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# On the origin of the asymmetry of the ejecta structure and explosion of G350.1-0.3 

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#### Abstract

We present X-ray analysis of the ejecta of supernova remnant G350.1-0.3 observed with Chandra and Suzaku, and clarify the ejecta's kinematics over a decade and obtain a new observational clue to understanding the origin of the asymmetric explosion. Two images of Chandra X-ray Observatory taken in 2009 and 2018 are analyzed in several methods, and enable us to measure the velocities in the plane of the sky. A maximum velocity is $4640 \pm 290 \mathrm{~km} \mathrm{~s}^{-1}\left(0.218 \pm 0.014 \operatorname{arcsec}_{\mathrm{yr}} \mathrm{yr}^{-1}\right)$ in the eastern region in the remnant. These findings trigger us to scrutinize the Doppler effects in the spectra of the thermal emission, and the velocities in the line-of-sight direction are estimated to be a thousand km $\mathrm{s}^{-1}$. The results are confirmed by analyzing the spectra of Suzaku. Combining the proper motions and line-of-sight velocities, the ejecta's three-dimensional velocities are $\sim 3000-5000 \mathrm{~km} \mathrm{~s}^{-1}$. The center of the explosion is more stringently constrained by finding the optimal time to reproduce the observed spatial expansion. Our findings that the age of the SNR is estimated at most to be 655 years, and the CCO is observed as a point source object against the SNR strengthen the "hydrodynamical kick" hypothesis on the origin of the remnant.


Keywords: ISM: individual objects (SNR G350.1-0.3) - ISM: supernova remnants - proper motions — stars: individual(XMMU J172054.5-372652)

## 1. INTRODUCTION

The explosion mechanism leading to core-collapse supernovae (CC SNe) is a long-standing problem in modern astrophysics. Asymmetry has played an important role in driving the CC SNe, where the pattern of the ejecta distribution of supernova remnants (SNRs) is a unique tool to trace the history back to the explosion (e.g., Hughes et al. 2000; Lopez et al. 2009). In particular, recent observational studies indicate that understanding the relation between asymmetric ejecta distribution and a motion of the neutron star (NS), so-called "NS kick", is critical to reveal the mechanism of the

[^0]supernova (e.g., Holland-Ashford et al. 2017; Katsuda et al. 2018). However, there are very few SNRs that allow us to investigate the kinematics of both ejecta and NS directly, making it challenging to compare the observation with the theory on the supernova models.

G350.1-0.3 is known to be a galactic supernova remnant with a strikingly non-spherical shape of the X-ray image. XMMU J172054.5-372652 is suggested as a candidate of the "central compact object (CCO)" of the remnant, thus indicating that the ejecta structure is biased to the east from the putative center of the explosion (Gaensler et al. 2008; Lovchinsky et al. 2011). They argue that the remnant is very young ( $600-1200 \mathrm{yr}$ ) and has a transverse motion of the CCO with a relatively high speed of $1400-2600 \mathrm{~km} \mathrm{~s}^{-1}$ for an assumed center of the explosion. The estimated age and the CCO speed offer the possibility that the ejecta and the CCO
kinematics can be observationally constrained with the X-ray spectroscopy and imaging of the existing X-ray missions. Borkowski et al. (2020) discovered that there is a variation in the brightness distribution in X-rays in several regions of G350.1-0.3. They used the maximum likelihood method to measure sky-plane velocities, which were $5000 \mathrm{~km} \mathrm{~s}^{-1}$ for the ejecta and $320 \mathrm{~km} \mathrm{~s}^{-1}$ for the NS. They also estimated the line-of-sight velocity from spectral analysis to be $900-2600 \mathrm{~km} \mathrm{~s}^{-1}$ redshift. They conclude that the age of G350.1-0.3 is younger than 600 years from the fast expansion proper motion.
In this paper, we present the measurements of the ejecta velocities in the three-dimensional (3D) space and the proper motion of the CCO in G350.1-0.3 using Chandra (Weisskopf et al. 2000) observations in 2009 and 2018. The three independent measurements of proper motion, (1)the optical flow, revealing the overall movement in the SNR, (2)the projection analysis, making it visually more clear, (3)the maximum likelihood method to quantify the movement, performed in this study consistently suggest that the speeds of the ejecta are $2000-5000 \mathrm{~km} \mathrm{~s}^{-1}$. Furthermore, the finite radial motion is confirmed by the reanalysis of the Suzaku (Mitsuda et al. 2007) data. Our results support a "hydrodynamic kick" mechanism based on the firm evidence that NS is kicked to the opposite direction of the spread of the ejecta, suggesting that the remnant can be the unique sample to investigate the origin of the asymmetry in CC SNe. Throughout this paper, uncertainty intervals of $90 \%$ confidence level are quoted unless explicitly stated otherwise.

## 2. OBSERVATIONS

The Chandra X-ray Observatory has observed G350.1-0.3 in 2009 April (PI: P. Slane) and 2018 July (PI: S. Reynolds) using the Advanced CCD Imaging Spectrometer Spectroscopic-array (ACIS-S). The total exposure times of the two observations are 82.97 ks and 189.24 ks , respectively. More detailed information on individual IDs is shown in table 1. The data are reprocessed using chandra_repro in CIAO 4.11 with CALDB 4.8.2, provided by the Chandra X-Ray Center.

