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# JENNER: Just-in-time Enrichment in Query Processing

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## ABSTRACT

Emerging domains, such as sensor-driven smart spaces and social media analytics, require incoming data to be *enriched* prior to its use. Enrichment often consists of machine learning (ML) functions that are too expensive/infeasible to execute at ingestion. We develop a strategy entitled Just-in-time ENrichmeNt in quERy Processing (JENNER) to support interactive analytics over data as soon as it arrives for such application context. JENNER exploits the inherent tradeoffs of cost and quality often displayed by the ML functions to progressively improve query answers during query execution. We describe how JENNER works for a large class of SPJ and aggregation queries that form the bulk of data analytics workload. Our experimental results on real datasets (IoT and Tweet) show that JENNER achieves progressive answers performing significantly better than the naive strategies of achieving progressive computation.

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The full version of paper, source code, and data have been made available at https://github.com/jennerrepo/jenner.

### **1 INTRODUCTION**

Today, organizations have access to potentially limitless information in the form of web data repositories, continuously generated sensory data, social media posts, captured audio/video data, click stream data from web portals, and so on [1]. Often, such data needs to be enriched before it can be analyzed. Functions used to enrich data (referred to as *enrichment functions* in the paper) could consist of (a combination of) custom-compiled code, declarative queries, and/or expensive machine learning techniques. Examples include mechanisms for sentiment analysis [54] over social media posts, named entity extraction [7] in text, and sensor interpretation such as face detection and face recognition [32, 43] from images, sensor data fusion [46], and data cleaning tasks such as missing value imputation in relational data [15].

Analytical applications that require raw data to be enriched prior to use can be built in several ways. One approach is to collect the data, periodically enrich it, and then load it into the database for analysis, as done in the traditional extract-transform-load (ETL) systems [56]. An alternate approach is to enrich the data as it arrives "on-the-fly" at insertion time. Systems (*e.g.*, Spark Streaming [62] often used for scalable ingestion) are capable of executing enrichment functions on newly arriving data prior to its storage in a DBMS and can be used to build such an approach.

Both approaches suffer from several limitations. The periodic approach could significantly increase latency between when data arrives to when it is enriched and available for analysis. It does not support interactive analytics on the data as it is inserted.<sup>1</sup> The alternate approach of enriching data at insertion time suffers from a different limitation - it is only feasible when enrichment functions are simple. If complex functions such as Multi-layer Perceptron and Random Forest (often used to interpret data) are used for enrichment, it may result in ingestion bottleneck. For instance, accurately locating a person using WiFi events based on their history of connections can take  $\approx 200$ ms/event [38, 39]. Clearly, with thousands of connection events with WiFi access points per second, it is infeasible to execute such functions at the ingestion time.

Both the insertion time and periodic enrichment approach waste resources as they indiscriminately enrich all data, irrespective of whether they are needed for future analysis. *E.g.*, in the previous example, the analyst may only be interested in executing ad-hoc queries that require fine-grained localization of a small number of individuals instead of continuous fine-grained location of all individuals. Finally, both approaches require that enrichment functions to be known in advance prior to data collection.

With the goal of supporting analytics on data as it arrives, recent work in ENRICHDB [2] has proposed a different approach that supports "just-in-time" data enrichment during query processing. Such a technique eliminates several limitations of the insertiontime and periodic techniques mentioned above. It prevents wastage of resources since only data accessed by queries during analysis is enriched. Furthermore, by eliminating enrichment at ingestion

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<sup>&</sup>lt;sup>1</sup>This is similar to the limitation of the traditional data warehouse applications wherein newly arrived data was not available for analysis until it was loaded into a warehouse which led to the emergence of HTAP systems [12] over the past decade.

(or limiting it to simple enrichment) the scheme does not create an ingestion bottleneck. Finally, the data is available for analysis as soon as it is inserted without incurring long latency between when data is inserted and is available for analysis.

While the query-time enrichment has several advantages, it nonetheless, increases latency of individual queries since enrichment of queried data need to be performed at the time of query execution. Interactive analytics can only be supported if the number of objects that require enrichment are small. To overcome such a limitation of query-time enrichment, we develop Just-in-time ENrichmeNt in quERy Processing (JENNER) that interactively refines query answers based on progressively enriching data. JENNER exploits the fact that often multiple functions can be used to enrich the data for the same task which display a cost-quality tradeoff.

Cost-quality tradeoffs are demonstrated by several ML functions, *e.g.*, a complex neural network classifier (with higher number of layers and/or higher number of neurons per layer) has better accuracy than a neural network with lower complexity.<sup>2</sup> Furthermore, simple classifiers such as Bayes classifier, logistic regression are less accurate than complex classifiers of Extra Tree, Random Forest, and Neural Network classifiers. Such tradeoff is also studied in LOCATER [38] where coarse level localization techniques were used which had a fraction of cost than the fine-grained techniques.

JENNER prioritizes/ranks which enrichment functions should be evaluated on which objects to improve the quality of the answer as quickly as possible for a query. JENNER divides the query execution time into several *epochs* and analyzes the evaluation progress at the beginning of each epoch to generate an enrichment plan. Such a plan includes tuples that have highest potential of improving the quality of the answer in that epoch.

The deferred/lazy enrichment in JENNER is motivated by prior work on lazy query time data cleaning such as [11, 26]. Such works developed techniques to combine entity resolution/database repair using denial constraints with query processing to minimize the amount of data that needs to be cleaned. Likewise, [8] developed an approach to dynamically link entities in top-k queries. Such approaches, however, do not support the progressiveness that JEN-NER does. Since data cleaning tasks, such as entity linking, can be viewed as enrichment, the approach developed in this paper can also benefit query time data cleaning by supporting progressiveness.

In summary, we propose JENNER, a progressive approach of answering queries on the data that needs to be enriched. JENNER orders enrichment in a way to optimize progressiveness of queries by using a probabilistic strategy of estimating the benefit of enrichment functions. Our experiments on real data and enrichment functions show the efficacy of JENNER. JENNER has been integrated into the ENRICHDB system [3] and forms the basis of its progressive query evaluation strategy.

#### 2 DATA MODEL TO SUPPORT ENRICHMENT

We consider an extended relational data model, wherein some of the attributes of a relation are *derived* (denoted as  $\mathcal{R}_i$ ) and require enrichment (by executing a set of enrichment functions). The remaining attributes are *fixed* (denoted as  $A_j$ ) and do not require enrichment. Table 1 shows a relation with fixed attributes (*e.g.*, id, user\_id, time, wifi\_ap) and a derived attribute of location that could be derived by multiple functions that vary in cost and quality.

The enrichment functions are categorized based on their input types: (*i*) *single-tuple-input* and (*ii*) *multi-tuple-input*, that take as input a set of fixed attribute values of a single tuple or multiple tuples, respectively. The output of both types of enrichment functions are for a single derived attribute of a tuple. A single-tuple-input enrichment function typically uses other attributes in the same tuple and a model to make the inference. The multi-tuple-input enrichment function takes the fixed attribute values of multiple tuples from the same relation or different relations based on a parameter to infer the derived attribute value of the tuple.

Enrichment functions can also be categorized by their output types: (*i*) *single-valued*, (*ii*) *multi-valued*, or (*iii*) *probabilistic*, that output as a prediction a single value, multiple values, or probability distribution over a set of possible values. Of the three, probabilistic outputs are most general as we can always interpret results of the other two as probability distributions. We, thus, assume that enrichment functions output probabilities in the rest of the paper. *E.g.*, the value of location in tuple  $t_1$  of wifi in Table 2 is [0.54, 0.35, 0.11] which corresponds to locations L1, L2, and L3. JENNER assumes that the enrichment functions are calibrated using mechanisms such as [49, 61] on a labeled validation dataset. After calibration, the enrichment functions output a real probability distribution.

The enrichment functions for a derived attribute  $\mathcal{A}_i$  are denoted by  $F^i = \{f_1^i, f_2^i, \dots, f_k^i\}$ . Each function  $f_j^i$  is associated with a *cost* (denoted by  $c_j^i$ ) which represents the average execution cost of the function on a single tuple. Since the output of an enrichment function is probabilistic, we associate a notion of uncertainty with the probabilistic outputs. An expensive enrichment function is expected to produce output with less amount of uncertainty.

Given a probabilistic attribute value, we measure uncertainty using the entropy metric [31]. For a tuple  $t_k$  and derived attribute  $\mathcal{A}_p$ , entropy is calculated as follows:

$$h(t_i, \mathcal{A}_j) = -\sum_i p_i \cdot \log(p_i) \tag{1}$$

where,  $p_i$  represents the probability of the derived attribute taking the *i*-th domain value for the tuple  $t_k$ . The entropy of  $t_1$  in Table 2 is  $[-0.54 \times \log_3(0.54) - 0.35 \times \log_3(0.35) - 0.11 \times \log_3(0.11)] = 0.86$ .

JENNER is based on the premise that enrichment functions (that are often based on ML models) can be ordered based on their average behavior and very often enrichment functions that are more accurate are more expensive. This behavior of classifiers was highlighted in the past, *e.g.*, [21] studied cost-accuracy tradeoff of classifiers for sentiment analysis in tweets. Other examples include work on deep neural networks that accelerated performance by reducing the floating point precision of intermediate outputs of the neural network [25, 53, 63] and reducing the network size by modifying the width of the layers or by skipping layers/modules [14, 57, 60]. Such techniques trade between complexity and cost, *e.g.*, [63] describes a "precision-adjustable" softmax computation to achieve different precision and cost requirements of ML tasks.

**State and Value of a Derived Attribute.** Enrichment state or state of a derived attribute  $\mathcal{A}_j$  in tuple  $t_i$  (denoted by  $state(t_i.\mathcal{A}_j)$ ) is the information about enrichment functions that have been executed on  $t_i$  to derive  $\mathcal{A}_j$  and their output. The state has two

<sup>&</sup>lt;sup>2</sup>This phenomena is true until the model overfits the training data [22].

Table 1: The wifi table where location is a derived attribute.

| id    | user_id | time  | wifi_ap | location |
|-------|---------|-------|---------|----------|
| $t_1$ | 24      | 09:14 | 56      | L1       |
| $t_2$ | 22      | 10:26 | 110     | NULL     |
| $t_3$ | 108     | 14:10 | 116     | L4       |

# Table 2: State output for derivedattributes.

| tid                   | location                     |
|-----------------------|------------------------------|
| $t_1$                 | L1:0.54, L2:0.35, L3: 0.11   |
| $t_2$                 | L1: 0.1, L2: 0.1,, L10: 0.1  |
| <i>t</i> <sub>3</sub> | L1:0.15, L2: 0.35,, L6: 0.05 |

Table 3: wifistate table (created for tuples in wifi table).

| tid   | BitMap  | LocationState Output                              |
|-------|---------|---|
| $t_1$ | [1,0,0] | [[0.54, 0.35, 0.11,], [], []]                     |
| $t_2$ | [1,0,1] | $[[0.2, 0.6,, 0.2], [], [0.86, 0.1, \dots 0.04]]$ |
| $t_3$ | [1,1,0] | [[0.1, 0.2,, 0.5, 0.2], [0.2, 0.5, 0,], []]       |

components: *bitmap*, that stores the list of enrichment functions already executed on  $t_i$ . $\mathcal{A}_j$ ; and *output*, that stores the output of executed enrichment functions on  $t_i$ . $\mathcal{A}_j$ . *E.g.*, considering three enrichment functions  $f_1$ ,  $f_2$ , and  $f_3$  for location, the state bitmap of  $t_2$ , *i.e.*, (101) signifies that only  $f_1$  and  $f_3$  have been executed on it (see Table 3).<sup>3</sup> Further, the output of the state  $\langle [0.2, 0.6, \ldots 0.2], [], [0.86, 0.1, \ldots, 0.04] \rangle$  is the output of  $f_1$  and  $f_3$ .

