraints from the Photometry

The X-ray spin modulation of IPs is usually due to complex absorption (Norton & Watson 1989), which is not expected to produce significant spin modulation above 10 keV. Therefore, when spin modulation is seen above 10 keV, a geometrical explanation is required. A likely scenario is that nonnegligible shock height \( (h > 0.1) \) results in both poles being visible over a range of viewing geometry (de Martino et al. 2001).

The lack of detectable spin modulation in the NuSTAR data on TV Col can be explained as follows. First, we do not expect geometrical spin modulation because the shock in TV Col is very close to the stellar surface \( (h \sim 0.7\%) \). Second, the maximum energy at which we can detect X-ray spin modulation due to complex absorption depends on \( N_{H_{\text{max}}} \). Our spectral fit shows \( N_{H_{\text{max}}} \) of only \( \sim 10^{25} \text{ cm}^{-2} \) during the NuSTAR observation, so the effects of complex absorption are mostly confined to photon energies below \( \sim 3 \text{ keV} \). The complex absorption appears to be variable from epoch to epoch according to our analysis of the Swift data, which also extends to lower energies. However, these Swift data do not have sufficient spin phase coverage, and our timing analysis was inconclusive. We expect that X-ray observations that showed spin modulations above 3 keV were obtained when TV Col was in a higher \( N_{H_{\text{max}}} \) state.

In V2731 Oph, \( N_{H_{\text{max}}} \) is high, so the low-energy (<10 keV) spin modulation may well have a contribution due to complex absorption. Nevertheless, the clear detection of the spin period above 10 keV (Figure 6) implies a strong geometrical component to the X-ray spin modulation in this IP. This indicates a nonnegligible shock height for V2731 Oph. We thus expect a low reflection amplitude, which can explain the absence of evidence of reflection in the X-ray spectrum of the...
system. In that sense, V2731 Oph appears similar to V709 Cas (Mukai et al. 2015). At first sight, it might seem surprising that a system as luminous as V2731 Oph should have a nonnegligible shock height \( h \). We suggest two factors that may explain the large \( h \). First, recall that \( h \) is determined not by the total accretion rate but by the specific accretion rate. We can explain the nonnegligible \( h \) by invoking a large \( f \). A major factor controlling \( f \) is the pinching by the dipole magnetic field \( (B \propto r^2) \), the degree of which is determined by the magneto-spheric radius. If we assume an approximate spin equilibrium, V2731 Oph \( (P_{\text{spin}} = 128 \text{ s}) \) must have a much smaller magnetosphere than TV Col \( (P_{\text{spin}} = 1909.07 \text{ s}) \), so dipole pinching is much less effective. Second, V2731 Oph may well have a massive WD. The freefall velocity is higher, which reduces the post-shock density, which reduces the X-ray cooling efficiency. Since the post-shock temperature is also high, this increases \( t_c \), and hence \( h \).

6.4. Our Targets and the Standard Evolutionary Scenario

The mass transfer in CVs with orbital periods less than \( \sim 10 \text{ hr} \) is driven by angular momentum loss and expected to be of order \( (3-5) \times 10^{-9} \text{ M}_\odot \text{ yr}^{-1} \) for a 5.5 hr period CV, as appropriate for TV Col (Knigge et al. 2011). Both the normalization of the MKCFLOW model and the bolometric X-ray luminosity of TV Col suggest a lower accretion rate, unless a large amount of transferred material is not accreted and is lost, perhaps propelled out of the system, therefore reducing the expected accretion rate and consequent X-ray emission. The observed X-ray luminosity is typical of IPs (Schwope 2018).

This standard evolutionary scenario does not apply to V2731 Oph, so we have no quantitative prediction for the mass transfer rate in this system. The BAT-band luminosity of V2731 Oph is already \( \log L_X(\text{erg s}^{-1}) = 34.6 \) (Schwope 2018), the highest of all IPs, and the uncertain evolutionary driver must be capable of sustaining a high mass transfer rate. The overabundance of \( N \), if confirmed, would place V2731 Oph among the subset of CVs known to be overabundant in \( N \) (see, e.g., Gansicke et al. 2003). This would imply that the donor matter has been CNO-processed: the secondary of V2731 Oph may be evolved in the normal (single-star evolution) sense, or it may indicate that this is a post-thermal timescale mass transfer system (Schenker et al. 2002).