In order to improve the positional accuracy of the images, eight point sources are identified using wavdetect and the coordinate difference between the two epochs is evaluated by wcs_match.
Then the coordinates of the event files are updated with wcs_update to minimize the differences. The correction results in the average positional accuracy of $0.378^{\prime \prime}$. Using eight point sources, this value was cal-
culated as follows

$$
\begin{equation*}
\overline{\delta d}=\sqrt{\frac{\sum_{i=1}^{N} \delta d_{i}^{2}}{N}} \tag{1}
\end{equation*}
$$

where $\delta d$ is the distance between the coordinates in 2009 (updated by using wcs_update) and $2018, N$ is the number of point sources. It gives a reference to the systematic uncertainties on the positional accuracy.
The X-ray image of G350.1-0.3 taken in 2009 is shown in figure 1. There is little or no X-ray emission to the west, and XMMU J172054.5-372652 is observed (Lovchinsky et al. 2011). It contrasts to typical supernova remnants, such as a spherical morphology seen in Tycho's SNR. The X-ray intensity is higher in the eastern region than in the northern and southern one. XMMU J172054.5-372652 is located in the western region, which about $2^{\prime}$ away from the bright eastern region.
XMMU J172054.5-372652 is observed in 2013 May with ACIS Continuous Clocking (CC) Mode (PI: Gotthelf), listed in table 1 for more details. The CC Mode is different from the Very Faint (VF) Mode used in the other G350.1-0.3 Chandra observations in that it sacrifices spatial resolution in two dimensions, so this data cannot be used for image analysis. The data are used only for CCO spectrum analysis.
The Suzaku X-ray Observatory has observed G350.1-0.3 in 2011 September (Yasumi et al. 2014). The data from the front-illuminated CCDs (XIS0 and XIS3; Koyama et al. 2007) are used and reprocessed with the current calibration database (2016 February 14) using the standard screening criteria. The effective exposure time is 70.2 ks . The X-ray spectrum is extracted from a circle region with a $1.5^{\prime}$ radius that covers the bright eastern structure. The background spectrum is extracted from the dim spot in the same data, which is a typical way of estimating the background.

## 3. RESULTS

### 3.1. Sky-plane velocities from image analysis

To visually grasp the slight change in the image from 2009 to 2018, we adopted one of the dynamic image analyses called "optical flow". It calculates the flow's two-dimensional vector fields, which obey the conservation law of the total intensity in the image. A similar approach has been applied to Cassiopeia A (Sato et al. 2018). More specifically, a derived version of the optical flow called Gunnar Farnebäck method (Farnebäck 2003) is used to focus more on the small movement of patchy areas. The parameters and the setups are the same as used in Sato et al. (2018). When a flux in a pixel is

Table 1. Observational log of the Chandra and Suzaku data.

| Observatory | Target Name | Obs. ID | Obs. Start (yyyy mm dd) | Exposure <br> (ks) | Detector ${ }^{a}$ | $\begin{gathered} \mathrm{RA} \\ (\mathrm{deg}) \end{gathered}$ | $\begin{gathered} \text { Dec } \\ (\mathrm{deg}) \end{gathered}$ | Roll <br> (deg) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Chandra | G350.1-0.3 | 10102 | 2009 Apr 21 | 82.97 | ACIS-S (VF) | 260.2653 | -37.4388 | 57.9084 |
|  | G350.1-0.3 | 20312 | 2018 Jul 2 | 40.58 | ACIS-S (VF) | 260.2615 | -37.4476 | 296.1505 |
|  | G350.1-0.3 | 20313 | 2018 Jul 4 | 19.84 | ACIS-S (VF) | 260.2606 | -37.4470 | 296.1504 |
|  | G350.1-0.3 | 21118 | 2018 Jul 8 | 42.91 | ACIS-S (VF) | 260.2608 | -37.4471 | 296.1497 |
|  | G350.1-0.3 | 21119 | 2018 Jul 7 | 48.29 | ACIS-S (VF) | 260.2605 | -37.4468 | 296.1490 |
|  | G350.1-0.3 | 21120 | 2018 Jul 5 | 37.62 | ACIS-S (VF) | 260.2608 | -37.4472 | 296.1490 |
|  | XMMU <br> J172054.5-372652 | 14806 | 2013 May 11 | 89.33 | ACIS-S (CC) | 260.2255 | -37.4454 | 64.2424 |
| Suzaku | G350.1-0.3 | 506065010 | 2016 Feb 14 | 70.18 | XIS-0, XIS-3 | 260.2697 | -37.4549 | 266.4234 |