The individual function outputs are aggregated into a combined value denoted by  $\mathcal{A}_j$ . *Value* (*e.g., Location.Value*) using a **combiner function** (*e.g.,* weighted average and majority voting). Since this value depends upon the state of the derived attribute, we denote  $\mathcal{A}_j$ . *Value* by *Val*(*state*( $t_i$ . $\mathcal{A}_j$ )) and the probability of it taking a particular value  $a_j$  by *Val*(*state*( $t_i$ . $\mathcal{A}_j$ ))[ $a_j$ ]. *E.g.,* in Table 3, the value of location for  $t_1$ , is *Val*(*state*( $t_1$ .location)) = [L1: 0.54, L2: 0.35, L2: 0.11]. The probability of  $t_1$  taking the value of location as L1, *i.e., Val*(*state*( $t_1$ .location))[L1] is 0.54.

**State and Value of Tuples and Relations.** The notions of state and value of derived attributes are generalized to tuples, relations, and the database in a straightforward way. The state (value) of a tuple  $t_i$ , denoted by  $state(t_i)$  ( $Val(state(t_i))$ ) is the concatenation of the state (value) of all derived attributes of  $t_i$ . Likewise, the state (value) of relation  $R_i$  and database D is denoted by  $state(R_i)$  ( $Val(state(R_i))$ ) and state(D) (Val(state(D))), respectively.

**Next Best Function at a State.** Execution of an enrichment function on an attribute  $\mathcal{A}_j$  in a tuple  $t_i$  in state  $state(t_i.\mathcal{A}_j)$  reduces uncertainty in its value  $Val(state(t_i.\mathcal{A}_j))$ . This reduction in uncertainty depends upon  $state(t_i.\mathcal{A}_j)$  and is learnt using a validation data set provided by the user as a preprocessing step. The size of the validation dataset is small and can be chosen from the same training dataset on which the enrichment functions are trained. Given  $state(t_i.\mathcal{A}_j)$  we order the enrichment functions associated with  $\mathcal{A}_j$  in the order of their uncertainty reduction and choose the one that reduces the uncertainty the most as next-best function, denoted as  $NBF(t_i, \mathcal{A}_j)$ . Note that uncertainty reduction due to enrichment functions that have already been executed in the past is zero and hence they cannot be the next best function at a state.

**Example 2.1.** Suppose the value of the *location* attribute of a tuple  $t_1$  is: [L1: 0.54, L2: 0.35, L3: 0.11]. The entropy of  $t_1$  with respect to *location* is 0.86 (measured using Equation 1). Suppose after the enrichment of  $t_1$  and using the next best function and combining the output with the outputs of previously executed functions, the *location* value of  $t_1$  becomes [L1: 0.8, L2: 0.15, L3: 0.05]. Hence, the entropy of the tuple with respect to *location* reduces to 0.56.

Currently JENNER rank orders enrichment functions based on their capability to reduce uncertainty (on an average) of derived attributes. Prior work [16] showed that ranking of classifiers can be context dependent. In [16], authors developed a strategy to train multiple classifiers where each classifier was an expert on a part of the data and their outputs were combined using a stacking based method. Such techniques result in the ranking to be context dependent. They can be supported in JENNER by storing a map that orders functions based on the context instead of a single nextbest function. JENNER needs to store the condition on context (*e.g.*, timestamp between  $t_1$  and  $t_2$ ) as the key and next best function as the value. When  $NBF(t_i, \mathcal{A}_j)$  is called, JENNER will use the context of  $t_i$  to find next-best function. Implementing JENNER with context dependent enrichment function is an interesting future direction.

**Query Model.** JENNER supports single block *select-project-join-aggregation* queries with conditions on both fixed and derived attributes, an example of which is shown in Code Listing 1.

# SELECT wifi.location as p\_location, wifi.time as p\_time FROM wifi WHERE p\_location = 'L1' AND p\_time BETWEEN ('10:00','12:00')

#### Code Listing 1: Example Query.

In the following, we focus on the queries with at least one derived attribute in the SELECT or WHERE clause. *E.g.*, the above query contains a condition on the derived attribute location.

Since derived attributes have probabilistic values, JENNER interprets queries based on *determinization-based* semantics [37, 45, 59], wherein Q is evaluated over determinized values for derived attributes in tuples that are part of O. The determinized value of a derived attribute  $\mathcal{R}_i$  is determined by executing a determinization function DET(.) on the associated value of the derived attribute (*i.e.*,  $DET(Val(state(t_i, \mathcal{A}_i)))$ ). Several methods to determinize a probabilistic attribute have been previously studied [37, 45, 59]. We choose the determinization function that returns the highest probable value after combining the output of the previously executed enrichment functions on the tuple. If the highest probable value is not unique then JENNER assigns the attribute value as NULL. For multi-valued determinization functions such as determinization based on a threshold, if all the possible attribute values have the probability lower than the threshold for a particular tuple, then the derived attribute is assigned a NULL value for that tuple.<sup>4</sup>

**Progressive Query Execution in Epochs.** The query execution time is discretized into multiple *epochs* (denoted by  $e_1, e_2, \ldots, e_z$ ) in which data enrichment is performed. We denote the time span of an epoch  $e_w$  by the notation  $|e_w|$ .<sup>5</sup>

<sup>4</sup>The techniques developed in the paper can be adopted to other determinization functions studied in [37, 45, 59] including those that return multiple values as discussed in the extended version of the paper [4].

Determinization concept naturally extends to a tuple and a relation. Determinized representation of a relation R is denoted as DET(R):

 $DET(R) = DET(Val(state(t_i.\mathcal{A}_j))) \mid \forall t_i \in R, \forall \mathcal{A}_j \text{ of } R.$ Thus, the execution of query Q is:

 $Q(R_1, R_2, ..., R_n) = Q(DET(R_1), DET(R_2), ..., DET(R_n))$ where  $DET(R_i)$  is the determinized representation of  $R_i$ .

<sup>5</sup>For simplicity, we will consider the duration of each epoch to be of fixed size in the remainder of the paper, though, the approach does not require this to be the case.

<sup>&</sup>lt;sup>3</sup>The bitmap does not represent any order between enrichment functions. It is possible to execute only the second enrichment function without executing the first one.

During an epoch  $e_w$ , certain enrichment functions (not executed before) are chosen to be executed. Let  $EP_w = \{\langle t_i, \mathcal{A}_j, f_k^j \rangle\}$  be a set of (tuple, derived attribute, enrichment function) triples, referred to as the *enrichment plan* of epoch  $e_w$ . Let S be the state of the database at the end of  $e_{w-1}$  and, let S' be the state after the execution of the enrichment plan  $EP_w$  in  $e_w$ . This results in state update of all tuples  $t_i \in EP_w$  as follows:  $\forall \langle t_i, \mathcal{A}_j, f_k^J \rangle \in EP_w$ , the  $state(t_i, \mathcal{A}_j)$ . bitmap is updated by setting the k-th bit to 1 to denote that k-th function is executed. Similarly,  $state(t_i.\mathcal{A}_j).output$ is updated as:  $state(t_i.\mathcal{A}_i).output = (t_i.\mathcal{A}_i).output \oplus \langle t_i, \mathcal{A}_i, f_i^J \rangle$ , where  $\oplus$  signifies that the *k*-th array of state output is updated and the new derived attribute value of the tuple is updated. At the end of  $e_w$ , user receives a query result, denoted as  $Ans_w$ , based on the current state of the database. Note that a tuple that was part of the answer in previous epoch, may no longer be part of  $Ans_w$ . In the rest of the paper, to disambiguate between different states/values of data in different epochs, we will denote the original database D on which O executes as  $D_0$  to signify its status prior to the query execution. We will refer to the database after the execution of  $e_w$ as  $D_w$  that corresponds to the database after all the enrichment functions until epoch  $e_w$  have been executed.

The user can access the query results at the end of each epoch. JENNER provides an expected quality of the returned results based on the enrichment performed until that time. This quality can be used by the user to determine if the query execution needs to be continued. The progressive query execution is motivated by online AQP systems where users can view the query results as soon as they are computed on the samples [17, 30]. The usefulness of online AQP systems were discussed in [24, 44]. An alternative is to use the query model of offline AQP systems [6, 48] where a maximum duration/quality requirement is specified by the user. The system continues the query execution till that time. JENNER supports the model of offline AQP by appropriately setting the epoch sizes.

Since in a progressive approach, users may stop query evaluation at any instance of time, performing enrichments that impact the answer quality as early as possible is desirable.

**Definition 2.1. Progressive Score.** The effectiveness of JENNER is measured using the following progressive score (similar to other progressive approaches used in [9, 47]):

$$\mathcal{PS}(Ans(q, E)) = \sum_{i=1}^{|E|} W(e_i) \cdot [Qty(Ans(Q, e_i)) - Qty(Ans(Q, e_{i-1}))]$$
(2)

where  $E = \{e_1, e_2, ..., e_k\}$  is a set of epochs,  $W(e_i) \in [0, 1]$  is the weight allotted to the epoch  $e_i$ ,  $W(e_{i-1}) > W(e_i)$ , Qty is the quality of answers, and  $[Qty(Ans(Q, e_i)) - Qty(Ans(Q, e_{i-1}))]$ is the improvement in the quality of answers occurred in epoch  $e_i$ . Assigning higher weights to the earlier epochs provide higher importance to the improvement in quality in the earlier epochs.

Since weights  $W_i$  in the progressive score defined above are decreasing, optimizing the progressive score is equivalent to selecting a set of enrichment functions (that have previously not executed) which can result in maximum increase in quality in the following epoch, that is,  $Maximize(Qty(Ans(Q, e_i)) - Qty(Ans(Q, e_{i-1})))$ .