6.5. WD Masses

We have shown that both a complex absorber and reflection are necessary to fit the wideband X-ray spectrum of TV Col. The combined NuSTAR+Swift data allowed us to constrain both, as well as the maximum temperature of the X-ray-emitting plasma. The high reflection amplitude supporting a small shock height \( h \) and the long spin period indicate that the inner radius of the truncated disk is large. Taking the maximum plasma temperature as a measure of the gravitational potential just above the WD surface, we determine the WD mass to be \( 0.735 \pm 0.015 \text{ M}_\odot \). Our value is somewhat smaller than but consistent with the previous NuSTAR measurement by Hailey et al. (2016).

On the other hand, we were unable to constrain the reflection amplitude in V2731 Oph. This has several effects on the mass measurement. First, our derived values for \( kT_{\text{max}} \) depend on whether we include reflection (with amplitude fixed to 1.0) or not. Also, our values, particularly in the case without reflection \( (0.92 \pm 0.04 \text{ M}_\odot) \), are significantly lower than what Hailey et al. (2016) derived; the reason for this is unclear. Moreover, we were unable to constrain the shock height, but the high-energy \( (>10 \text{ keV}) \) spin modulation suggests it is not small. Because of this, and because V2731 Oph is a fast rotator that probably requires correction for the small inner radius of the disk, we consider our numbers to be lower limits for the true WD mass in this system.

7. Summary

We have combined analyses of broadband X-ray spectroscopy and photometry, as in Mukai et al. (2015), to study two IPs, TV Col and V2731 Oph, already analyzed by Hailey et al. (2016). We have gained valuable insight into the geometry and physics of accretion in these systems.

1. TV Col:
   (a) Complex absorption, such as described by the pwab model, is required to obtain a good spectral fit.
   (b) Reflection is also clearly detected, with an amplitude of \( 0.88 \pm 0.13 \), indicating a small shock height caused by a high specific accretion rate.
   (c) We do not detect the spin modulation in the NuSTAR data, showing that the amplitude of the spin modulation can vary over different epochs, as is also seen at optical wavelengths.
   (d) The WD mass is determined to be \( 0.735 \pm 0.015 \text{ M}_\odot \).

2. V2731 Oph:
   (a) The X-ray spectrum is affected by a complex and variable local absorption, with a much higher \( N_H \) than for TV Col.
   (b) The spectral model, which includes a hot blackbody, used to fit the XMM-Newton data does not work for the Suzaku XIS1 data. We have tentatively proposed an alternative model without such a blackbody but with an overabundance of nitrogen.
   (c) The NuSTAR data did not allow us to constrain the reflection amplitude. The detection of high-energy \( (>10 \text{ keV}) \) spin modulation suggests a tall shock.
   (d) A combination of clues points to a high-mass WD in V2731 Oph.

We thank the anonymous referee for numerous helpful suggestions. R.L.O. was partially supported by the Brazilian agency CNPq (Universal grants 459553/2014-3, PQ 302037/2015-2, and PDE 200289/2017-9). This work has made use of data from the European Space Agency (ESA) mission Gaia (https://www.cosmos.esa.int/gaia), processed by the Gaia Data Processing and Analysis Consortium (DPAC; https://www.cosmos.esa.int/web/gaia/dpac/consortium). Funding for the DPAC has been provided by national institutions, in particular the institutions participating in the Gaia Multilateral Agreement. This research has made use of the NuSTAR Data Analysis Software (NuSTARDAS), jointly developed by the ASI Science Data Center (ASDC, Italy) and the California Institute of Technology (Caltech, USA). This research has made use of the XRT Data Analysis Software (XRTDAS) developed under the responsibility of the ASI Science Data Center (ASDC), Italy.

Facilities: NuSTAR, Swift, Suzaku, XMM-Newton.
ORCID iDs

R. Lopes de Oliveira @ https://orcid.org/0000-0002-6211-7226
K. Mukai @ https://orcid.org/0000-0002-8286-8094

References

Aizu, K. 1973, PTsPh, 49, 1184
Tsujimoto, M., Morihana, K., Hayashi, T., & Kitaguchi, T. 2018, PASJ, 70, 109