$a_{\text {The terms in parentheses indicate the mode of imaging. VF and CC represent the Very Faint Mode and Continuous Clocking }}$ Mode of ACIS, respectively.
less than $1 \times 10^{-7}$ counts $\mathrm{cm}^{-2} \mathrm{~s}^{-1}$, it is regarded as background, and the corresponding pixel is discarded in this calculation. The result of the optical flow is shown in figure 2a. The obtained vector fields are indicated by the length and the direction of the arrows. In this way, we succeeded in visualizing the change in the two images in the bright eastern region, and revealing at least two distinctive flows on a large scale: from west to east in the upper half and from west to south-east in the bottom half. Note that only vectors with an amplitude greater than $\sim 1 \operatorname{arcsec}\left(1152 \mathrm{~km} \mathrm{~s}^{-1}\right.$ at the distance of 4.5 kpc$)$ are shown in figure 2 a , where the counts are significantly higher than the typical level of the background.
We then proceed in visualizing a change on a much smaller spatial scale. The X-ray image of 2009 is subtracted from that of 2018 and shown in figure 2 b , which works to emphasize the difference between the two images. The positive part (white in the figure) means the X-ray intensity in 2018 is brighter than in 2009, and vise versa. In other words, the pairs of the black and white region indicate the movement of the image. Filamentary structures are extending from north to south in several places, indicating that the ejecta moved in an east-west direction, which is consistent with the results obtained by optical flow. Furthermore, it vividly illustrates a more pronounced but detailed internal structure of the movement in the remnant.
To further confirm the flow, one-dimensional (1D) radial profiles are created from the box regions shown in figure 2 b . The direction of the flow is defined as the positive values from east to south. The unit is the number of pixels ( 1 pixel $=0.492^{\prime \prime}$ ). The projection of the flux is performed by integrating along the direction perpendicular to the flow direction. As a result, the projected pro-
files of the fluxes are obtained from each image of 2009 and 2018. The projection profile from box4 is shown in figure 3 as an example. Each profile is fitted with a Gaussian function using the least-squares method. The centers of the Gaussian functions obtained refer to the distance of the move over the two observations, resulting in the velocity of the ejecta. By assuming that the distance to G350.1-0.3 is 4.5 kpc (Lovchinsky et al. 2011), the proper motion velocities in all the 6 box regions are calculated and summarized in table 2. The ejecta velocities are found to range from 3500 to $5000 \mathrm{~km} \mathrm{~s}^{-1}$.

To estimate the direction of the flow with statistical significance, we calculate the 2 D proper motions for the box regions in figure 1 by using the maximum likelihood method. The method is based on the previous work (Sato \& Hughes 2017; Sato et al. 2018; Millard et al. 2020). The image of 2018 is used as a template, while that of 2009 is floated to find a 2D vector to maximize the likelihood. Here the likelihood function is defined as,

$$
\begin{equation*}
L=\prod_{i, j} \frac{\lambda_{i, j}^{k_{i, j}} e^{-\lambda_{i, j}}}{k_{i, j}!}, \tag{2}
\end{equation*}
$$

where $(i, j), k_{i, j}$ and $\lambda_{i, j}$ are the integers to specify the location of the pixel, the photon counts in a pixel $(i, j)$ of 2018 , and the photon counts in a pixel $(i, j)$ of 2009 , respectively ${ }^{1}$. By searching the local extrema of the likelihood function by changing the pairs of $i$ and $j$, we obtain the significance map in the space of $i$ and $j$. It gives the range and the peak of the significance. As a

[^1]

Figure 1. Chandra ACIS-S flux image taken in 2009. The energy range is $0.5-7.0 \mathrm{keV}$. The five green boxes refer to the proper motion analysis regions using the maximum likelihood method. The cyan arrows indicate the relative magnitude of 2D velocities and directions of motion of the ejecta that we obtained. The white cross marker indicates the on-axis aimpoint for the observation in 2009.
result, the ejecta's best-fit transverse velocities are estimated to be $\sim 2000-4600 \mathrm{~km} \mathrm{~s}^{-1}$ as shown in table 2 , which is consistent with the result of the 1D projection. Furthermore, the best-fit 2D vectors are evaluated with their statistical significance.
We apply the same method to the CCO, and obtained its proper motion of $\sim 640 \mathrm{~km} \mathrm{~s}^{-1}$. Since the CCO is a point source, the systematic uncertainty on the pointspread function (PSF) is not negligible. As the roll angle is different between the 2009 and 2018 observations (see table 1), the non-axisymmetric pattern of the PSF needs to be taken into account. Therefore, we created the
simulation images by using a simulator called MARX ${ }^{2}$. The center of the point source in the observed image is assessed by using the maximum likelihood method with the simulation image. By subtracting the corrected coordinate of 2018 from that of 2009, the CCO's proper motion between two epochs is evaluated to be $\sim 640 \pm$ $290 \mathrm{~km} \mathrm{~s}^{-1}$.

### 3.2. Line-of-sight velocities from spectral analysis

[^2]

Figure 2. (a) The Chandra X-ray image in 2009 overlaid with the vector fields obtained by the optical flow method. (b) Differential Chandra image of G350.1-0.3 between 2009 and 2018 observation ( $2018-2009$ ). The six green boxes are the regions chosen for proper motion analysis using the projection method. Throughout this figure, the energy range used is 0.5-7.0 keV .