The quality *Qty* in Equation 2, for a set-based query answer corresponds to a set-based quality metrics such as precision, recall,

 $F_{\alpha}$ -measure [50], or Jaccard similarity coefficient [34]. We define the  $F_{\alpha}$  measure and Jaccard's similarity below.

$$F_{\alpha}(Ans_{w}) = \frac{(1+\alpha) \cdot Pre(Ans_{w}) \cdot Rec(Ans_{w})}{(\alpha \cdot Pre(Ans_{w}) + Rec(Ans_{w}))}$$
$$\mathcal{J}(Ans_{w}) = \frac{|Ans_{w} \cap Ans^{real}|}{|Ans_{w} \cup Ans^{real}|} = \left[\frac{1}{Pre(Ans_{w})} + \frac{1}{Rec(Ans_{w})} - 1\right]$$
(3)

where  $Ans^{real}$  is the real answer of the query in ground truth set G, Pre is precision, *i.e.*,  $Pre(Ans_w) = |Ans_w \cap Ans^{real}|/|Ans_w|$ , and Recis recall, *i.e.*,  $Rec(Ans_w) = |Ans_w \cap Ans^{real}|/|Ans^{real}|$ , and  $\alpha \in [0, 1]$ is the weight of precision in  $F_{\alpha}$ -measure. In the rest of the paper, for computing the quality of set-based query result, we restrict to  $F_{\alpha}$ measure. The quality of an aggregation query could be measured using root-mean-square error [33] or mean-absolute-error [58].

**Quality Guarantees in JENNER.** At each epoch JENNER strives to choose the best set of objects to enrich that can improve the quality of the query result most. Since the ground truth of objects are not known, JENNER can neither directly measure the quality of query results returned so far, nor can it precisely determine the improvement in quality by executing an enrichment function. Instead, JENNER estimates both the quality of results (of previous epoch) and the improvement in quality if a selected set of objects are enriched in the current epoch. Based on these estimates, JENNER chooses and executes the enrichments that maximizes the improvement in quality of the resulting query answer from previous epoch.

Below we discuss how JENNER estimates the quality for setbased queries. For aggregation queries, JENNER optimizes the enrichment process using a set-based metric (*e.g.*,  $F_{\alpha}$ -measure) and then applies the aggregation function on the resulting tuples.

**Definition 2.2. Estimated Quality.** Let  $Ans_w^{MAX}$  be the set of tuples that have non-zero probability to be in the answer to query Q,  $Ans_w$  be a set of tuples returned as an answer to the user. Let  $\mathcal{P}_i$  be the probability of a tuple  $t_i \in Ans^{real}$  (we discuss ways to compute  $\mathcal{P}_i$  later). Furthermore, let m be the cardinality of  $Ans_w$ , and n be the cardinality of  $Ans_w^{MAX}$ . We compute the estimated precision and recall of  $Ans_w$ , denoted by  $\widehat{Pre}$  and  $\widehat{Rec}$ , as follows:

$$\widehat{Pre} = \frac{\sum\limits_{t_i \in Ans_w} \mathcal{P}_i}{m}, \quad \widehat{Rec} = \frac{\sum\limits_{t_i \in Ans_w} \mathcal{P}_i}{\sum\limits_{t_j \in Ans_w} \mathcal{P}_j}$$
(4)

Given the above estimates of precision and recall, we can next define estimate of  $F_{\alpha}$  measure denoted as  $\hat{F}_{\alpha}$ .

$$\widehat{F}_{\alpha}(Ans_{w}) = \frac{(1+\alpha)\sum\limits_{t_{i}\in Ans_{w}}\mathcal{P}_{i}}{\alpha\sum\limits_{t_{i}\in Ans_{w}^{MAX}}\mathcal{P}_{j} + m}$$
(5)

The above definition of estimated quality depends upon determining the probability  $\mathcal{P}_i$  of an answer tuple  $t_i$  to be in the real answer of the query. For a selection query with a single condition  $(t_i.\mathcal{A}_j = a_j)$  on a derived attribute  $\mathcal{A}_j$ , the  $\mathcal{P}_i$  of  $t_i$  is simply  $Val(state(t_i.\mathcal{A}_j))[a_j]$  if the determinized value of  $t_i.\mathcal{A}_j$  corresponds to  $a_j$ , else it is zero. For queries with selection conditions on multiple derived attributes, the probability of  $t_i$  satisfying the predicate is computed under the independence assumption of derived attributes by combining the probabilities of  $t_i$  satisfying the predicates on single attributes. For a join query,  $\mathcal{P}_i$  of a tuple  $t_i$  in a base relation is calculated as follows: (i) for each answer tuple that was generated from  $t_i$ , the probability of the answer tuple satisfying all the conditions on derived attributes are combined according to the independence assumption and (ii) the probability of all the answer tuples generated from  $t_i$  are added to generate  $\mathcal{P}_i$  as done in [55]. JENNER uses expected quality metric to choose which tuples should be enriched in an epoch as will be clear in §3. Note that it is possible that after enriching a tuple  $t_i$ , the probability  $\mathcal{P}_i$  of the tuple to satisfy the query decreases from the previous epoch, but it is expected that the overall quality of the query result improves. Furthermore, if multiple enrichment functions with cost quality tradeoff can not be defined (e.g., enrichment can only be performed by a unique function), JENNER may not achieve progressive improvement of query results. Even in such a case, as JENNER only enriches objects relevant to the query, it is beneficial than complete enrichment of objects before answering queries.

**Progressive Enrichment Problem.** Given the notations above, we can now formally state the problem of progressive enrichment. Let Q be a query and let  $e_1, e_2, \ldots, e_n$  be the epochs used to execute Q. Let state(D) be the state of the database after epoch  $e_{w-1}$ , where  $w \le n-1$ . Let  $CS_w$  be the set of tuples in D that are not fully enriched. The progressive enrichment problem consists of determining a set of  $\langle tuple, derived attribute, enrichment function \rangle$  triples  $EP_w$  such that, when executed in  $e_w$ , results in a database value of:  $(Val(state(D)) \oplus EP_w)$  that optimizes the following objective:

 $\max_{\langle t_i, \mathcal{A}_j, f_k^j \rangle} \left[ \widehat{\mathcal{Q}ty}(\mathcal{Q}(\mathit{DET}(\mathit{Val}(\mathit{state}(D)) \oplus \mathit{EP}_w))) - \widehat{\mathcal{Q}ty}(\mathcal{Q}(\mathit{Val}(\mathit{state}(D)))) \right]$ 

subject to

$$\sum_{\substack{\langle t_i, \mathcal{A}_j, f_k^j \rangle \in EP_w}} cost(\langle t_i, \mathcal{A}_j, f_k^j \rangle) \leq |e_w|$$

where  $\widehat{Qty}(Q(Val(state(D)) \oplus EP_w))$  is the expected quality of the query result when it is executed on the updated state of the database in epoch  $e_w$  and  $\widehat{Qty}(Q(Val(state(D))))$  is the expected quality of the query result at the end of previous epoch of  $e_{w-1}$ .

#### **3 PROGRESSIVE ENRICHMENT IN JENNER**

The overall algorithm of JENNER is presented in Algorithm 1. The zero-th epoch performs pre-processing in order for the answers to be generated in the later epochs. The later epochs of  $e_w$ , w > 0, iteratively enriches the tuples and compute the query results.

**Zero-th Epoch (Lines 5 - 10):** The goal of the zero-th epoch is to seed JENNER with the tuples that may need to be enriched in the upcoming epochs (*i.e.*, epoch 1 and onwards). It also sets up the data structures used in the later epochs. JENNER does not require any enrichment function to be executed on the data before. In zero-th epoch, JENNER identifies for each relation  $R_i$  a *minimal set* of candidate tuples whose enrichment in subsequent epochs may influence the query result (denoted as *CandidateSet*( $R_i$ )). Such a *CandidateSet*( $R_i$ ) is identified by executing *probe queries* (Line 4). Generation of probe queries are discussed in §3.1.

Next, for each  $t_i$  in the *CandidateSet* for each relation, for each derived attribute  $\mathcal{A}_j$  in  $t_i$  that is part of Q, JENNER estimates the probability of  $t_i$  matching the condition on  $\mathcal{A}_j$  (listed in the code as *match\_prob*). For each such attribute  $\mathcal{A}_j$  in  $t_i$ , JENNER also

| Al  | gorithm 1: Overall Algorithm.   |
|-----|---|
| Iı  | <b>nputs:</b> Query $Q$ and the duration of each epoch <i>epoch_duration</i> .            |
| 0   | outputs: An enrichment plan for each epoch.   |
| 1 F | unction Optimize_Enrichment() begin   |
| 2   | $CandidateSet^M \leftarrow \emptyset$   |
| 3   | <b>Epoch 0:: for</b> each $R_i \in Q$ do  |
| 4   | $CandidateSet(R_i) \leftarrow Execute(GenerateProbeQ(Q, R_i))$                            |
| 5   | <b>for</b> each $R_i.\mathcal{A}_k \in Q$ <b>do</b>                                       |
| 6   | <b>for</b> each $t_j \in CandidateSet(R_i)$ <b>do</b>                                     |
| 7   | $M \leftarrow CompProb(t_j, \mathcal{A}_k); C \leftarrow Cost(NBF(t_j, \mathcal{A}_k))$   |
| 8   | $B \leftarrow ComputeBenefit(NBF(t_j, \mathcal{A}_k))$                                    |
| 9   | CandidateSet <sup>M</sup> $\cup \langle t_j, \mathcal{A}_k, NBF, B, C, M \rangle$         |
| 10  | $CandidateSet^M \leftarrow Sort_{match_prob}(CandidateSet^M)$                             |
| 11  | <b>Epoch</b> $w, w \ge 1$ :: for each epoch $e_w$ do                                      |
| 12  | $EP_{w} \leftarrow ChooseEnrichmentPlan(CandidateSet^{M})$                                |
| 13  | <b>for</b> each entry $\in EP_w$ <b>do</b>  |
| 14  | ExecuteEnrichment( $t$ , $\mathcal{A}$ , $f$ ); UpdateState( $t$ , $\mathcal{A}$ , $f$ ); |
| 15  | $Determinize(t, \mathcal{A}); UpdateBenefit(CandidateSet^{M}, t, \mathcal{A});$           |
| 16  | $Ans_w \leftarrow ProduceQueryResult(Q)$  |
| 17  | Return Ans  |

computes the *benefit* and *cost* of executing the next best function (*NBF*) associated with  $t_i \mathcal{A}_i$  based on its current state (Line 7- 8).

The *match\_probability* of a derived attribute  $t_i.\mathcal{A}_j$  is determined using the probability  $Val(state(t_i.\mathcal{A}_j))[a_j]$  where the selection condition is  $\mathcal{A}_j = a_j$ . For derived attributes, that do not appear in any selection condition, the value of *match\_probability* is 1.

The benefit of enrichment of tuple  $t_i$  using the next best function (as shown in Line 8) for attribute  $\mathcal{A}_j$  is computed by estimating the improvement in quality from the previous epoch. We describe this step in details in §3.2. The benefit, cost, and matching probability for each candidate in *CandidateSet*( $R_i$ ) is stored in the corresponding *CandidateSet*<sup>M</sup> to represent the metadata of candidates (Lines 7-9). Candidates in *CandidateSet*<sup>M</sup> are sorted based on their *match\_prob* values (Line 10).