Table 2. Velocity measurements in the regions shown in figure 1, 2 b from Chandra and Suzaku data.

| region ${ }^{a}$ | angular velocity |  | line-of-sight velocity$\left(\mathrm{km} \mathrm{~s}^{-1}\right)$ | $\begin{gathered} \text { total } \\ \left(\mathrm{km} \mathrm{~s}^{-1}\right) \end{gathered}$ | $\begin{gathered} \chi^{2} / \text { d.o.f. } \\ z=0 \text { (fixed) } \end{gathered}$ | $\begin{gathered} \chi^{2} / \text { d.o.f. } \\ z=\text { free } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\left(\operatorname{arcsec} \mathrm{yr}^{-1}\right)$ | $\left(\mathrm{km} \mathrm{s}^{-1}\right)^{b}$ |  |  |  |  |
| East-1 | $0.218 \pm 0.014$ | $4640 \pm 290$ | $1280_{-20}^{+20}$ | $4820_{-280}^{+280}$ | 527/251 | 369/250 |
| East-2 | $0.149 \pm 0.014$ | $3180 \pm 290$ | $1100_{-190}^{+170}$ | $3360_{-280}^{+280}$ | 760/299 | 433/298 |
| North | $0.138 \pm 0.027$ | $2940 \pm 580$ | $660_{-110}^{+160}$ | $3010_{-570}^{+570}$ | 244/252 | 231/251 |
| South | $0.097 \pm 0.027$ | $2080 \pm 580$ | $2570_{-40}^{+140}$ | $3300_{-370}^{+380}$ | 615/219 | 255/218 |
| CCO | $0.030 \pm 0.014$ | $640 \pm 290$ | - | - | - | - |
| box1 | $0.174 \pm 0.028$ | $3720 \pm 600$ | $1160_{-230}^{+1400}$ | $3900_{-580}^{+710}$ | 168/131 | 134/130 |
| box2 | $0.192 \pm 0.008$ | $4100 \pm 170$ | $1310_{-30}^{+700}$ | $4310_{-160}^{+270}$ | 147/132 | 121/131 |
| box3 | $0.172 \pm 0.015$ | $3670 \pm 330$ | $1070_{-150}^{+220}$ | $3820_{-320}^{+320}$ | 130/114 | 115/113 |
| box4 | $0.167 \pm 0.009$ | $3650 \pm 200$ | $670_{-490}^{+250}$ | $3620_{-220}^{+200}$ | 167/144 | 156/143 |
| box5 | $0.181 \pm 0.014$ | $3860 \pm 290$ | $470_{-100}^{+330}$ | $3890_{-290}^{+290}$ | 136/116 | 126/115 |
| box6 | $0.227 \pm 0.018$ | $4850 \pm 390$ | $1540_{-1210}^{+300}$ | $5090_{-520}^{+380}$ | 148/123 | 127/122 |
| Suzaku East | - | - | $1460_{-10}^{+40}$ | - | 1096/776 | 599/775 |

All errors listed in the table represent statistical errors. The systematic errors are discussed in Section 2.
${ }^{a}$ East-1, East-2, North, South, CCO are indicated in figure 1, box1, 2, 3, 4, 5 and 6 are indicated in figure 2b.
${ }^{b}$ The distance to the G350.1-0.3 is assumed to be 4.5 kpc . The systematic error obtained from the point source correction described in Section 2 is $884 \mathrm{~km} \mathrm{~s}^{-1}$ by assuming 4.5 kpc as well.

We measure the line-of-sight velocities of the ejecta using the X-ray spectra's Doppler effect. We extracted the spectra from four regions (East-1, East-2, North, and South in figure 1) and six regions (box1-6 in fig-
ure 2 b ) using the CIAO specextract command. The energy band of $0.5-6.0 \mathrm{keV}$ was used in the analysis.

The spectra were fitted with two components in XSPEC (version 12.10.1): a non-equilibrium ionization


Figure 3. Projection profile created from box 4 shown in figure 2 b . The red and blue points refer to the data taken in 2009 and 2018, respectively. The red and blue curves represent the best-fit Gaussian functions.
plasma model (NEI), "vvpshock", and a photoelectric absorption model with the "angr" abundance (Anders \& Grevesse 1989). In the fitting procedure, the $k T_{e}, n_{e} t$, and normalization are treated as free parameters. Abundances of $\mathrm{Mg}, \mathrm{Al}, \mathrm{Si}, \mathrm{S}, \mathrm{Ar}$, and Ca are allowed to vary freely, while the other abundances of elements are frozen to the solar values. The typical value of the equivalent hydrogen column density of the neutral absorber along the line-of-sight, $N_{\mathrm{H}}$, is $3-4 \times 10^{22} \mathrm{~cm}^{-2}$. The spectra of the two epochs are combined in combine_spectra because the shape of each data is similar (see Appendix). Figure 4 shows the spectra of G350.1-0.3, the best-fit model, and its residuals for East-1 and East-2 in the energy range of $1.65-2.3 \mathrm{keV}$. Figure 4 a shows the fitting result of East-1 when the redshift $(z)$ parameter of the NEI model is frozen at zero, resulting in $\chi^{2} /$ d.o.f. of $527 / 251$. The residuals are still present nearby the emission lines, suggesting the shift of the energy scale. Therefore, we continue fitting with a floating redshift, and figure 4b shows the fitting results. The residuals significantly decreases ( $\chi^{2} /$ d.o.f. $=369 / 250$ ). By fitting all the spectra with the redshift freed, the best-fit values of the redshift are obtained and summarized in table 2. Si Ly $\alpha$ emission lines $(\sim 2 \mathrm{keV})$ are visible in the spectra in figure 4. They are the emission lines of which the centroid energy does not depend on the ionization state and are well fitted when $z$ parameters are set to free in this study. By measuring the center and intensity of the Si $\mathrm{K} \alpha+\mathrm{Ly} \alpha$ lines, we can determine the ion fraction, or ionization state. Now that they are well fitted as well, the ionization state can be determined independently of the doppler effect. The X-ray plasma in the east, the
north, and the south are redshifted at $1000-1300 \mathrm{~km}$ $\mathrm{s}^{-1}, \sim 660 \mathrm{~km} \mathrm{~s}^{-1}$, and above $2500 \mathrm{~km} \mathrm{~s}^{-1}$, respectively.