Later epochs  $e_w, w \ge 1$ , (Lines 11 - 16): The later epochs (*i.e.*,  $e_1, e_2, \ldots, e_n$ ) consist of a sequence of the following three steps: (*i*) Choose Enrichment Plan: that selects a set of candidate tuples from CandidateSet<sup>M</sup> to generate an enrichment plan  $EP_w$  for the epoch  $e_w$  (Line 12); We discuss choosing the enrichment plan in details in §3.2 and in §3.3; (*ii*) Execute Enrichment Plan: that enriches the tuples in  $EP_w$ , update their state, determinized representations and their benefit in CandidateSet<sup>M</sup> (Lines 14 - 15); We discuss them in §3.4; (*iii*) Produce Query Results: produce a query result by executing the query on determinized representation of the tuples and then choosing a subset of tuples that maximizes the quality of the result measured using  $E(F_\alpha)$  measure (Line 16); We discuss this step in §3.5. Progressive approach for aggregation queries is realized by developing a progressive approach for the corresponding set-based query on which the aggregation is performed.

#### 3.1 Probe Query Generation

In order to populate  $CandidateSet(R_i)$  for relation  $R_i$ , *i.e.*, to find out the set of tuples that may have impact on the query results, one could add all the tuples that are not fully enriched to this set. However, it would result in a significant number of redundant enrichments, *i.e.*, the tuples that do not satisfy predicates on the

(6)

SELECT \* FROM  $R_1$ ,  $R_2$  WHERE  $R_1$ . $\mathcal{A}_1 = a_1$  AND  $R_1$ . $A_2 = a_2$  AND  $R_1$ . $\mathcal{A}_3 = R_2$ . $\mathcal{A}_3$  AND  $R_1$ . $A_4 = R_2$ . $A_4$  AND  $R_2$ . $A_5 = a_5$  AND  $R_2$ . $\mathcal{A}_6 = a_6$ (a) Original query. SELECT \* FROM  $R_1$  WHERE  $R_1$ . $A_2 = a_2$ (b) Step 1 of probe query generation for relation  $R_1$ . SELECT \* FROM  $R_1$  WHERE  $R_1$ . $A_2 = a_2$ AND  $R_1$ . $A_4$  IN (SELECT  $A_4$  FROM  $R_2$  WHERE  $R_2$ . $A_5 = a_5$ ) (c) Step 2 of probe query generation for  $R_1$ . SELECT \* FROM  $R_1$ ,  $R_1$ State WHERE  $R_1$ . $A_2 = a_2$ AND  $R_1$ . $A_4$  IN (SELECT  $A_4$  FROM  $R_2$  WHERE  $R_1$ . $A_2 = a_2$ AND  $R_1$ . $A_4$  IN (SELECT  $A_4$  FROM  $R_2$  WHERE  $R_1$ . $A_2 = a_2$ AND  $R_1$ . $A_4$  IN (SELECT  $A_4$  FROM  $R_2$  WHERE  $R_2$ . $A_5 = a_5$ ) AND  $R_1$ . $id = R_1$ State.idAND  $(R_1$ State.array\_sum( $\mathcal{A}_1$ StateBitmap)! =

 $R_1State.array\_length(\mathcal{A}_1StateBitmap))$ 

(d) Step 3 of probe query generation for  $R_1$ .

#### Figure 1: Steps of probe query generation for $R_1$ in Q.

fixed attributes will be added to this set for enrichment. To avoid this, JENNER exploits the predicates over fixed attributes to filter out tuples whose enrichment has no consequence on the results. The probe queries identify a "minimal" subset of tuples (as small a subset as possible) for each  $R_i \in Q$  that need to be enriched to execute Q (denoted as  $pq(R_i)$ ).

We illustrate how probe queries are generated using the query in Figure 1a. The selection conditions on fixed attributes of  $R_1$  are identified, *i.e.*,  $R_1.A_2 = a_2$ . The tuples of  $R_1$  that require enrichment are restricted using this condition as shown in Figure 1b. JENNER further exploits join conditions on fixed attributes. *E.g.*, in Figure 1a, an  $R_1$  tuple must join with at-least one of  $R_2$  tuples that satisfy the condition of  $R_2.A_5 = a_5$ . A tuple of  $R_1$  can be part of the answer if it joins some tuples of  $R_2$  which satisfy the join condition  $R_1.A_4 =$  $R_2.A_4$ . JENNER determines such a set by computing semi-join with other relations in the query with which  $R_1$  joins using conditions on fixed attributes. Utilizing the semi-join optimization results in a nested query as shown in Figure 1c. We restrict the description of probe query using an example as the algorithm is an adaptation of semi-join optimization in [13]. The algorithm is available in [4].

Further, JENNER exploits the current state of the tuples to avoid repeated enrichment of tuples that are completely enriched. JENNER rewrites the selection condition as in Figure 1d on derived attribute, *i.e.*,  $R_1.\mathcal{A}_1 = a_1$  by the condition:  $[R_1.id = R_1State.id \text{ AND } R_1.array\_sum(\mathcal{A}_1StateBitmap)! =$  $R_1.array\_length(\mathcal{A}_1StateBitmap)]$ . This checks if a derived attribute is completely enriched using *StateBitmap* column of state table (*i.e.*, all the bits set to 1). Such tuples are not enriched.

#### 3.2 Benefit Estimation

JENNER chooses the  $\langle \text{tuple}, \text{derived attribute}, \text{enrichment function} \rangle$ triples from *CandidateSet<sup>M</sup>* as an enrichment plan based on the *benefit* of the triple per unit cost. Benefit, discussed formally below, corresponds to the expected improvement in the quality of the answers from previous epoch due to the execution of the enrichment plan. We restrict the choice of tuples for enrichment to only

| Al  | Algorithm 2: Benefit Calculation.   |  |  |  |  |  |
|-----|---|--|--|--|--|--|
| I   | <b>Inputs:</b> A triple containing a tuple $t_i$ , a derived attribute $\mathcal{A}_j$ , the                      |  |  |  |  |  |
|     | next best function $f_k$ for the tuple at the state in $e_{w-1}$ .  |  |  |  |  |  |
| C   | <b>Dutputs:</b> The benefit of the $\langle \text{tuple } t_i, \text{ derived attribute } \mathcal{A}_j, \rangle$ |  |  |  |  |  |
|     | enrichment function $f_k$ \ triplet.  |  |  |  |  |  |
| 1 F | unction Compute_Benefit() begin   |  |  |  |  |  |
| 2   | $PrevQuality \leftarrow \widehat{F}_{\alpha}(Ans_{w-1})$  |  |  |  |  |  |
| 3   | $\mathcal{E}_{w-1} \leftarrow ComputeEntropy(t_i, \mathcal{A}_j)$   |  |  |  |  |  |
| 4   | $\widehat{\mathcal{E}}_{w} \leftarrow \mathcal{E}_{w-1} - DeltaEntropy(t_i, \mathcal{A}_j, f_k)$                  |  |  |  |  |  |
| 5   | $Match_Probability \leftarrow ComputeInverseOfEntropy(\widehat{\mathcal{E}}_w)$                                   |  |  |  |  |  |
| 6   | $ExpectedQuality \leftarrow Quality(Match_Probability, Ans_{w-1})$  |  |  |  |  |  |
| 7   | $Benefit(t_i, \mathcal{A}_j, f_k) \leftarrow Max(ExpectedQuality - PrevQuality, 0)$                               |  |  |  |  |  |
| 8   | Return $Benefit(t_i, \mathcal{A}_j, f_k)$   |  |  |  |  |  |

those that are not in the answer set of previous epoch. This step is performed as the benefit of further enriching a tuple in  $e_w$  that was in  $Ans_{w-1}$  is significantly lower than the tuples that are not in  $Ans_{w-1}$ . We formally justify this decision in [4].

**Definition 3.1. Benefit of an Enrichment Function.** Let Q be a query,  $D_{w-1}$  be the database at the end of epoch  $e_{w-1}$ , and  $\langle t_i, \mathcal{A}_j, f_k \rangle$  be a triple to be executed in  $e_w$ . The benefit of  $\langle t_i, \mathcal{A}_j, f_k \rangle$  is defined as follows:

$$Benefit(\langle t_i, \mathcal{A}_j, f_k \rangle) = \widehat{Qty}(Q(D_{w-1} \oplus \langle t_i, \mathcal{A}_j, f_k \rangle)) - \widehat{Qty}(Q(D_{w-1}))$$
(7)

where  $Qty(Q(D_{w-1} \oplus \langle t_i, \mathcal{A}_j, f_k \rangle))$  is the estimated quality of the query answer after the triple  $\langle t_i, \mathcal{A}_j, f_k \rangle$  is executed and  $Qty(Q(D_{w-1}))$  is the estimated quality at the end of  $e_{w-1}$ .

Thus, to determine the benefit of executing an enrichment function, JENNER estimates (*i*) the quality of answer after epoch  $e_{w-1}$ and (*ii*) the expected quality of the answer set if the enrichment function is executed in the current epoch.

3.2.1 **Selection Queries**. Given  $Ans_{w-1}$  (*i.e.*,  $Q(D_{w-1})$ ), for selection queries, estimating its quality (*i.e.*,  $Qty(Q(D_{w-1}))$ ) is straightforward, since for every tuple  $t_i \in Ans_{w-1}$ , the probability of the tuple  $t_i$  to be in the  $Ans^{real}$  is known, as discussed in §2 and illustrated using the following example.

**Example 3.1.** Consider the selection query in Code Listing 1 on wifi (see Table 1). Suppose at the end of epoch  $e_1$ , the state of the tuples are as shown in Table 3 and let  $t_1$  be part of the query result. Since, the location of  $t_1$ , *i.e.*, Location.Value in Table 2 (calculated from Table 3) is [L1: 0.54, L2: 0.35, L3: 0.11] and, thus, the determinized value of location in Table 1 is L1. Hence, the combined probability of  $t_1$  satisfying all the selection conditions of the query is 0.54. The expected precision of the answer is 0.54. The recall calculation requires probability of the tuples that are part of the answer as well as of the tuples that are outside of the answer.

To compute the benefit of  $\langle t_i, \mathcal{A}_j, f_k \rangle$ , JENNER estimates the quality of the answer that would result if Q were to be executed on the database after executing  $f_k$  on  $t_i$ . Recall that with each enrichment function  $f_k$ , we have associated a measure of uncertainty reduction that is a function of the state of the derived attribute  $\mathcal{A}_j$  of tuple  $t_i$  on which  $f_k$  executes. Let the uncertainty reduction of the execution of  $f_k$  over the state of  $\mathcal{A}_j$  in tuple  $t_i$  in the current database  $D_{w-1}$  be  $\Delta$ . Such an uncertainty reduction measure  $\Delta$ 

allows us to estimate the probability of the tuple satisfying the selection condition of the query after execution of  $f_k$  as follows. Let  $\mathcal{E}_{w-1}$  be the entropy of attribute  $\mathcal{A}_j$  of  $t_i$  prior to the execution of  $f_k$ . The tuple's entropy after the execution of  $f_k$  is  $\mathcal{E}_{w-1} - \Delta$ . We estimate the new probability p of  $t_i . \mathcal{A}_j$  satisfying the selection condition by solving the following equation:

$$\mathcal{E}_{w-1} - \Delta = -p \cdot \log(p) - (1-p) \cdot \log(1-p) \tag{8}$$

Note that the equation above leads to two solutions, one that reduces the probability p of  $t_i$ .  $\mathcal{A}_i$  satisfying the selection condition (denoted as  $p_{low}$ ) and another that corresponds to the increase in probability (denoted as  $p_{high}$ ). While JENNER does not depend on the probability to monotonically increase with the execution of more enrichment functions on each tuple, for the approach to be effective we expect that such would be the case for much of the data. The works on ensemble classifiers [23, 52] provide evidence that multiple classifiers together can reduce the inference error more as compared to the individual classifiers. For a single object, the enrichment functions can make mistakes in the prediction but overall, executing more enrichment functions increases the quality of the inference. Furthermore, several authors addressed the problem of reducing the cost of ensemble classifiers on large datasets. Authors either used a separate dataset to score the performance of classifiers and chose ensemble dynamically at inference time (in Dynamic Ensemble Selection mechanisms [18, 19]) or dynamically pruned away classifiers in an existing ensemble with accuracy lower than a threshold (in Ensemble Pruning mechanisms [28, 41]).

**Example 3.2.** Consider  $t_3$  in Table 3 the value of which, based on the execution of the first two enrichment functions, is a distribution [0.15, 0.35, . . ., 0.05] over the possible locations. Given the query in Code Listing 1, the probability of  $t_3$  satisfying the predicate on location is 0.15 and not satisfying is 0.85. As a result, entropy is calculated as 0.60. Consider the execution of third enrichment function and the associated entropy reduction as 0.3. With the new entropy of (0.6-0.3) =0.3, JENNER solves Equation 1 to determine  $p_{low}$  and  $p_{high}$  as 0.05 and 0.95 respectively.

Given  $(p_{low} \text{ and } p_{high})$  of the tuple, JENNER computes the probability of the tuple to be part of the real answer of the query in epoch  $e_w$ , denoted as  $\mathcal{P}_{low}$  and  $\mathcal{P}_{high}$  respectively (as described in Definition 2.2). Considering  $\mathcal{P}_{low}$  and  $\mathcal{P}_{high}$  of the tuple and the probabilities of other tuples satisfying the query condition (which is the same as in the previous epoch  $e_{w-1}$ ), JENNER determines the answer that would be return to the user in order to maximize the answer quality (as discussed in §3.5). Thus, JENNER can determine the answers returned in both cases when the probability of  $t_i.\mathcal{A}_j$  satisfying the query condition is  $\mathcal{P}_{low}$  or it is  $\mathcal{P}_{high}$ . Let these answers be  $Ans_{low}$  and  $Ans_{high}$  respectively.

We can now determine the estimated quality of the answer after execution of  $f_k$  on  $t_i$ . $\mathcal{A}_j$  as a weighted sum of the quality of the potential answers  $\widehat{Qty}(Ans_{low})$  and  $\widehat{Qty}(Ans_{high})$ .

$$p_{w-1}Qty(Ans_{high}) + (1 - p_{w-1})Qty(Ans_{low})$$
(9)

where  $p_{w-1}$  refers to the probability of  $t_i \mathcal{A}_j$  satisfying the query condition in its state in  $D_{w-1}$ .

Given the above expected quality of answers after execution of  $f_k$  on  $t_i$ . $\mathcal{A}_j$ , we can now determine the benefit of its execution to the results. Note that such a value could be negative depending

upon the value of  $p_{w-1}$ . In this case, we consider the benefit to be 0 and such a function would not be chosen for enrichment.

3.2.2 **Generalizing to Other Queries**. To estimate the benefit for general queries, we extended the model for both estimating the quality of query result in the previous epoch  $e_{w-1}$  and the benefit of executing the triples in enrichment plan  $EP_w$  of the current epoch  $e_w$ . Let us consider a query Q with conditions on n relations  $R_1$ ,  $R_2, \ldots, R_n$ . For each  $R_i$ , there could be multiple selection and join conditions on both fixed and derived attributes.

For queries with join conditions, the benefit is computed for each tuple of the relations separately, *i.e.*, JENNER does not compute the benefit of the composite tuples generated from two tuples of the different relations. This allows JENNER to measure the benefit of the tuples in linear time irrespective of the type of the query. At epoch  $e_{w-1}$ , the tuples of  $R_i$  are classified as one of the following two types: (*i*) the tuples that have met the selection condition on derived attributes of  $R_i$ , denoted by  $R_i^{\sigma}$ , <sup>6</sup> and (*ii*) the tuples that do not satisfy such selection conditions, are denoted by  $R_i^{-\sigma}$ . The tuples of  $R_i^{\sigma}$  are further classified as those that were part of the answer set (*i.e.*, at-least one tuple in the answer set (*i.e.*, no tuples in the answer set of  $e_{w-1}$  was generated by these tuples) or not in the answer set (*i.e.*, no tuples).

To determine  $R_i^{\sigma}$ , JENNER first determines  $Ans_{w-1}$  and finds out the tuple of  $R_i$  with minimum *match\_prob* (*i.e.*, probability of satisfying all the selection conditions of  $R_i$ ) that still qualified to be part of  $Ans_{w-1}$ . This minimum *match\_prob* is denoted as the *relation-threshold* of  $R_i$ . The tuples with *match\_prob* higher than this threshold forms  $R_i^{\sigma}$  and the remaining tuples form the set of  $R_i^{\neg\sigma}$ . The candidate tuples are chosen from  $R_i^{\neg\sigma}$  of the relations.

To compute the probability of a tuple  $t_i \in Ans_w$  to be part of Ans<sup>real</sup>, let us consider the projection of  $t_i$  to its constituent tuples in relations of  $R_1, \ldots, R_n$ . Let us denote the corresponding tuple in  $R_i$  as  $t_i[R_i]$ . The probability of  $t_i[R_i]$  satisfying the selection condition in Q on attributes in  $R_i$  is computed as discussed above in the context of selection queries. The probability of the join condition between two relations  $R_i$  and  $R_k$  (say  $R_i \mathcal{A}_m = R_k \mathcal{A}_m$ ) being satisfied by  $t_i$  is computed as follows: let the determinized value of  $t_i[R_i]$  be  $Det(t_i[R_i])$ . The probability of  $t_i[R_i]$  satisfying the join condition on derived  $\mathcal{A}_m$  is  $Val(state(t_i[R_i],\mathcal{A}_m))[Det(t_i[R_i],\mathcal{A}_m)]$ . attribute Likewise, suppose the determinized value of  $t_i[R_k]$  be  $Det(t_i[R_k])$ . The probability of  $t_i[R_k]$  satisfying the join condition on  $\mathcal{A}_m$  is  $Val(state(t_i[R_k].\mathcal{A}_m))[Det(t_i[R_k].\mathcal{A}_m)]$ . Hence, the probability of tuple  $t_i$  satisfying the join condition of  $R_j \mathcal{A}_m = R_k \mathcal{A}_m$  is the product of the above two probabilities, *i.e.*,  $Val(state(t_i[R_i].\mathcal{A}_m))[Det(t_i[R_i].\mathcal{A}_m)] \times$  $Val(state(t_i[R_k],\mathcal{A}_m))[Det(t_i[R_k],\mathcal{A}_m)]$ . The overall probability of tuple  $t_i$  is computed by computing the product of all the probabilities for the predicates present in Q.

Given the probability of all tuples  $t_i \in Ans_w$  to be part of real answer set  $Ans^{real}$ , JENNER computes  $F_{\alpha}$  measure by Equation 5. To compute benefit of a triple  $\langle t_i, \mathcal{A}_j, f_k \rangle$ , where  $t_i$  is in relation  $R_p$  and it is part of  $R_p^{\neg\sigma}$ , JENNER estimates the quality of the answer that would result if Q were to be executed on the database after executing <sup>6</sup>If there are no selection conditions on derived attributes then all the tuples are part of  $R_i^{\sigma}$ .  $f_k$  on  $t_i$ . $\mathcal{A}_j$ . JENNER follows the same strategy as selection queries where it generates  $p_{low}$  and  $p_{high}$  for the condition on  $t_i$ . $\mathcal{A}_j$  to be met. In each case, it re-executes the query, generates the answers  $Ans_{high}$  and  $Ans_{low}$ . As in selection queries, it chooses an answer with maximum quality (as described in §3.5).

The above way of computing benefit for executing  $f_k$  on  $t_i$ . $\mathcal{A}_j$  requires (*i*) determining the probabilities  $p_{low}$  and  $p_{high}$  from the entropy reduction of  $f_k$ , (*ii*) re-executing Q on the database state resulting in  $D_{e_{w-1}}$  with the probability of  $t_i$ . $\mathcal{A}_j$  matching the query condition modified to  $p_{low}$  (or  $p_{high}$ ), and (*iii*) run *ProduceQueryResult* in both cases (the complexity, as will be clear in §3.5 is |Ans|log(|Ans|), where |Ans| is the size of the answer from which query result is selected). Thus, the complexity of above three steps is  $O(costQ + |Ans_w|log(|Ans_w|))$ , where costQ is the time to execute Q,  $|Ans_w|$  is the size of answers returned. As a result, the overall complexity of benefit estimation is  $O(n(costQ + |Ans_w|log(|Ans_w|)))$  where n is the size of  $CandidateSet^M$ .

#### 3.3 Selecting Enrichment Plan

This step chooses a set of (tuple, derived attribute, enrichment function) triples as the enrichment plan of epoch  $e_w$ . The problem of selecting an enrichment plan is a budgeted Knapsack problem as we need to find an enrichment plan with total cost less than or equal to epoch duration and that has maximum sum of benefit values among all the possible subset of ranked tuples. JENNER uses a greedy approach to choose this enrichment plan for the epoch  $e_w$ . For the (tuple, derived attribute, enrichment function) triples in  $CandidateSet^M$ , it computes the benefit as described earlier. The triples in CandidateSet are sorted in decreasing order of their *benefit/cost* values. The enrichment plan is chosen from the sorted set starting from the triple with highest *benefit/cost* value. Note that choosing the triples based on benefit/cost, allowed JEN-NER to achieve two goals: (i) If a triple has a very high benefit value but the cost of enrichment function is also high then such triples are not executed in the beginning and (ii) triples with smaller benefit and cost can be enriched in the beginning in large numbers to achieve higher improvement of the answer quality.

#### 3.4 Execution of Enrichment Plan

This step executes the (tuple, derived attribute, enrichment function triples present in  $EP_w$ . While executing an enrichment function on a set of tuples, JENNER batches the tuples together and then execute the enrichment function on them. For each tuple  $t_i \in EP_w$ , JENNER updates the state of  $t_i$ . Next, the determinized representation of  $t_i$  is updated based on the output of all the enrichment functions executed on it. For each tuple for which a derived attribute value was enriched, the NBF function for that attribute changes. Hence, JENNER, calculates the new benefit of the tuple, if it is enriched using the NBF function at the current state. These updated benefit of the tuples that were enriched in epoch  $e_w$  are reflected in the *CandidateSet*<sup>M</sup> data structure. Hence, the next epoch can choose an enrichment plan by comparing the updated benefit of enriched tuples in  $e_w$  and the previous benefit of tuples that were not enriched. In an epoch, JENNER keeps executing the triples until the epoch duration is exhausted.