Since it is commonly challenging to calibrate the energy scale of CCD in orbit, it is prudent to confirm the result by using more than one mission. We thus analyzed the Suzaku data because it has a larger effective area and a higher signal-to-background ratio per $\operatorname{arcmin}^{2}$. The spectra are obtained from a circle with a radius of $1.5^{\prime}$ covering the bright eastern structure. As shown in figure 4 c and 4 d , the residuals become smaller when the redshift parameter is floated. The line-of-sight velocity is estimated to be $\sim 1500 \mathrm{~km} \mathrm{~s}^{-1}$. The result is consistent with those obtained with Chandra.

### 3.3. Spectral analysis of XMMU J172054.5-372652

The CCO spectrum is fitted phenomenologically with the absorbed blackbody radiation model in XSPEC. The energy band of $0.5-6.0 \mathrm{keV}$ is used in the analysis. The spectra of the 2009,2013 , and 2018 observations are individually fitted and then joint-fitted (but only untied for normalization for each epoch). The results of the best-fit parameters are shown in table 3 . The fit is acceptable even without adding extra complex components, and there are no significant changes in parameters between different epochs of observations. The blackbody temperature $k T_{e}$ was also consistent with Lovchinsky et al. (2011). We then fitted the data with a physically-motivated model. According to Potekhin et al. (2020), the CCO spectrum was fitted with absorbed nsx model (Ho \& Heinke 2009) reproducing the spectrum of the atmosphere from NS. In the analysis of Potekhin et al. (2020), the 2009 and 2013 observations targeting XMMU J172054.5-372652 (ID: 14806) are also used in the spectral analysis. For better statistics, we add observations from 2018, which are not included in the analysis of Potekhin et al. (2020). The spectrum of XMMU J172054.5-372652 superimposed on the absorbed nsx model is shown in figure 5. Note that there are no significant changes in surface temperature or flux between 2009 and 2018. It can be seen from table 3 that the amount of flux in 2013 with different ACIS modes is larger than that in other epochs. We estimated the amount of pileup in 2009 and 2018 using the tool PIMMS ${ }^{3}$, and found that it was $13 \%$ and $8 \%$, respectively. Thus, the pileup may be the reason why the flux in the 2013 observation appears to be the largest in the observations of three epochs.

## 4. DISCUSSION

${ }^{3}$ https://cxc.harvard.edu/toolkit/pimms.jsp


Figure 4. The Chandra and Suzaku spectra in $1.65-2.3 \mathrm{keV}$ of G350.1-0.3. (a) The best-fit spectra of Chandra and the NEI models (top), and the corresponding residuals (bottom). The colors of the data refer to East-1 (black) and East-2 (red). The models are plotted in a solid line. (b) The same as (a) except that $z$ is free. (c) and (d) are the same as (a) and (b) except that the data are taken from one region in the Suzaku data, and the red and black spectra represent the XIS-0 and XIS-3 data.

Table 3. Best-fit spectral parameters of XMMU J172054.5-372652.

| Model | Parameter | 2009 | 2018 | 2013 | joint fit |
| :---: | :---: | :---: | :---: | :---: | :---: |
| absorbed blackbody model |  |  |  |  |  |
| tbabs | $N_{\mathrm{H}}\left(10^{22} \mathrm{~cm}^{-2}\right)$ | $3.02_{-0.18}^{+0.19}$ | $3.122_{-0.14}^{+0.15}$ | $2.70_{-0.16}^{+0.17}$ | $3.00_{-0.09}^{+0.10}$ |
| bbody | $k T_{e}(\mathrm{keV})$ | $0.52_{-0.02}^{+0.02}$ | $0.511_{-0.01}^{+0.01}$ | $0.50_{-0.02}^{+0.02}$ | $0.51_{-0.01}^{+0.01}$ |
|  | flux ${ }^{a}\left(10^{-13} \mathrm{erg} \cdot \mathrm{cm}^{-2} \cdot \mathrm{~s}^{-1}\right)$ | $4.59_{-0.11}^{+0.15}$ | $4.64{ }_{-0.09}^{+0.08}$ | $5.96{ }_{-0.14}^{+0.15}$ | - |
|  | $\chi^{2} /$ d.o.f. | 120/110 | 173/178 | 225/202 | 574/494 |
| absorbed nsx model |  |  |  |  |  |
| tbabs | $N_{\mathrm{H}}\left(10^{22} \mathrm{~cm}^{-2}\right)$ | $3.711_{-0.23}^{+0.23}$ | $3.89_{-0.18}^{+0.17}$ | $3.41_{-0.20}^{+0.20}$ | $3.72_{-0.11}^{+0.12}$ |
| nsx | $\log T_{\text {eff }}(\mathrm{K})$ | $6.37_{-0.03}^{+0.03}$ | $6.34_{-0.02}^{+0.03}$ | $6.33_{-0.03}^{+0.03}$ | $6.34_{-0.02}^{+0.02}$ |
|  | flux ${ }^{a}\left(10^{-13} \mathrm{erg} \cdot \mathrm{cm}^{-2} \cdot \mathrm{~s}^{-1}\right)$ | $4.611_{-0.57}^{+0.09}$ | $4.64{ }_{-0.28}^{+0.09}$ | $5.99_{-0.52}^{+0.10}$ | - |
|  | $\chi^{2} /$ d.o.f. | 112/110 | 153/178 | 220/202 | 539/494 |