#### 3.5 Produce Query Result

After the state update of tuples enriched in  $e_w$ , the original query Q is re-executed on the determinized representation to find the set of potential answer. For each tuple  $t_i$  in computed  $Ans_w$ , JENNER determines the probability of  $t_i$  to be in  $Ans^{real}$ , based on the probability of the tuples in base relations that constructed  $t_i$ . Instead of returning  $Ans_w$ , it returns a subset of tuples that maximizes the answer quality (*i.e.*,  $F_\alpha$ -measure for set-based queries). For aggregation queries, JENNER first determines the set of answers that optimizes  $F_\alpha$ -measure and then computes the aggregation function. Note that it is possible that a tuple that was returned as an answer in one of the previous epochs is retracted in the current epoch  $e_w$ .

JENNER is based on the following observation (proved in a theorem in [4]) : Let  $t_1, t_2, \ldots, t_n$  be the set of tuples in  $Ans_w$  sorted by their probability of being in  $Ans^{real}$ . The  $E(F_\alpha)$  measure of the query result increases monotonically with the inclusion of more tuples  $t_i$  starting with the highest probability value up to the inclusion of a certain tuple; beyond which the  $E(F_\alpha)$  measure decreases monotonically with the inclusion of any more tuples.

JENNER utilizes this observation where it sorts the tuples of  $Ans_w$  based on their probability of being in  $Ans^{real}$  and continue including answer tuples until  $E(F_\alpha)$  measure of the answer is maximized. We refer to the probability of the last tuple that is part of the answer of epoch  $e_w$  as the *answer-threshold*. The time complexity of this step is O(nlog(n)) where *n* is the size of *CandidateSet<sup>M</sup>*.

**Example 3.3.** Consider the query of Figure 1a with conditions on relations  $R_1$  and  $R_2$ . Suppose the probe query results of  $R_1$  and  $R_2$  contained five tuples:  $\langle r_1^1, r_2^1, ..., r_5^1 \rangle$  and ten tuples:  $\langle r_1^2, ..., r_{10}^2 \rangle$  respectively. Without loss of generality, suppose the tuples of each relation are sorted by their probability of satisfying all the selection conditions on derived attributes. Considering the possible tuple pairs of  $\langle \langle r_1^1, r_1^2 \rangle, ..., \langle r_5^1, r_{10}^2 \rangle \rangle$ , JENNER computes the probability of the tuples as shown in Example 3.4. JENNER keeps including the tuples in  $Ans_w$  chosen in this way has maximum  $E(F_\alpha)$  measured.

We next discuss how the probability of a tuple  $t_i \in Ans_w$  to be in the true answer is calculated based on the corresponding tuples in base relations  $R_i \in Q$  that formed  $t_i$ . For selection queries over a single derived attribute, it is the probability of the value of the tuple to match the condition (*i.e.*,  $Val(state(t,\mathcal{R}_j)) = a_j$  for a selection condition of  $\mathcal{R}_j = a_j$ ). For multiple selection conditions on derived attributes of a relation, the probability is estimated under the independence assumption of derived attributes. For queries where answer tuple  $t_i$  is formed using tuples from multiple relations, the corresponding probability is based on the product of probabilities of individual tuples to satisfy the individual selection and join conditions.<sup>7</sup> An example is shown below.

**Example 3.4.** Consider the query of Figure 1a on  $R_1$  and  $R_2$  and two tuples  $r_1 \in R_1$  and  $r_2 \in R_2$  which were part of the probe query results of  $R_1$  and  $R_2$ . Suppose,  $r_1.\mathcal{A}_1$  is  $a_1$  (*i.e.*, the value with highest probability after determinization) and the probability associated with the value is 0.9. Similarly, let  $r_2.\mathcal{A}_6$  be  $a_6$  and the probability associated with it is 0.8. Considering the join condition on derived attribute (*i.e.*,  $R_1.\mathcal{A}_3 = R_2.\mathcal{A}_3$ ), suppose the attribute values of the tuples after determinization on  $\mathcal{A}_3$  match and the

<sup>&</sup>lt;sup>7</sup>For duplicates, probability values are added up as in probabilistic databases [20].

Table 4: Queries used in the experiments.

| ID | Query  |
|----|--|
| Q1 | Trajectory of a person in a time interval.                         |
| Q2 | Users who came in contact with a specific user in a time interval. |
| Q3 | Average time spent by a user in different infrastructure types.    |
| Q4 | Tweets with positive sentiment and of a particular topic.          |
| Q5 | Tweet pairs with same sentiment value posted between an interval.  |
| Q6 | Tweets with positive sentiment posted from a particular state be-  |
|    | tween two time intervals.  |
| Q7 | Number of tweets posted for each topic between two time intervals. |

corresponding probabilities are 0.95 and 0.85. Hence, the probability of the tuple pair  $\langle r_1, r_2 \rangle$  satisfying all the query conditions in Qis  $\mathcal{P}(\langle r_1, r_2 \rangle) = 0.9 \times 0.8 \times 0.95 \times 0.85 = 0.58$ . We compute these probabilities for all the tuple pairs in the probe query result of  $R_1$  and  $R_2$  and whose determinized representation of the derived attribute matches the conditions in the query.

After determining the  $Ans_w$  that optimizes the quality metric  $E(F_\alpha)$ , JENNER prunes tuples from the candidate set whose impact on quality improvement of the answer set in subsequent epochs is expected to be low. JENNER finds out the tuples of each relation that already contributed to  $Ans_w$  of the current epoch and removing them from *CandidateSet*<sup>M</sup>. Enriching such tuples has low impact on improving the quality of the query result as proved in [4].

#### 3.6 Optimizing Benefit Computation

The techniques for benefit computation for an enrichment function  $f_k$  on attribute  $t_i \mathcal{A}_i$ , as described in §3.2.1 and §3.2.2, used simulated execution of  $f_k$  to assess the impact of execution on the overall quality of the query answers. Their overall time complexity is  $O(n(costQ + |Ans_w|loq(|Ans_w|)))$  where n is the size of *CandidateSet<sup>M</sup>*. This section presents a strategy wherein SelectEnrichmentPlan can select the plan without explicitly calculating the benefit of the enrichment functions. We define a metric, RelativeBenefit, that allows JENNER to order the triples as if they were ordered based on their *benefit/cost* value. This metric is derived from the expression of expected  $F_{\alpha}$  measure in Equation 5. In deriving this metric, we choose two triples from  $CandidateSet^M$ and derive how much expected  $F_{\alpha}$  measure improvement per unit cost can be brought by enriching them in the current epoch. Then, we derive the condition in which one of the triples has higher expected  $F_{\alpha}$  measure improvement per unit cost than the other. It is observed that their ordering depends on  $\mathcal{P}_i$ , *i.e.*, probability of the tuple satisfying the query condition in epoch  $e_{w-1}$ ,  $(\mathcal{P}_i + \Delta \mathcal{P}_i)$ , *i.e.*, the new probability of  $t_i$  if it is enriched in the current epoch of  $e_w$ , and the cost of the enrichment function. We explain the metric first for selection queries and then generalize it.

**Selection Query.** In the modified strategy, for each  $\langle t_i, \mathcal{A}_j, f_k \rangle \in CanddiateSet^M$ , we compute the *RelativeBenefit* defined below.

$$RelativeBenefit(t_i, \mathcal{A}_j, f_k) = \frac{\mathcal{P}_i(\mathcal{P}_i + \Delta \mathcal{P}_i)}{c_k}$$
(10)

where  $\mathcal{P}_i$  is the probability of the tuple satisfying the query in the previous epoch of  $e_{w-1}$  and  $(\mathcal{P}_i + \Delta \mathcal{P}_i)$  is the value of  $\mathcal{P}_{high}$ , *i.e.*, the new probability of  $t_i$  satisfying the query if it is enriched in the current epoch of  $e_w$ . The value of  $\mathcal{P}_{high}$  is calculated as described in Definition 2.2 and in Section 3.2.1. JENNER only uses  $\mathcal{P}_{high}$ , instead

Table 5: Datasets and cost/quality tradeoff of functions.

|             |                | 1 2      |           |         |
|-------------|----------------|----------|-----------|---------|
| Relation    | Derived attrs. | Function | Cost (ms) | Quality |
| WiFi        |                | LOC_2    | 24.5      | 0.68    |
| 10M tuples  | location(304)  | LOC_4    | 46.4      | 0.75    |
| 9GB Size    | 100at1011(304) | LOC_8    | 93.7      | 0.82    |
| JOD 512C    |                | LOC_16   | 186.4     | 0.91    |
|             | sentiment(3)   | SVM      | 1.67      | 0.61    |
|             |                | KNN      | 2.81      | 0.72    |
| TweetData   |                | GNB      | 5.32      | 0.81    |
| 11M tuples  |                | MLP      | 6.26      | 0.89    |
| 10.5GB Size |                | LDA      | 2.17      | 0.58    |
| 10.500 5120 |                | LR       | 3.89      | 0.67    |
|             | topic(40)      | KNN      | 5.48      | 0.75    |
|             |                | GNB      | 7.82      | 0.88    |

of  $\mathcal{P}_{low}$ , as by using the latter the benefit of the triple is 0. Below, we show that ordering two triples based on *RelativeBenefit* metric ensures that they are ordered based on their *Benefit/Cost* values.

Example 3.5. Consider the query of Figure 1a on relations R<sub>1</sub> and  $R_2$  and two tuples  $r_1 \in R_1$  and  $r_2 \in R_2$ . Suppose, the probability of  $r_1$  satisfying all the conditions on derived attributes (*i.e.*,  $\mathcal{P}_1$ ) be 0.8 in epoch  $e_{w-1}$ . Similarly, let the probability of the tuple  $r_2$  be 0.7 in  $e_{w-1}$ . If  $r_1$  is enriched in epoch  $e_w$ , let the new probability values of satisfying the query be as follows:  $\mathcal{P}_{high} = 0.9$  and  $\mathcal{P}_{low} = 0.1$ . The *RelativeBenefit* of  $r_1$  is  $(0.8 \times 0.9)/0.04 = 18$ . Similarly, if  $r_2$  is enriched, let the new probabilities of  $r_2$  be  $\mathcal{P}_{high} = 0.75$  and  $\mathcal{P}_{low} =$ 0.25. Hence, the *RelativeBenefit* of  $r_2$  is  $(0.75 \times 0.7)/0.03 = 17.5$ . Comparing the *RelativeBenefit* of tuples, JENNER ranks  $r_1$  before  $r_2$ . Now, we check if enriching tuple  $r_1$  improves the expected  $F_{\alpha}$  measure of the answer set per unit cost more as compared to  $r_2$ . Recall that expected  $F_{\alpha}$  measure is calculated using Equation 5. Considering that all the tuples, except  $r_1$  and  $r_2$ , that were in the answer set of epoch  $e_{w-1}$ , still remain part of the answer in  $e_w,$  the numerator of  $F_\alpha$  measure is increased by  $\mathcal{P}_{high}$  in  $e_w.$  The denominator increases by the value of  $(1 + \Delta \mathcal{P}_1) = 1 + (\mathcal{P}_{high} - \mathcal{P}_{high})$  $\mathcal{P}_1$ ). Let the numerator of expected  $F_{\alpha}$  measure in  $e_{w-1}$  be 30 and the denominator be 50, *i.e.*,  $F_{\alpha} = (30/50) = 0.6$ . Hence, the  $F_{\alpha}$ measure of the answer due to the enrichment of  $r_1$  is (30+0.9)/(50+1 + 0.1 = 0.6046. Similarly, the  $F_{\alpha}$  measure due to  $r_2$  is (30 + (0.75)/(50 + 1 + 0.05) = 0.6024. Hence, the *Benefit* per unit cost of  $r_1$ (i.e., (0.046/0.04) = 1.15) is higher than  $r_2$  (i.e., (0.024/0.03) = 0.8).