${ }^{a}$ Flux is calculated in the range of $1.0-6.0 \mathrm{keV}$.

We succeeded in measuring the velocities in the plane of the sky of G350.1-0.3 through the analysis of the two X-ray images owing to Chandra's high spatial resolution. By analyzing the flow using several different methods, the regions in north, east, and south are found to move in a different direction. Thus the velocities in the plane of the sky are regarded as the velocities of the ejecta's proper motion. Inspired by this result, we have attempted to release $z$ to be free, and obtained finite values of $z$ from both Chandra and Suzaku data. This has been overlooked in Yasumi et al. (2014), probably because there was no clear evidence on the proper motion. The velocities that we obtained are compiled in table 2. These results are generally consistent with the results of Borkowski et al. (2020), which shows the speed of the G350.1-0.3 ejecta. We reinforced it with different calculation methods for velocities in the plane of the
sky (e.g. optical flow) and Suzaku data for the line-ofsight direction. Furthermore, we could characterize the CCO by detailed spectral analysis with better statistics than Potekhin et al. (2020). We discuss a possible origin of the asymmetry of the ejecta structure and explosion of G350.1-0.3. We estimate the center of explosion in G350.1-0.3 for the first time and use this to argue for the NS kick scenario.

### 4.1. Explosion center

In this asymmetric object, the location of the center of the explosion is an extremely important aspect, especially in considering the relationship between the motion of CCO and the ejecta. Regarding the center of the explosion, previous studies such as (Lovchinsky et al. 2011; Gaensler et al. 2008) simply defined it as being in the middle of the bright region in X-rays or


Figure 5. The Chandra spectra in $0.5-6.0 \mathrm{keV}$ of XMMU J172054.5-372652. The best-fit spectra of Chandra and absorbed nsx model (top), and the corresponding residuals (bottom). The colors of the data refer to 2009 (red), 2013 (green), and 2018 (black). The fit parameters are shown in table 3.
at the lowest point of the radio contour. But especially for CC SNRs, these explosion centers are poorly defined due to their asymmetric tendencies. Extrapolating the proper motion measured by image analysis can determine the kinematic center (Fesen et al. 2006; Sato \& Hughes 2017).

We estimated the time since the explosion by assuming that the ejecta had a common origin and drawing lines back to the presumed center adopting the velocities we measured and allowing the time since explosion to be a free parameter. Specifically, we calculated the time at which the variance of each origin point with respect to the presumed center was minimized. We investigated the case where the case (i) used two regions in the east and case (ii) used all five regions for which the maximum likelihood was used. In the case (i), the center is at the position shown in figure 6 , left panel, 460 years ago. The location of the explosion appears to be precisely determined, but the motion of the CCO cannot be explained. In this case, XMMU J172054.5-372652 would not be associated with the SNR. In the case (ii), the center is located at the position shown in figure 6 right panel, 655 years ago. The error circle is larger, but it explains the movement of the CCO. However, the degree of deceleration should vary from region to region, so there is that indeterminacy in the estimate of the explo-
sion center (e.g., Sato et al. 2018). Our measurements assert that the center of the explosion lies closer to the CCO than previously thought.

### 4.2. Combined velocity field

Combining the proper motions and line-of-sight velocities measured for the same region, we can construct a total velocity vector for each since the two speeds are orthogonal. The four regions except for the CCO in figure 1 and the six small boxes in figure 2 b were used for this study. For the large regions shown in figure 1, velocity magnitudes of $\sim 5000 \mathrm{~km} \mathrm{~s}^{-1}$ were obtained for East-1 and $\sim 3000 \mathrm{~km} \mathrm{~s}^{-1}$ for East-2, North, and South. For the the entire six regions along the eastern ejecta shown in figure 2 b , velocities of more than $4000 \mathrm{~km} \mathrm{~s}^{-1}$ or close to $4000 \mathrm{~km} \mathrm{~s}^{-1}$ were obtained. In particular, the ejecta motion was found to reach velocities of $\sim 5000 \mathrm{~km}$ $\mathrm{s}^{-1}$ for box6, which is located at the lower end of the remnant.