THEOREM 1. A triple  $(t_i, \mathcal{A}_j, f_k)$  has higher benefit than a triple  $(t_q, \mathcal{A}_s, f_v)$  in epoch w irrespective of the values of  $\mathcal{P}_i, \mathcal{P}_q, \Delta \mathcal{P}_i$  and  $\Delta \mathcal{P}_q$  if the following condition holds:

 $RelativeBenefit(t_i, \mathcal{A}_j, f_k) > RelativeBenefit(t_q, \mathcal{A}_s, f_v)$ (11)

**Proof Sketch.** We prove this theorem as follows: for the given values of  $\mathcal{P}_i$ ,  $\mathcal{P}_q$ ,  $\Delta \mathcal{P}_i$  and  $\Delta \mathcal{P}_q$ , there can be four possible orders among them. They are as follows: (i)  $\mathcal{P}_i > \mathcal{P}_q$  and  $\Delta \mathcal{P}_i > \Delta \mathcal{P}_q$ , (ii)  $\mathcal{P}_i > \mathcal{P}_q$  and  $\Delta \mathcal{P}_i > \Delta \mathcal{P}_q$ , (iii)  $\mathcal{P}_i < \mathcal{P}_q$  and  $\Delta \mathcal{P}_i < \Delta \mathcal{P}_q$ , (iii)  $\mathcal{P}_i < \mathcal{P}_q$  and  $\Delta \mathcal{P}_i > \Delta \mathcal{P}_q$ , (iv)  $\mathcal{P}_i < \mathcal{P}_q$  and  $\Delta \mathcal{P}_i < \Delta \mathcal{P}_q$ . In each of these orders, we determine the answer set by calculating the new threshold probability value. After determining the answer set, the quality of the answer set is calculated separately both when triple  $(t_i, \mathcal{A}_j, f_k)$  and triple  $(t_q, \mathcal{A}_s, f_v)$  are enriched. We measure their benefit using Equation 7. By simplifying the equation, it is observed that the first triple will have higher benefit/cost than the second one when the condition in Equation 11 is satisfied. We provide the complete proof in [4].

Given the above theorem, JENNER computes *RelativeBenefit* of the triples and selects an enrichment plan (§3.3). This results in a

Table 6: Exp 1. Query time without progressiveness (in Mins).

| Query | Q1 | Q2   | Q3   | Q4   | Q5   | Q6   | Q7   |
|-------|----|------|------|------|------|------|------|
| Time  | 31 | 44.5 | 40.6 | 22.1 | 67.1 | 39.2 | 45.1 |

time complexity of O(n), where *n* is the size of *CandidateSet*<sup>*M*</sup> as compared to the approach of computing benefits explicitly.

**More General Queries.** To exploit the previous strategy in other queries, we need to estimate the number of tuples that would result from a tuple  $t_i$  in relation  $R_p$ . JENNER estimates the average number of tuples that were generated by the tuples in  $R_p^{\sigma}$  in the answer of  $Ans_{w-1}$ . We refer to this value as  $\lambda^{w-1}(R_p)$ . We measure the relative benefit of  $\langle t_i, \mathcal{A}_j, f_k \rangle$ , where  $t_i \in R_p$  as follows:

$$RelativeBenefit(t_i, \mathcal{A}_j, f_k) = \lambda_{R_i} \cdot \left[\frac{\mathcal{P}_i(\mathcal{P}_i + \Delta \mathcal{P}_i)}{c_k}\right]$$
(12)

The relative benefit reflects the amount of improvement in the quality of the query result that is achieved by the answer tuples generated from tuple  $t_i$  in  $R_p$ . As for selection queries, the enrichment plan  $EP_w$  is chosen using the above *RelativeBenefit* metric.

#### **4 EXPERIMENTAL EVALUATION**

**Datasets.** We used the following datasets to evaluate JENNER: (*i*) WiFi data containing 10M WiFi connectivity events of user's mobile devices in a university campus (taken from the SmartBench benchmark[29]) and (*ii*) TweetData containing 11 million tweets.

**Enrichment Functions.** The enrichment functions are presented in Table 5. For the wifi dataset, we used multiple versions of the algorithm in [38] (LOC\_n). LOC\_n analyzes the pattern of the locations visited by the user and the interaction between the user and other users to infer their location. It is implemented as a multituple-input enrichment function with the tuples collected in the past *n* days as input. For the tweet dataset, we used the following probabilistic classifiers (single-tuple-input enrichment functions): Support Vector Machine (SVM), k-Nearest Neighbor (KNN), Gaussian Naïve Bayes (GNB), Multi-Layered perceptron (MLP), Linear Discriminant Analysis (LDA), and Logistic Regression (LR).

**Queries.** Table 4 shows the queries used in our experimental study. **Q1-Q3** are from the SmartBench benchmark [29] on the wifi dataset. Q1 is a simpler query with selection conditions on derived attributes while Q2 and Q3 require join on derived attributes. Q4-Q7 are analytical queries over Tweet data with different complexities - Q4 is a selection query, Q5-Q6 are join queries, and Q7 is an aggregation query. The SQL implementations of all queries are available in [4]. The epoch sizes in Experiment 1 are set according to the optimal epoch sizes determined by Experiment 5 for different queries. The quality of the query results are measured using the ground truth data available for the datasets. JENNER uses expected  $F_{\alpha}$  measure and *RelativeBenefit* to select the enrichment plans without using ground truths. Note that, we do not consider the enrichment functions to be 100% accurate (i.e., executing all enrichment functions might result in an  $F_1$  measure lower than 1).

**Enrichment Plan Generation Strategies.** We compare JENNER with three different plan generation strategies: (*i*) *Sample-based with Object Order* (**OO**): that randomly selects tuples from the set of tuples satisfying predicates on fixed attributes. Selected tuples are completely enriched by executing all enrichment functions

Table 7: Exp 2. Total time of query execution and enrichment with varying selectivity of fixed condition in Q4.

| Selectivity | TTR (90%)  | TTR (95%)  | Query Completion   |
|-------------|------------|------------|--------------------|
| 100%        | 18.37 mins | 25.19 mins | 10 hours (timeout) |
| 10%         | 5.88 mins  | 8.71 mins  | 4.48 hours         |
| 1%          | 25.19 sec  | 2.1 mins   | 27.29 mins         |

Table 8: Exp 3. Progressive Scores.

| Q  | JENNER | FO   | 00   | RO   | Q  | JENNER | FO   | 00   | RO   |
|----|--------|------|------|------|----|--------|------|------|------|
| Q1 | 0.87   | 0.36 | 0.33 | 0.32 | Q5 | 0.73   | 0.39 | 0.35 | 0.33 |
| Q2 | 0.84   | 0.34 | 0.32 | 0.31 | Q6 | 0.72   | 0.37 | 0.36 | 0.32 |
| Q3 | 0.76   | 0.43 | 0.35 | 0.31 | Q7 | 0.74   | 0.37 | 0.33 | 0.34 |
| Q4 | 0.80   | 0.34 | 0.33 | 0.31 |    |        |      |      |      |

available for derived attributes present in the query. (*ii*) Samplebased with Function Order (FO): that selects enrichment functions based on the decreasing order of their  $\frac{quality}{cost}$  values. The function with the highest value is executed on all tuples of the probe query result before choosing the next function. In an epoch, only tuples are chosen and they are enriched using the chosen function. (*iii*) Sample-based with Random Order (RO): that selects both tuples (from probe query results) and enrichment functions randomly.

#### 4.1 Experimental Results

The experiments were performed on an enrichment server with 16 core 2.50GHz Intel Xeon CPU, 64GB RAM, and 1TB SSD. The datasets were stored in two tables of a PostgreSQL database. If we had to perform complete enrichment of 11M tweets of TweetData table for both topic and sentiment attributes using the functions of Table 5, it would have taken  $\approx$  **43 hours** to complete after using all the 16 cores of the server.<sup>8</sup> The authors in [21] also showed that sentiment inference on tweets using complex ML algorithms can take hours for the Sentiment140 dataset [27] with 1.6 million tweets. The complete enrichment of 100K wifi data for the derived attribute of location would have taken  $\approx$  37 days on the same server. Hence, complete enrichment of the data is infeasible.

**Experiment 1 (Need for a Progressive Approach).** We compare JENNER with the approach of completely enriching the objects required to answer the query first and then evaluating the query. The query execution times in the second approach are presented in Table 6. Since, in the second approach, all the required objects (*i.e.*, the objects present in the probe query result) are enriched first, all the queries have very high execution times. In contrast, if we execute the same queries in JENNER, users do not have to wait for a long time to receive the query results. Furthermore, the variation of the quality of the results with respect to time are presented in Figure 2. It shows that in JENNER, the quality of the query result achieves very high value within a few seconds of query execution.

**Experiment 2 (Eager Enrichment VS. JENNER).** We vary query selectivities to compare JENNER against the strategy of complete enrichment (*i.e.*, Eager). We define the selectivity as the ratio of output-cardinality to the input-cardinality of a query. We use Q4 and replace the predicate on TweetTime to control the selectivity. Table 7 shows the time to reach the qualities of 90%, 95%, and 100%

<sup>&</sup>lt;sup>8</sup>We experimentally measured the runtime of the enrichment functions in the tweet dataset for 1 million tweets to be 3 hours 55 minutes. This runtime multiplied by a factor of 11, as the dataset has 11 million tweets, is  $\approx$  43 hours.