We used the software to model the evolution of SNR (Leahy \& Williams 2017) to infer SNR properties from the 3D velocities obtained in this study. We assumed a red supergiant as a progenitor and used a range of possible parameters of stellar wind mass loss and wind speed from (Smith 2014). The power-law indexes of the ISM and ejecta density profiles were fixed at 2 and 10 (Matzner \& McKee 1999). The velocity of contact discontinuity was assumed to be 0.75 times the velocity of blast-wave shock and the radius of contact discontinuity was assumed to be 0.75 times the radius of blast-wave shock (Laming \& Hwang 2003). The measured velocity ( $\sim 4800 \mathrm{~km} \mathrm{~s}^{-1}$ for East-1) is assumed to be the contact discontinuity velocity, and the distance of 3.64 pc (by assuming 4.5 kpc ) from the explosion center to the edge of the bright ejecta is considered to be the contact discontinuity radius. The age of the SNR was assumed to be 655 years. We searched for SNR properties consistent with these conditions. Given the above assumptions, a model with ejecta energy of $E_{\text {ej }}=0.8-2 \times 10^{51} \mathrm{erg}$, ejecta mass of $M_{\mathrm{ej}}=4-15 M_{\odot}$ (Yasumi et al. 2014), and stellar wind mass loss of $10^{-6} M_{\odot} / \mathrm{yr}$ provides a reasonable interpretation for our measurements and the size observed by Chandra in X-ray only in the area of East-1. However, when it comes to the South and North regions, it is impossible to explain the velocity with these properties. This implies that the spherically symmetric model cannot explain this object.

### 4.3. Properties and Environment of XMMU J172054.5-372652

The geometric center of the X-ray SNR and the XMMU J172054.5-372652 are about 1.5 arcmin apart,


Figure 6. G350.1-0.3 image of $0.5-7.0 \mathrm{keV}$ and explosive center using two regions in the east by the case (i) (left pannel) and explosive center using five regions by the case (ii) (right pannel). Green and yellow cross makers indicate the origins of each region when rewinding (i) 460 and (ii) 655 years. The green crosses are used to calculate the explosion center and the yellow crosses are not used. Pink cross makers indicate explosive centers determined by the case (i) and case the (ii), respectively. The dashed green circle shows the systematic error circle calculated by aligning the point sources.
so it should be noted what is the relationship between the two parties. The typical values of the $N_{\mathrm{H}}$ for the ejecta and the $N_{\mathrm{H}}$ for the CCO are in agreement with values ranging from $3-4 \times 10^{22} \mathrm{~cm}^{-2}$, consistent with the ejecta and the CCO having a common distance.
We explore the age of XMMU J172054.5-372652 from the theoretical cooling curves of NS (Potekhin et al. 2020) and the surface temperature of the NS obtained by observations. The fit gives the effective temperature $\log T_{\text {eff }}=6.34_{-0.01}^{+0.02} \mathrm{~K}$. This result is reasonable given the cooling curve (Potekhin et al. 2020), with the age being around 655 years and a young NS. In other words, XMMU J172054.5-372652 is most likely a neutron star associated with G350.1-0.3.

### 4.4. NS kick

G350.1-0.3 shows a highly asymmetric ejecta distribution, however, its kinematics has been unclear. Based on our ejecta velocity measurements in 3D space, we found most of the shocked ejecta at the eastern region in G350.1-0.3 are expanding with high velocities of $>3500$ $\mathrm{km} \mathrm{s}^{-1}$, which is comparable to that in the youngest galactic core-collapse SNR Cassiopeia A (DeLaney et al. 2010), to the opposite direction from the NS position. As shown in figure 6, the estimated explosion centers in the two cases are both located to the east of the current NS position, so if the NS is receiving a kick, it should be receiving a kick to the west (opposite to the ejecta). The asymmetric ejecta/NS distribution and their kinematics
in this remnant allow us to examine how asymmetric effects work for exploding massive stars.
The ejecta expansion in the opposite direction to the NS kick supports a "hydrodynamic kick" mechanism. In theory, neutrino-driven convective mass flows (Burrows et al. 1995) and standing-accretion shock instability (SASI) sloshing motions (Blondin et al. 2003) could lead to large-scale asymmetries of the ejecta. The aspherical expanding ejecta gain radial momentum and its center of mass begins to shift away from the coordinate origin. Here the NS must receive the negative of the total momentum of the anisotropically expanding ejecta mass due to linear momentum conservation, which causes a NS kick in the opposite direction of the SN mass ejection. Recent hydrodynamic simulations of the neutrino-driven mechanism show such NS kicks up to more than $1000 \mathrm{~km} \mathrm{~s}^{-1}$ (e.g., Scheck et al. 2006; Wongwathanarat et al. 2010, 2013). While the NS kick could also originate from an anisotropic emission of neutrinos ("neutrino-driven kick": Fryer \& Kusenko 2006), however, the strongest mass ejection in the direction of the NS motion is predicted in this scenario, which is not suitable for G350.1-0.3.
The nucleosynthesis in G350.1-0.3 would be useful for understanding the asymmetric effects during the explosion. In the neutrino-driven mechanism, "high-entropy bubbles" in the process of forming large-scale asymmetries play an important role in the explosive nucleosynthesis (e.g., Wongwathanarat et al. 2017). In the highentropy nuclear burning region, the abundant $\alpha$ parti-
cles $\left({ }^{4} \mathrm{He}\right)$ are captured by heavy elements. Thus, the production of $\alpha$ elements (e.g., ${ }^{44} \mathrm{Ti}$ ) is enhanced in the high-entropy process. Thus, the strong asymmetry in the remnant implies a large production of ${ }^{44} \mathrm{Ti}$ as in Cassiopeia A (e.g., Grefenstette et al. 2014), and the age of the remnant would encourage us to investigate the ${ }^{44} \mathrm{Ti}$ emission ${ }^{4}$. On the other hand, the ${ }^{44} \mathrm{Ti}$ production depends not only on the entropy, but also on the electron fraction, $Y_{\mathrm{e}}$ (the average electron number per baryon) in the high-entropy region (e.g., Magkotsios et al. 2010; Wanajo et al. 2013). In particular, the amount of ${ }^{44} \mathrm{Ti}$ in proton-rich high-entropy ejecta predicted in several theoretical simulations (e.g., Wanajo et al. 2018) is much smaller than that in the neutronrich ejecta (Wongwathanarat et al. 2017). Therefore, the neutron-rich environment is needed to create the abundant ${ }^{44} \mathrm{Ti}$ in the remnant. The Suzaku observation of G350.1-0.3 shows extremely high abundances of Ni compared to $\mathrm{Fe}\left(Z_{\mathrm{Ni}} / Z_{\mathrm{Fe}} \approx 8\right.$ : Yasumi et al. 2014), which implies a suitable environment for the ${ }^{44} \mathrm{Ti}$ production. As discussed here, the mass ratio among the iron-group elements and titanium could be a tracer of the nuclear burning conditions around the birth place of the NS. Further investigations for the element compositions in the remnant will be helpful to understand the supernova engine for driving CC SNe.

The asymmetric ejecta distribution and NS kick in G350.1-0.3 has not received much attention until now (for example, the remnant is out of samples in HollandAshford et al. 2017; Katsuda et al. 2018). We here succeeded in revealing the detailed kinematics of both ejecta and CCO in the remnant, which supports that the asymmetry in the kinematics of the remnant could originate from the neutrino-driven explosion and the strong hydrodynamic kick associated with the mechanism. Based on our results, it is more certain that the remnant can be one of the best samples in the future studies for discussing the origin of asymmetry in CC SNe such as Cassiopeia A.

## 5. CONCLUSION

In this paper, we present the analysis of G350.1-0.3 and XMMU J172054.5-372652 of a bright source in X-
rays with image and spectral analysis using data from two X-ray astronomy satellites. There are three main points to consider.

- The velocities of the G350.1-0.3 ejecta are measured from three different image analyses in the plane of the sky due to the excellent spatial resolution of Chandra, and in the line-of-sight direction consistent with the observed data of the two satellites. The three-dimensional velocities are as fast as $\sim 3000-5000 \mathrm{~km} \mathrm{~s}^{-1}$, indicating that the G350.1-0.3 is a very young SNR.
- For XMMU J172054.5-372652, the agreement with the column density of the SNR and the comparison between the surface temperature and the cooling curve suggest that the CCO originated from the same explosion as G350.1-0.3.
- The explosion center, inferred from the current proper motion, is located east of the CCO, which supports the "hydrodynamic kick" mechanism depiction of the NS. However, measuring the kick of CCO by image analysis was difficult due to the large systematic error.

We took a closer look at the mysteries of the origin of this strange shaped SNR from the perspective of kinematics. More spanning monitoring observations are desired in the future to observe the NS kick and to study changes in the shape and velocity of the ejecta, which will lead to a better understanding of this explosion.

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## APPENDIX. VELOCITIES IN THE LINE-OF-SIGHT DIRECTION ESTIMATED FROM EACH OF THE OBSERVATIONS IN 2009 AND 2018.

Spectral analyses were performed separately for the 2009 observation and 2018 observations. The best-fit values of the redshift are obtained and summarized in table 4. The fitting model and parameter settings are the same as in Section 2.

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Table 4. Velocity measurements in the region shown in figure 1 for each of the observations in 2009 and 2018 and the merged ones.

| region $^{a} a$ | line-of-sight velocity $\left(\mathrm{km} \mathrm{s}^{-1}\right)$ |  |  |
| :---: | :---: | :---: | :---: |
|  | 2009 | 2018 | Two-epoch combined |
| East-1 | $690_{-160}^{+160}$ | $1560_{-20}^{+20}$ | $1280_{-20}^{+20}$ |
| East-2 | $920_{-10}^{+10}$ | $1280_{-10}^{+20}$ | $1100_{-190}^{+170}$ |
| North | $60_{-410}^{+300}$ | $660_{-130}^{+130}$ | $660_{-110}^{+160}$ |
| South | $2740_{-280}^{+10}$ | $2540_{-20}^{+40}$ | $2570_{-40}^{+140}$ |

${ }^{a}$ East-1, East-2, North and South are indicated in figure 1.

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[^1]:    ${ }^{1}$ To be precise, we multiplied the 2018 count map by the ratio of the exposures map between the two epochs to consider the difference in effective area between them.

[^2]:    ${ }^{2}$ https://space.mit.edu/cxc/marx/