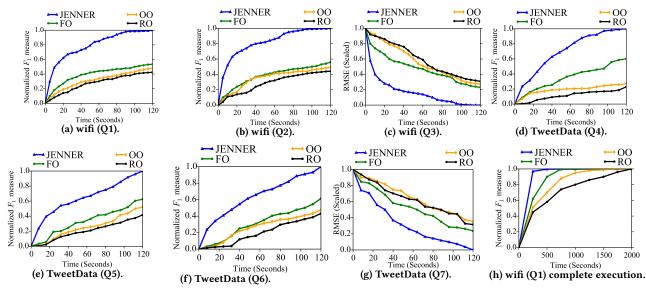


Figure 2: Exp 1 and Exp 3. Performance results of different plan generation strategies.

of the maximum quality in JENNER. Comparing Table 7 and the time required in the eager enrichment strategy (*i.e.*,  $\approx$  43 hours), we observe that the total time for query processing and enrichment in JENNER is much lower than the eager strategy. Furthermore, Table 7 shows that JENNER achieves 90% and 95% of the maximum quality within a few minutes of query execution. Only in the unfavorable case of 100% selectivity and 100% quality, the execution time is as high as the eager strategy. Even in such situations (not our design target) JENNER does not result in much overhead (as in Table 9), whereas it saves several orders of magnitude in the favorable situations of lower selectivity and quality requirement.

**Experiment 3 (Comparison with Different Progressive Ap**proaches). This experiment compares JENNER with FO, OO, and RO approaches. Progressive score is computed as a weighted summation of  $F_1$  measures with weight of the epoch  $e_w$  set as  $(1 - \frac{w}{w_{max}})$ where the  $w_{max}$  (corresponding to the maximum number of epochs) is set as 15. The results are shown in Figure 2 where we measure the quality of the query result using normalized  $F_1$  measure for set based queries and normalized root-mean-square-error (RMSE) for aggregation queries (Q3 and Q7). The normalized  $F_1$  measure is calculated as  $F_1/F_1^{max}$ , where  $F_1^{max}$  is the maximum  $F_1$  measure that is achievable by executing all the enrichment functions.<sup>9</sup> Similarly, normalized root-mean-square-error is calculated by measuring RMSE/RMSE<sup>min</sup> where RMSE<sup>min</sup> is the minimum RMSE achievable by executing all enrichment functions. Furthermore, we report the progressive scores in Table 8. Note that in Figures 2a-2g, the plots are capped to only the first two minutes of query execution as the time to enrich completely is large. When the queries are run for the duration of complete enrichment, all the approaches converge to the value of 1 for set-based queries (as shown for Q1 in Figure 2h) and the value of 0 for the aggregation query of Q7.

Figure 2 and Table 8 show that JENNER outperforms the other approaches significantly for all queries. With JENNER, the answer achieves a high quality within first few epochs of query execution. For example, Figure 2(a) shows that JENNER achieves  $F_1$ -measure of 0.9 within first 80 seconds. Furthermore, JENNER achieves a

 Table 9: Exp 4. Overhead as compared to the total query execution time. The remaining time is used in enrichment.

| Q  | Plan   | DBMS  | Network | Q  | Plan  | DBMS  | Network |
|----|--------|-------|---------|----|-------|-------|---------|
|    | Gen.   | Time  | Cost    |    | Gen.  | Time  | Cost    |
| Q1 | 0.64 % | 0.37% | 0.86%   | Q5 | 1.32% | 1.84% | 2.90%   |
| Q2 | 0.93%  | 0.52% | 0.60%   | Q6 | 0.71% | 1.20% | 2.71%   |
| Q3 | 0.96%  | 0.73% | 0.65%   | Q7 | 1.33% | 1.10% | 1.40%   |
| Q4 | 1.45%  | 0.70% | 2.80%   |    |       |       |         |

high rate of quality improvement in early epochs resulting in the highest progressive score among all the approaches. This is due to JENNER's strategy of monitoring the progress of enrichment in each epoch and dynamically selecting an enrichment plan.

Experiment 4 (Overhead). Table 9 shows different time overheads of JENNER: (i) time spent in the enrichment plan generation, (ii) execution time in the DBMS, and (iii) the network cost of transmitting data between DBMS and enrichment server. We measured the total plan generation time across all epochs and reported the sum as the percentage of total time. For DBMS time, we measured the total cost of probe queries and the queries at the end of each epoch. For network cost, we measured the total cost of transmitting the result of probe queries at zero-th epoch and updating the states of tuples at the end of epochs. The results show that (i) the cost at DBMS increases when the query complexity increases (e.g., see increase in DBMS time between Q4 and Q5); (ii) total overhead remains a small fraction of the overall execution time (ranging from 1.87% to 6.05%). Thus, JENNER's adaptive approach of selecting tuples to enrich does not pose significant overhead. For storage overhead, the total size of *CandidateSet*, *CandidateSet*<sup>M</sup>, and *EP*<sub>w</sub> were less than 10 MB which is a small fraction of the data sizes (i.e., 9 GB and 10.5 GB as shown in Table 5). Furthermore, the state table sizes for wifi and TweetData tables were 0.4 GB and 0.9 GB, respectively.

**Experiment 5 (Epoch Size).** This experiment studies how epoch size affects progressiveness achieved for the queries. Figure 3 plots: (*i*) Time to reach (TTR) 90% quality by JENNER for Q2 (1% selectivity) and (*ii*) Time overhead as percentage of total query execution time. Figure 3(a) shows that when the epoch size is reduced from 8 to 4 seconds, the TTR 90% reduces as JENNER chooses enrichment

 $<sup>^9</sup>$  Recall that our evaluation of  $F_1$  measure in experiments is based on the ground truth data since we have access to them.

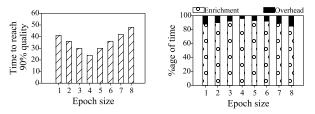


Figure 3: Exp 5. Effect of epoch sizes: (a) time to reach 90% of max. quality (Q2) and (b) %age of plan generation time.

Table 10: Exp 6. Avg. Number of Candidates in CandidateSet<sup>M</sup>.

| Query | JENNER | Naive | Query | JENNER | Naive |
|-------|--------|-------|-------|--------|-------|
| Q1    | 800    | 3000  | Q5    | 11000  | 20000 |
| Q2    | 1200   | 5000  | Q6    | 6000   | 10000 |
| Q3    | 16000  | 50000 | Q7    | 500    | 1000  |
| Q4    | 1200   | 2000  |       |        |       |

Table 11: Exp 7. Percentage of enrichment plan generation time taken by using relative benefit as compared to benefit.

| Query | rel. benefit | benefit | Query | rel. benefit | benefit |
|-------|--------------|---------|-------|--------------|---------|
| Q1    | 0.64%        | 32.17%  | Q5    | 1.32%        | 94.17%  |
| Q2    | 0.93%        | 61.45%  | Q6    | 0.85%        | 58.96%  |
| Q3    | 0.96%        | 82.38%  | Q7    | 0.62%        | 43.14%  |
| Q4    | 1.45%        | 88%     |       |              |         |

plans more frequently. However, when it is reduced further from 4 to 2 seconds, the overheads due to frequent plan generation reduces the effective time for enrichment, thereby increases the TTR.

**Experiment 6 (Impact of Pruning).** As shown in §3.2, JENNER restricts tuples in the enrichment plan to only those that are not in the answer of previous epoch. We compare this strategy with the strategy of using all tuples in *CandidateSet*( $R_i$ ) for generating enrichment plans. Table 10 shows that the size of *CandidateSet<sup>M</sup>* in JENNER is significantly smaller, hence reducing the cost of plan generation. The entries in *CandidateSet<sup>M</sup>* pruned by JENNER were (almost) never chosen for enrichment. As a result, this cost reduction comes with no impact on the quality achieved by JENNER.

**Experiment 7 (Impact of Optimized Benefit Estimation).** This experiment compares JENNER when it uses the naive strategy (described in §3.2) of benefit estimation as compared to the strategy in §3.6 used in JENNER (with complexity O(n)). Table 11 presents the percentage of total execution time taken by the two approaches. The table shows that the naive strategy would have taken 32% to 94 % of total execution time to estimate benefit, thereby making JENNER impractical. Hence, benefit estimation using *RelativeBenefit* allowed JENNER to allocate most of the execution time to enrichment.

**Experiment 8 (Accuracy of Different Estimation Steps).** In each epoch  $e_w$ , for a tuple  $t_i \in R_j$  that was in the probe query result, JENNER estimates the probability that it will be in the answer of  $e_w$  (*i.e.*, generate at-least one answer tuple). Furthermore, JENNER estimates the cardinality, *i.e.*, the number of answer tuples that will be generated by  $t_i$ . Both estimations are based on the answer returned in the previous epoch  $e_{w-1}$ . We measure accuracy of both estimations by calculating the Standard Deviation (SD) from the actual value (determined by ground truth) and the estimated value.

In an epoch, the deviation in estimated probability and cardinality is calculated for each tuple of the probe query result and then

Table 12: Exp 8. Accuracy of (a) probability estimation and(b) cardinality estimation.

| Q  | Std. Dev. | Q  | Std. Dev. |   | Q  | Std. Dev. |
|----|-----------|----|-----------|---|----|-----------|
| Q1 | 1.18%     | Q5 | 2.31%     |   | Q1 | 2.06%     |
| Q2 | 1.87%     | Q6 | 1.94%     |   | Q2 | 2.37%     |
| Q3 | 2.03%     | Q7 | 2.43%     |   | Q5 | 3.14%     |
| Q4 | 2.11%     |    |           | ] | Q6 | 2.74%     |

SD is computed over all such tuples. This process is continued over all epochs and SD is reported in Table 12. We report the accuracy of probability estimation in Table 12 (a) and cardinality estimation (for join queries) in Table 12 (b). These results highlight that JENNER provides accurate estimation for both the metrics.

#### **5 RELATED WORKS**

JENNER is related to several lines of prior research work. Progressive query answering was explored in approximate processing of aggregate queries [30]. The techniques offer error bounds based on sampling [6, 48] that improves when larger samples are used. However, they do not consider the problem of enrichment during query processing and cannot be used in our setting. Progressive data processing has also been considered in data cleaning contexts such as in entity resolution [9, 10, 42, 47]. JENNER adapted the metric for progressive enrichment from these works. Since JENNER explores progressive enrichment during query processing, it differs from these works as they did not consider progressive data cleaning in the context of queries. As mentioned in §1, data cleaning during query processing has been studied in [51]. However, such works did not consider progressive data processing. Recently, in [5] we explored a complementary challenge of supporting enrichment during query processing: using a loose design (enrichment inside a middleware) and a tight design (enrichment in DBMS). However, [5] does not consider the problem of ordering enrichment functions to optimize enrichment during progressive query processing as addressed in this paper. JENNER is also related to expensive predicate optimization of [35, 36, 40] which focused on predicate reordering during query processing to minimize cost. In contrast, JENNER focused on progressive enrichment during query processing.

#### 6 CONCLUSIONS

We described an approach that optimizes data enrichment with progressive query processing. JENNER overcomes several limitations of both offline and at-ingest enrichment by optimally integrating enrichment during query processing. To overcome the increased query latency, JENNER exploits trade-off between quality and efficiency that is implicit in the realization of enrichment functions that are typically based on machine learning/signal processing techniques. Furthermore, JENNER hides latency by supporting progressive query answering that refines as data gets enriched. Our experiments validate the improvement achieved by JENNER over naive strategies to support progressiveness in query processing.

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